

Combined Analysis

texture, structure, microstructure, phase, stresses and reflectivity investigations of real multi-phased ceramics and thin structures using scattering of rays

Daniel Chateigner

CRISMAT-ENSICAEN (Caen-France)

Bi2223
Superconductors

PCT
Ferroelectrics

Irradiated
Fap ceramics

$\text{Ca}_3\text{Co}_4\text{O}_9$
Thermoelectrics

nano-Si
thin films

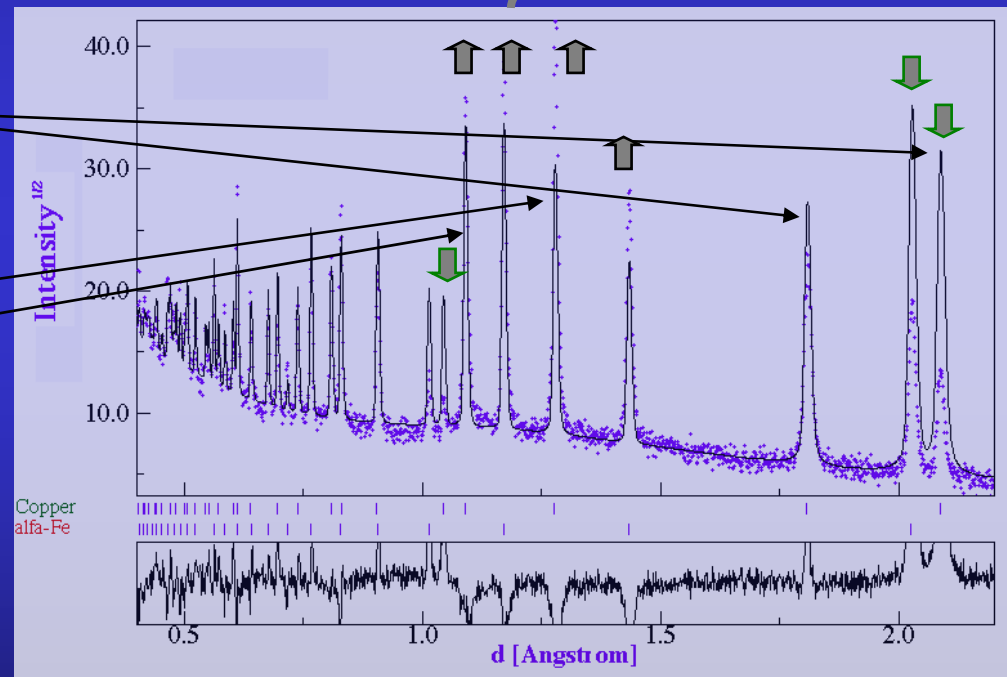
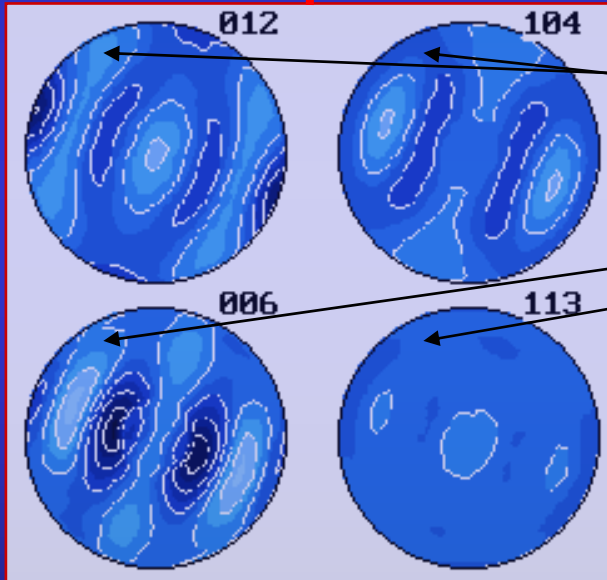
AlN/Pt/Ni(Co)
thick films

Texture from Spectra

Orientation Distribution Function (ODF)

From pole figures

From spectra



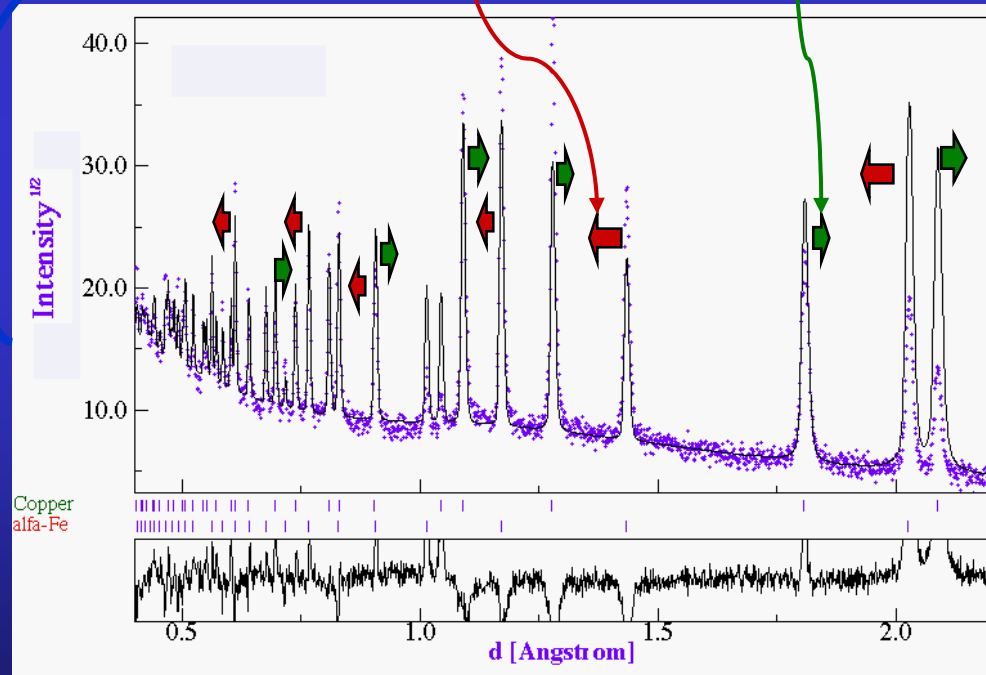
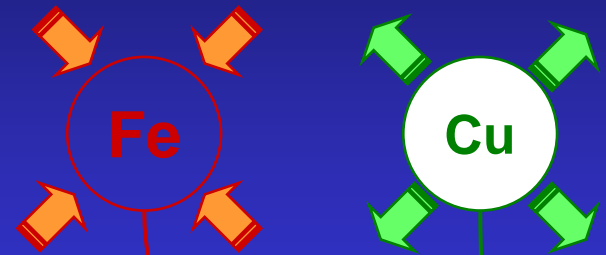
Residual Stresses and Rietveld

- Macro elastic strain tensor (I kind)
- Crystal anisotropic strains (II kind)

IC

Macro and micro stresses

Applied macro stresses



Textured samples: Reuss, Voigt, Hill, Bulk geometric mean approaches

How it works

Le Bail extraction

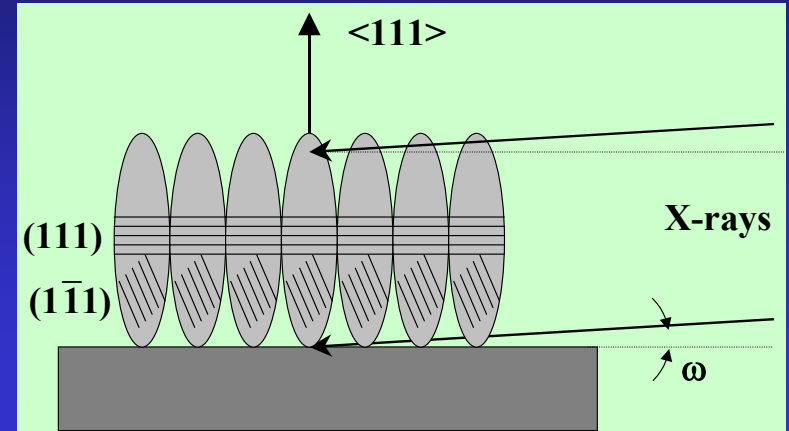
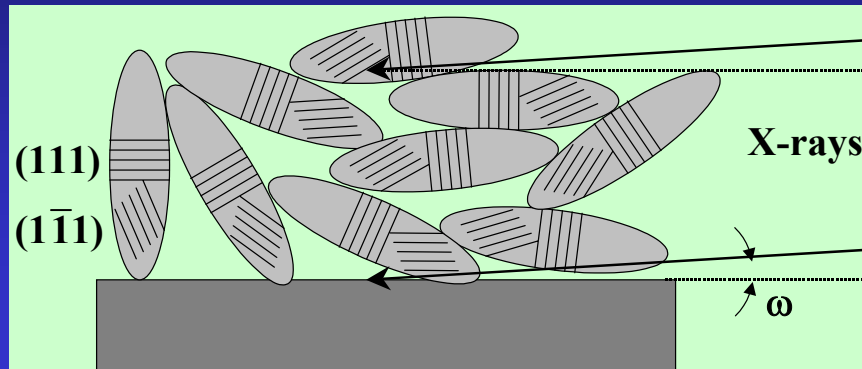
$$T_{hkl}^k = T_{hkl}^{k-1} \frac{\sum_i I_i^{\text{exp}} S_{hkl}^i}{\sum_i I_i^{\text{calc}} S_{hkl}^i}$$

- Starts with nominal intensities (T_{hkl})
 - Computes the full pattern (I^{calc})
 - Uses the formula to compute next T_{hkl}
 - Cycle the last two steps until convergence
-
- In Maud, options:
 - Only few cycles for texture (3-5) necessary
 - The range for the weighting of the profile can be reduced
 - Background subtracted or not

Minimization algorithms

- Can be fully used in the method (everywhere)
- **Marquardt Least Squares** (based on steepest decrease and Gauss-Newton)
 - Efficient, best with few parameters, near the solution
- **Evolutionary computation** (or genetic algorithm)
 - Slow, not efficient, requires a lot of resources
 - Unlimited number of parameters
 - Can start far from the solution
- **Simulated annealing** (the solution proceed like a random walk, but the walking step decreases as temperature decreases)
 - In between the Marquardt and evolutionary algorithms
- **Simplex** (generates $n+1$ starting solutions as vertices of a polygon, n number of parameters, and contract/expand the polygon around the minima)
 - Slow on convergence
 - Remains close to the solution, but explore more minima with respect to the Marquardt

Anisotropic sizes and microstrains



- Texture helps the "real" mean shape determination
- Determination by peak deconvolution + Popa formalism

$$\langle R_h \rangle = R_0 + R_1 P_2^0(x) + R_2 P_2^1(x) \cos \varphi + R_3 P_2^1(x) \sin \varphi + R_4 P_2^2(x) \cos 2\varphi + R_5 P_2^2(x) \sin 2\varphi + \dots$$

$$\langle \varepsilon_h^2 \rangle E_h^4 = E_1 h^4 + E_2 k^4 + E_3 l^4 + 2E_4 h^2 k^2 + 2E_5 l^2 k^2 + 2E_6 h^2 l^2 + 4E_7 h^3 k + 4E_8 h^3 l + 4E_9 k^3 h + 4E_{10} k^3 l + 4E_{11} l^3 h + 4E_{12} l^3 k + 4E_{13} h^2 k l + 4E_{14} k^2 h l + 4E_{15} l^2 k h$$

Rietveld-Structure

$$I_i^{calc}(\chi, \phi) = \sum_{n=1}^{Nphases} S_n \sum_k L_k |F_{k;n}|^2 S(2\theta_i - 2\theta_{k;n}) P_{k;n}(\chi, \phi) A + bkg_i$$

Texture

$$P_k(\chi, \phi) = \int_{\varphi} f(g, \varphi) d\varphi$$

- Generalized Spherical Harmonics (Bunge):

$$P_k(\chi, \phi) = \sum_{l=0}^{\infty} \frac{1}{2l+1} \sum_{n=-l}^l k_l^n(\chi, \phi) \sum_{m=-l}^l C_l^{mn} k_n^{*m}(\Theta_k \phi_k)$$

$$f(g) = \sum_{l=0}^{\infty} \sum_{m,n=-l}^l C_l^{mn} T_l^{mn}(g)$$

- Components (Helming):

$$f(g) = F + \sum_c I^c f^c(g)$$

- WIMV (William, Imhof, Matthies, Vinel) iterative process:

$$f^{n+1}(g) = N_n \frac{f^n(g) f^0(g)}{\left(\prod_{h=1}^I \prod_{m=1}^{M_h} P_h^n(\mathbf{y}) \right)^{\frac{1}{IM_h}}}$$

$$f^0(g) = N_0 \left(\prod_{h=1}^I \prod_{m=1}^{M_h} P_h^{\text{exp}}(\mathbf{y}) \right)^{\frac{1}{IM_h}}$$

E-WIMV (Rietveld only):

with $0 < r_n < 1$, relaxation parameter,
 M_h number of division points of the integral
 around k ,
 w_h reflection weight

$$f^{n+1}(g) = f^n(g) \prod_{m=1}^{M_h} \left(\frac{P_h(\mathbf{y})}{P_h^n(\mathbf{y})} \right)^{r_n \frac{w_h}{M_h}}$$

- Entropy maximisation (Schaeben):

$$f^{n+1}(g) = f^n(g) \prod_{m=1}^{M_h} \left(\frac{P_h(\mathbf{y})}{P_h^n(\mathbf{y})} \right)^{\frac{r_n}{M_h}}$$

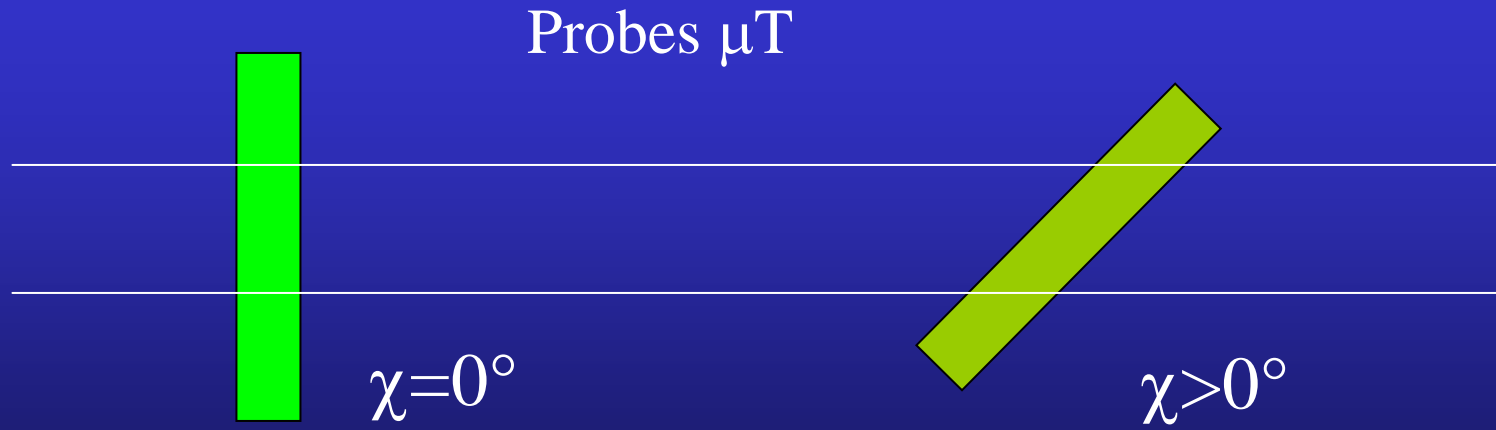
- arbitrarily defined cells (ADC, Pawlik): Very similar to E-WIMV, with integrals along path tubes

Layering

Asymmetric Bragg-Brentano

$$C_{\chi}^{\text{top film}} = g_1 (1 - \exp(-\mu T g_2 / \cos \chi)) / (1 - \exp(-2\mu T / \sin \omega \cos \chi))$$

$$C_{\chi}^{\text{cov. layer}} = C_{\chi}^{\text{top film}} \left(\exp(-g_2 \sum \mu_i' T_i' / \cos \chi) \right) / \left(\exp(-2 \sum \mu_i' T_i' / \sin \omega \cos \chi) \right)$$



Specular reflectivity: $\mathbf{q}=(0,0,z)$

- Fresnel:

$$R(\mathbf{q}) = \left| \frac{q_z - \sqrt{q_z^2 - q_c^2 + \frac{32i\pi^2\beta}{\lambda^2}}}{q_z + \sqrt{q_z^2 - q_c^2 + \frac{32i\pi^2\beta}{\lambda^2}}} \right|^2 \delta q_x \delta q_y$$

- matrix:

$$R^{flat} = \frac{r_{0,1}^2 + r_{1,2}^2 + 2r_{0,1}r_{1,2} \cos 2k_{z,1}h}{1 + r_{0,1}^2 r_{1,2}^2 + 2r_{0,1}r_{1,2} \cos 2k_{z,1}h}$$

- Born approximation:

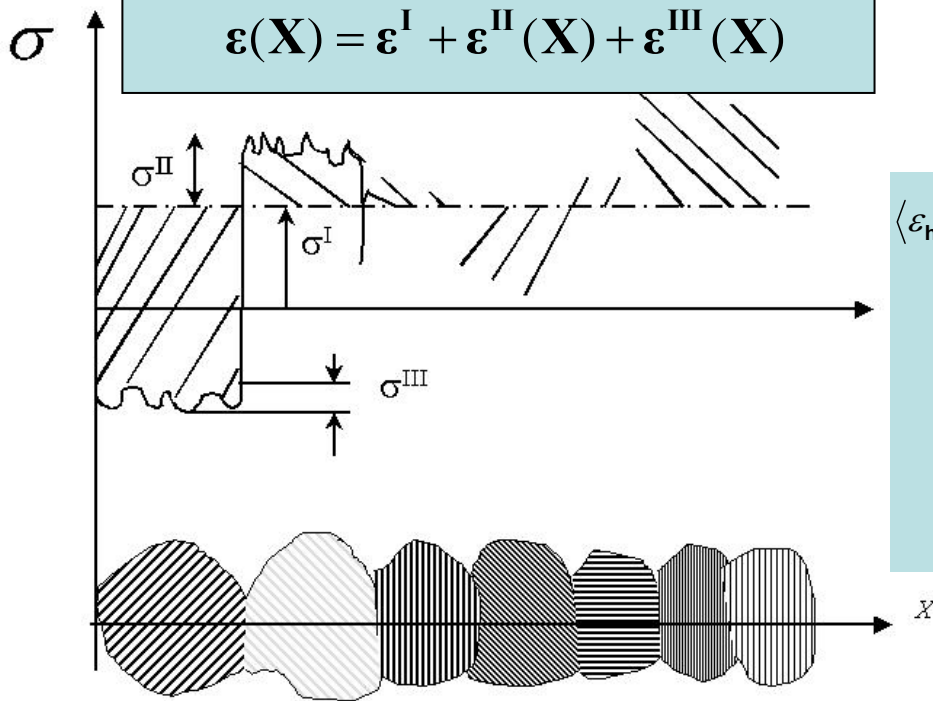
$$R(q_z) = r \cdot r^* = R_F(q_z) \left| \frac{1}{\rho_s} \int_{-\infty}^{+\infty} \frac{d\rho(z)}{dz} e^{iq_z z} dz \right|^2$$

- Roughness:

$$R^{rough}(q_z) = R(q_z) \exp(-q_{z,0} q_{z,1} \sigma^2) \quad \text{Low-angles (reflectivity)}$$

$$S_R = 1 - p \exp(-q) + p \exp\left(\frac{-q}{\sin \theta}\right) \quad \text{high-angle (Suortti)}$$

Strain-Stress



Isotropic samples:
triaxial, biaxial uniaxial stress state

$$\begin{aligned} \langle \varepsilon_{\mathbf{h}}(\mathbf{y}) \rangle_{V_d} &= \frac{1}{V_d} \int_{V_d} (\varepsilon_{33}^I + \varepsilon_{33}^{II} + \varepsilon_{33}^{III}) dV \\ &= (\varepsilon_{11}^I \cos^2 \phi + \varepsilon_{12}^I \sin 2\phi + \varepsilon_{22}^I \sin^2 \phi - \varepsilon_{33}^I) \sin^2 \psi + \varepsilon_{33}^I + \\ &\quad (\varepsilon_{13}^I \cos \phi + \varepsilon_{23}^I \sin \phi) \sin 2\psi + \frac{1}{V_d} \int_{V_d} (\varepsilon_{33}^{IIe} + \varepsilon_{33}^{IIIi} + \varepsilon_{33}^{IIIpi}) dV \\ &= \frac{\langle d(hkl, \phi, \psi) \rangle_{V_d} - d_0(hkl)}{d_0(hkl)} \end{aligned}$$

Textured samples:
triaxial, biaxial uniaxial stress state
+ ODF + SDF + model

$$\chi^2 = \sum_i w_i^2 \left[\varepsilon_i^{calc}(S_{ijkl}^M, \mathbf{h}, \mathbf{y}) - \varepsilon_i^{meas}(S_{ijkl}^M, \mathbf{h}, \mathbf{y}) \right]^2$$

Non-linear least-square fit

$$\begin{aligned} \langle E(\mathbf{g}) \rangle_{V_d} &= \frac{1}{V_d} \int_{V_d} E^{SC}(\mathbf{g}) f(\mathbf{g}) d\mathbf{g} \\ &= \left(\prod_{V_d} E^{SC}(\mathbf{g}) f(\mathbf{g}) d\mathbf{g} \right)^{\frac{1}{V_d}} \end{aligned}$$

Phase analysis

- Volume fraction

$$V_{\Phi} = \frac{S_{\Phi} V_{uc\Phi}^2}{\sum_{\Phi} (S_{\Phi} V_{uc\Phi}^2)}$$

- Weight fraction

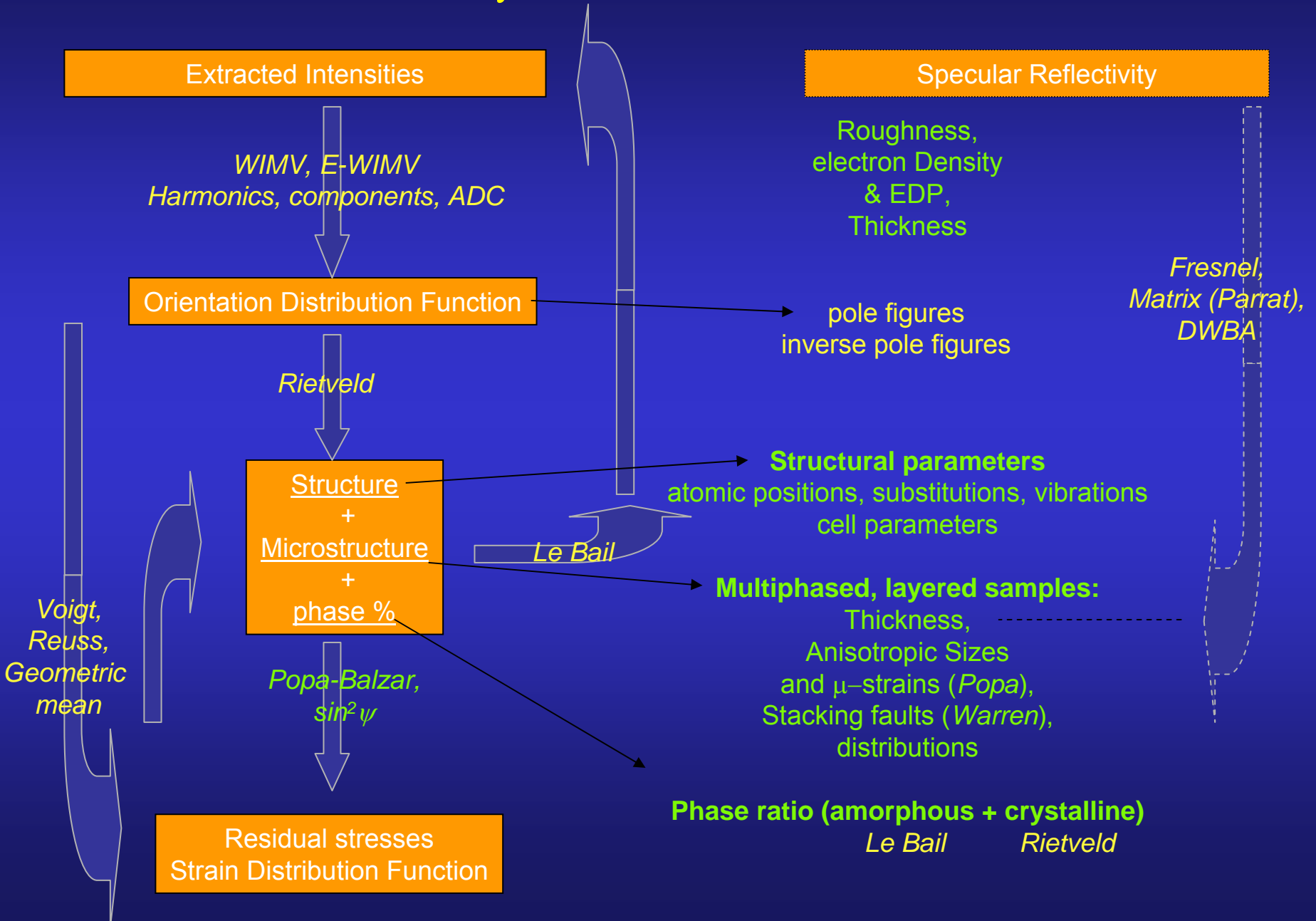
$$m_{\Phi} = \frac{S_{\Phi} Z_{\Phi} M_{\Phi} V_{uc\Phi}^2}{\sum_{\Phi} (S_{\Phi} Z_{\Phi} M_{\Phi} V_{uc\Phi}^2)}$$

Z = number of formula units

M = mass of the formula unit

V = cell volume

Implemented codes



Minimum experimental requirements

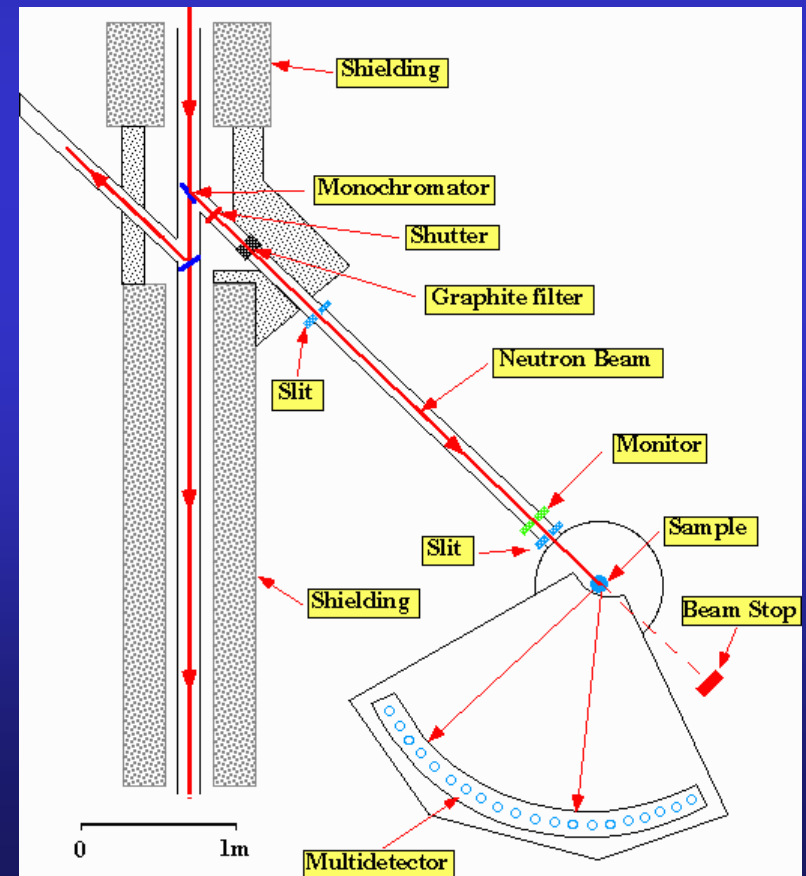
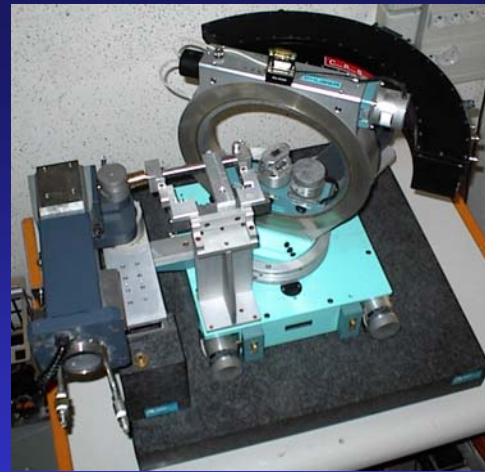
1D or 2D Detector + 4-circle diffractometer
(X-rays and neutrons)
CRISMAT, ILL

+

~1000 experiments (2θ diagrams)
in as many sample orientations

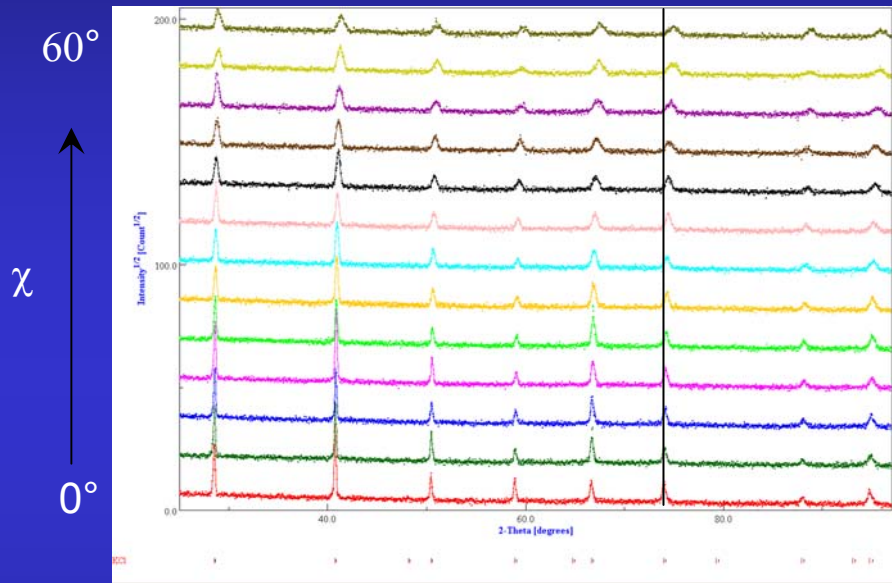
+

Instrument calibration
(peaks widths and shapes,
misalignments, defocusing ...)

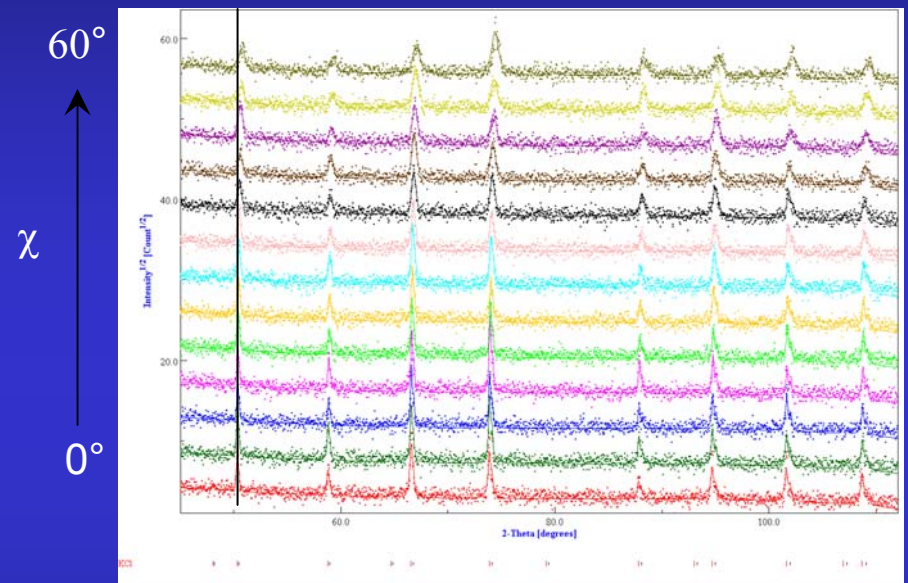


Calibration

$\omega = 20^\circ$



$\omega = 40^\circ$



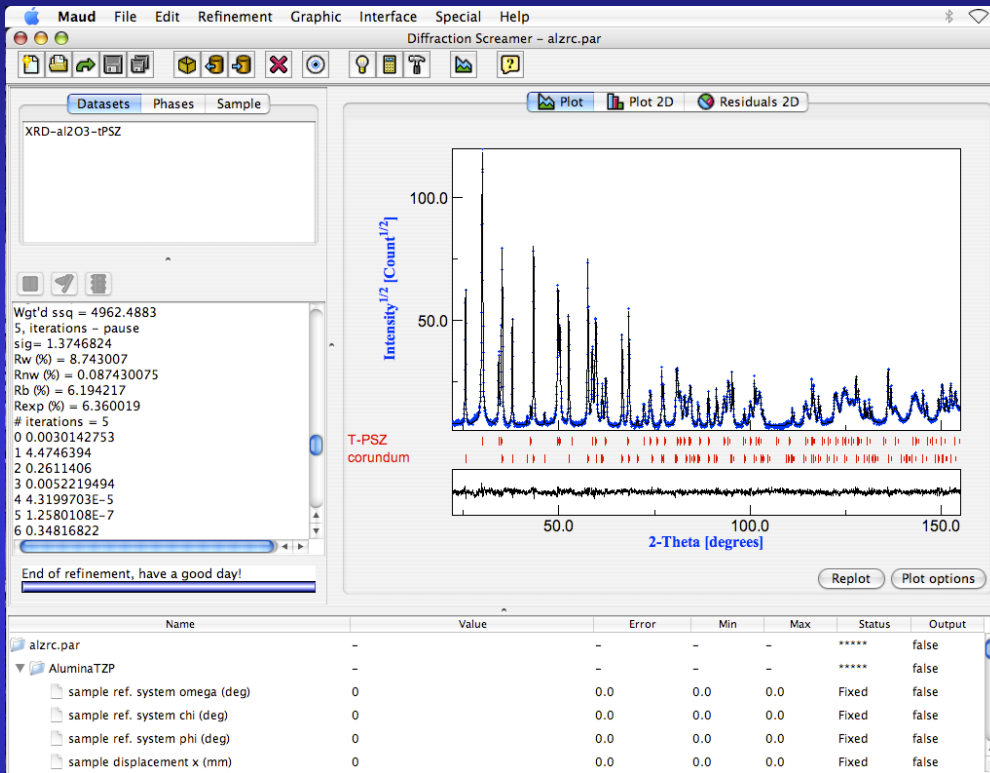
KCl, LaB₆ ...



FWHM (ω , χ , 2θ ...)
2 θ shift
gaussianity
asymmetry
misalignments ...

Methodology implementation

L. Lutterotti, Trento



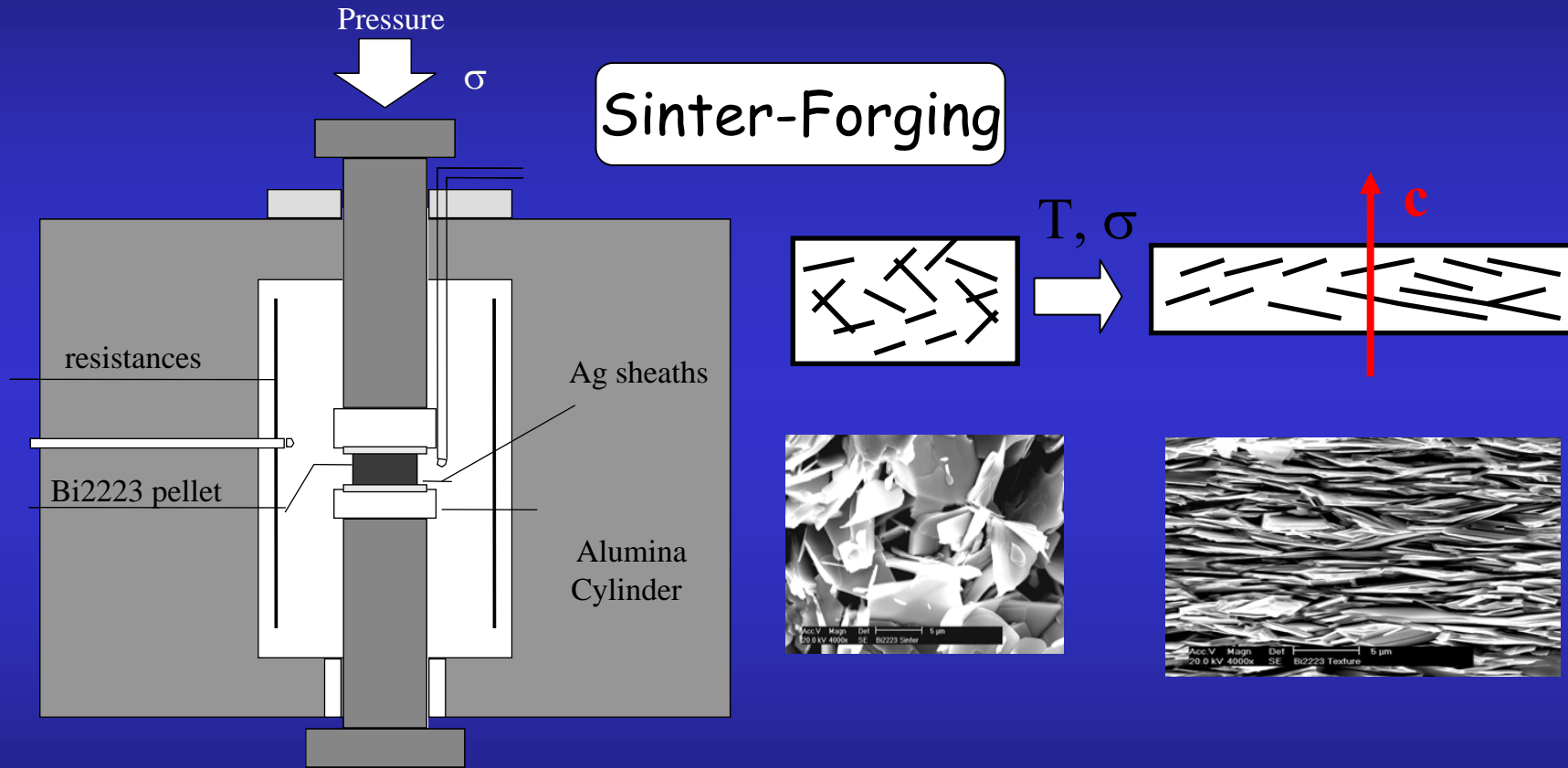
User friendly interface

Java codes

Java web start updates

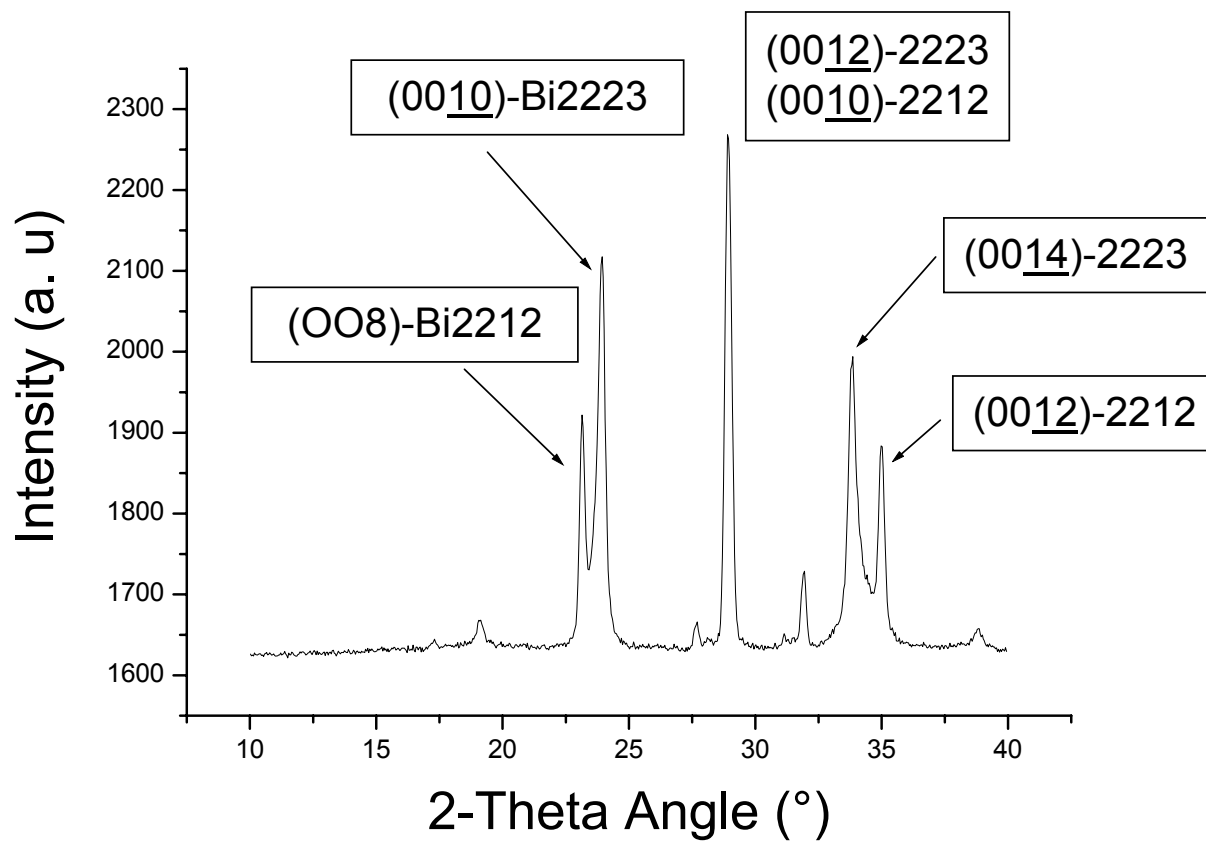
Bi2223 compounds

E. Guilmeau, PhD

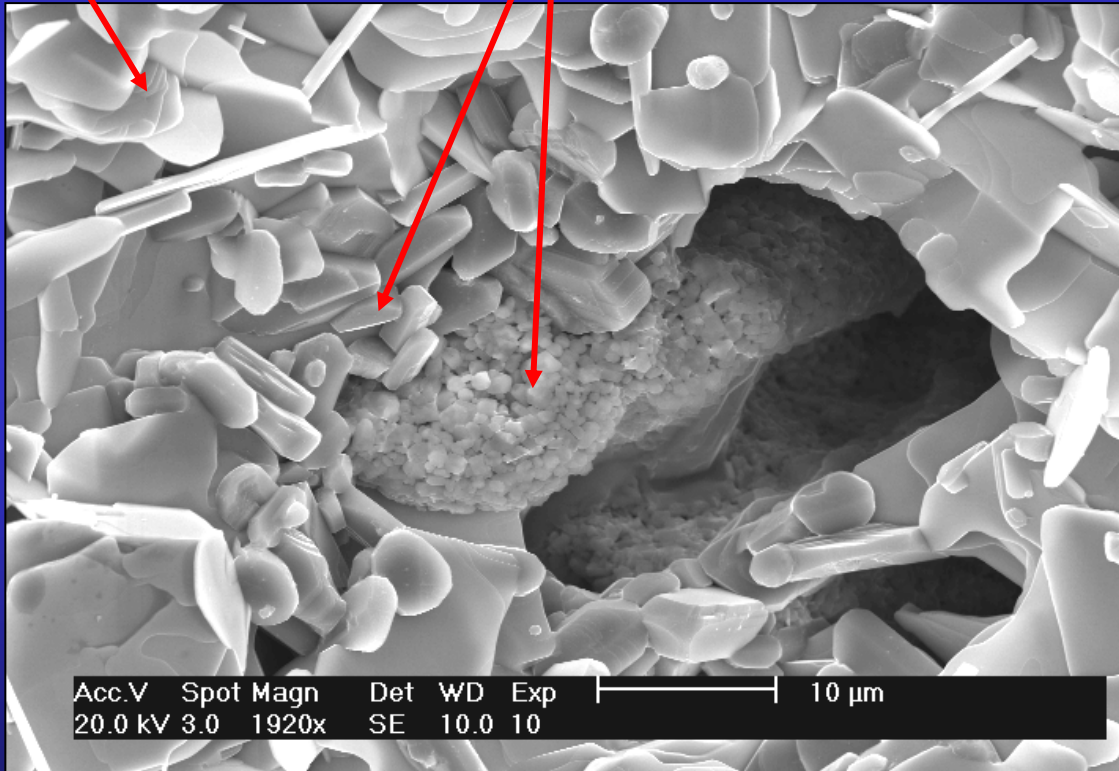


Grain alignment \Rightarrow J_c

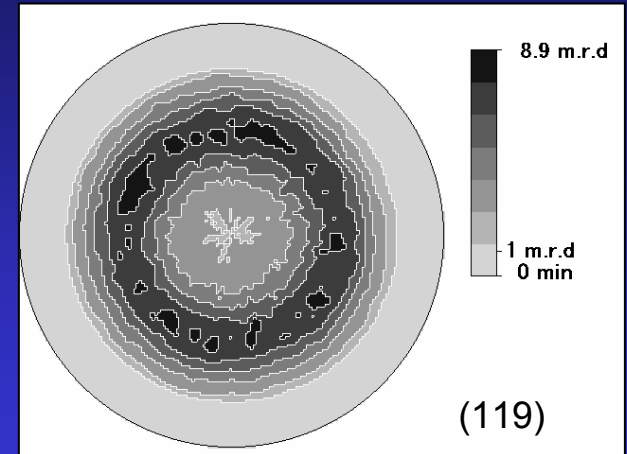
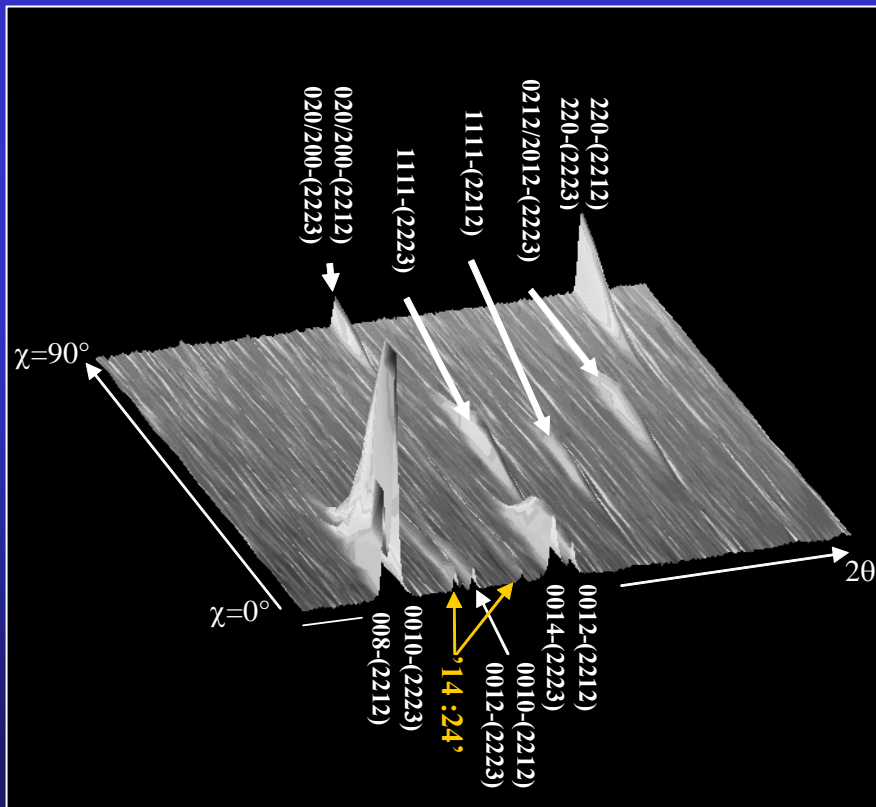
(00 l) Texture



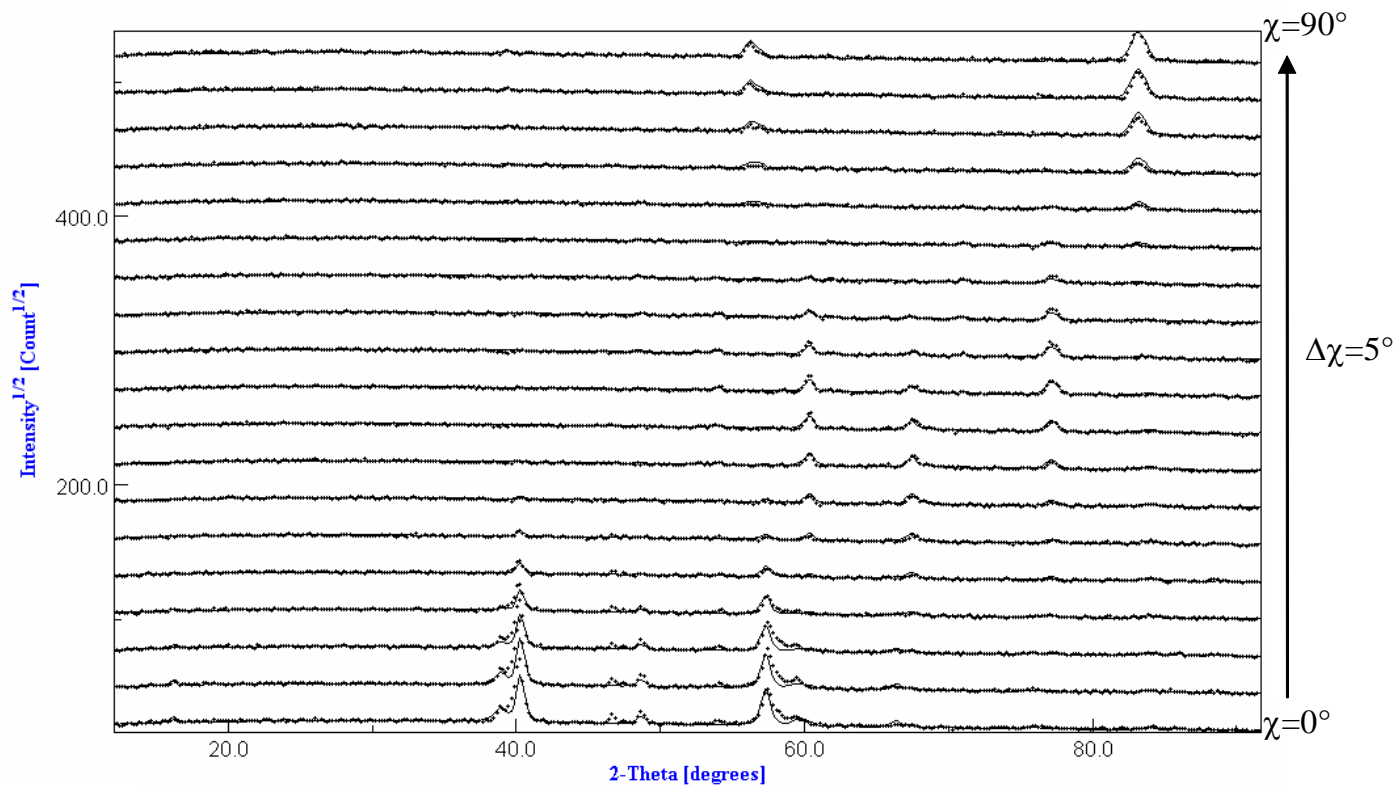
Bi2212 + Secondary phases \longrightarrow Bi2223



Combined Analysis



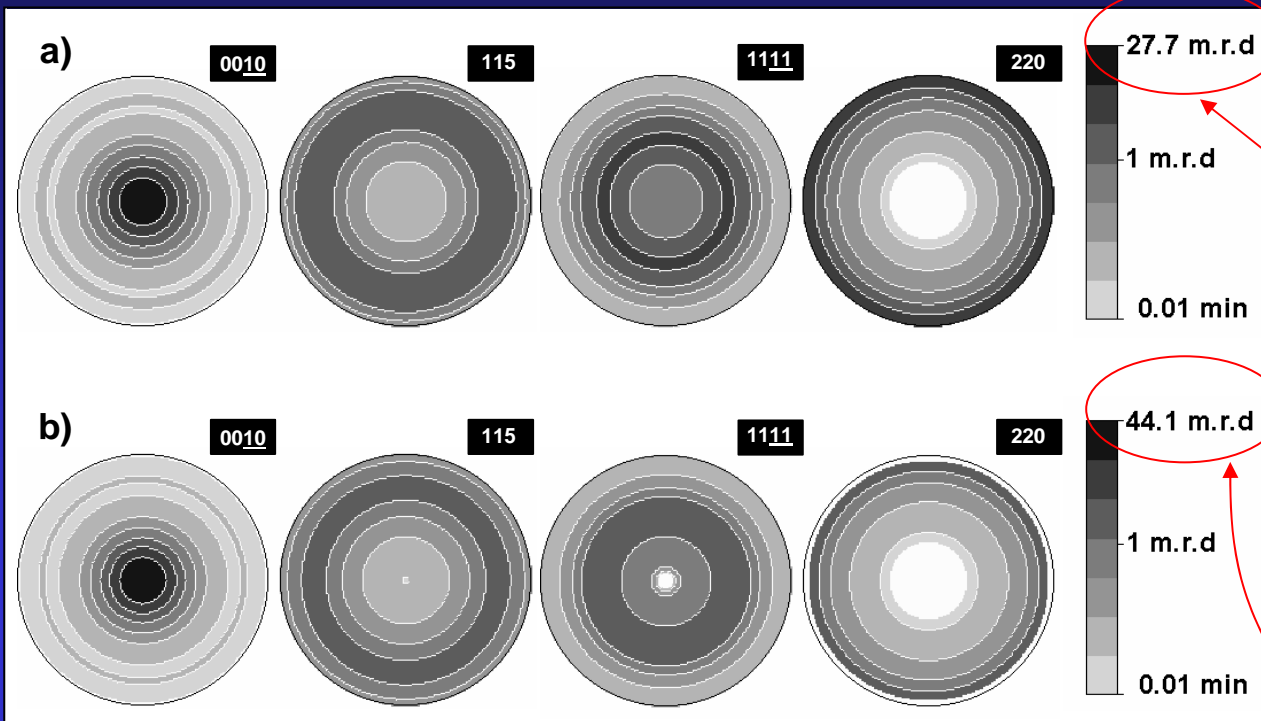
- Neutrons
- Sample: $\sim 70 \text{ mm}^3$
- 2θ patterns for $\chi=0^\circ$ to 90°
- No ϕ rotation (fibre texture).



2223
2212



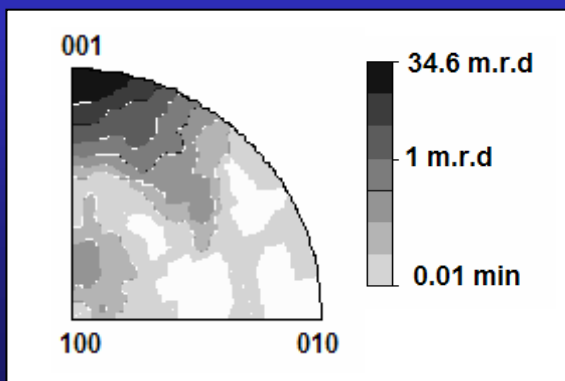
R_w=9.12
R_P=16.24



*Recalculated
(WIMV)*

*Extracted
(Le Bail)*

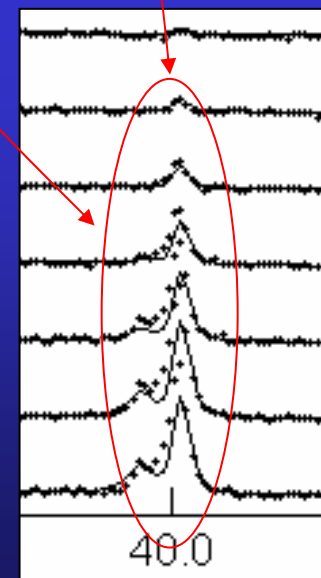
Logarithmic density scale, equal area projection



Logarithmic density scale, equal area projection

Stacking faults and/or intergrowth on the c-axis
 → New periodicities and peaks characterized with intermediate c parameters.

However, no algorithm is included to solve intergrowths in the combined approach.



40.0

Effect of the sinter-forging treatment on the texture development, crystal growth, transport properties

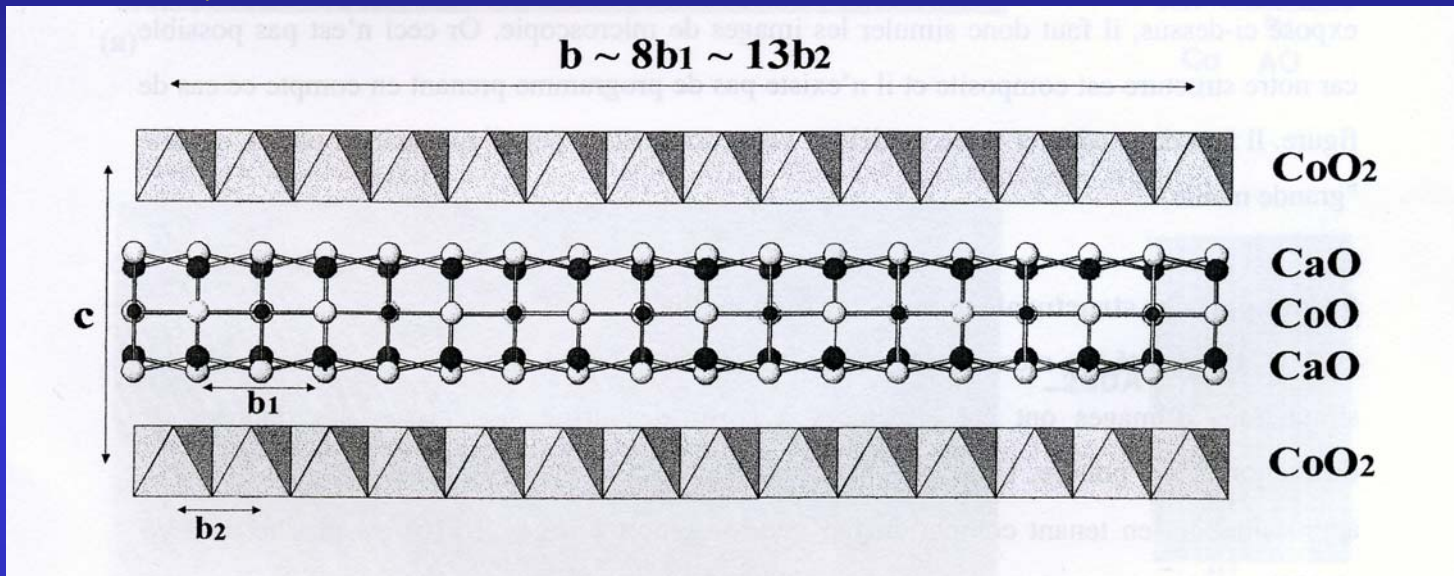
Sinter-forging dwell time (h)	Orientation Distribution Max (m.r.d.)		% Bi2223	Cell parameters (Å)		Crystallite size Bi2223 (nm)	Rb (%)	Rw (%)	Rexp (%)	RP0 (%)	RP1 (%)	J _c (A/cm ²)
	Bi2212	Bi2223		Bi2223	Bi2212							
20	21.8	20.7	59.9±1.3	a=5.419(3) b=5.391(3) c=37.168(3)	a=5.414(3) b=5.393(3) c=30.800(3)	205±7	7.56	11.1	4.55	17.74	10.56	12500
50	24.1	24.4	72.9±2.9	a=5.419(3) b=5.408(3) c=37.192(3)	a=5.416(3) b=5.396(3) c=30.806(3)	273±10	7.54	11.37	4.58	17.05	11.04	15000
100	31.5	25.2	84.4±4.6	a=5.410(3) b=5.405(3) c=37.144(3)	a=5.412(3) b=5.403(3) c=30.752(3)	303±10	5.4	8.04	3.69	13.54	9.31	19000
150	65.4	27.2	87.0±4.1	a=5.417(3) b=5.403(3) c=37.199(3)	a=5.413(3) b=5.407(3) c=30.792(3)	383±13	6.13	9.12	4.8	16.24	12.25	20000



$Ca_3Co_4O_9$ thermoelectrics

J.G. Noudem, Caen

$Ca_3Co_4O_9$: Misfit lamellar and modulated Structure, with high thermopower



Two monoclinic sub-systems:

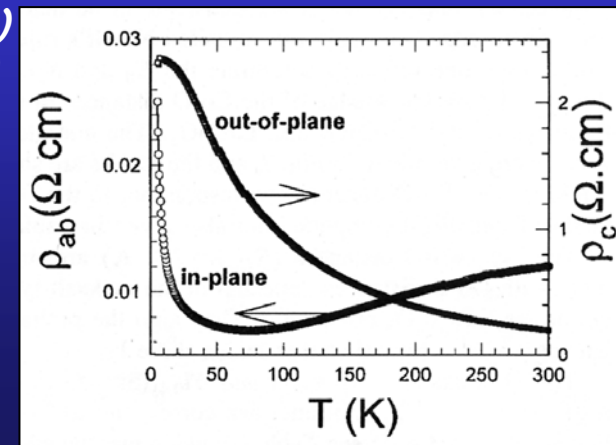
S1 with $a \sim 4.8\text{\AA}$, $b_1 \sim 4.5\text{\AA}$, $c \sim 10.8\text{\AA}$ et $\beta \sim 98^\circ$ (NaCl-type)

S2 with $a \sim 4.8\text{\AA}$, $b_2 \sim 2.8\text{\AA}$, $c \sim 10.8\text{\AA}$ et $\beta \sim 98^\circ$ (CdI_2 -type)

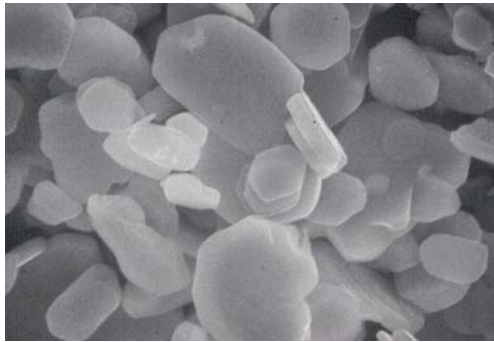
$$\Gamma = \sigma_{ab} / \sigma_c \sim 10$$



Texture

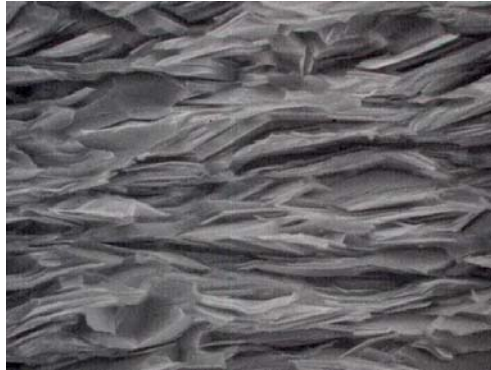


powder



10 μ m

Textured bulk

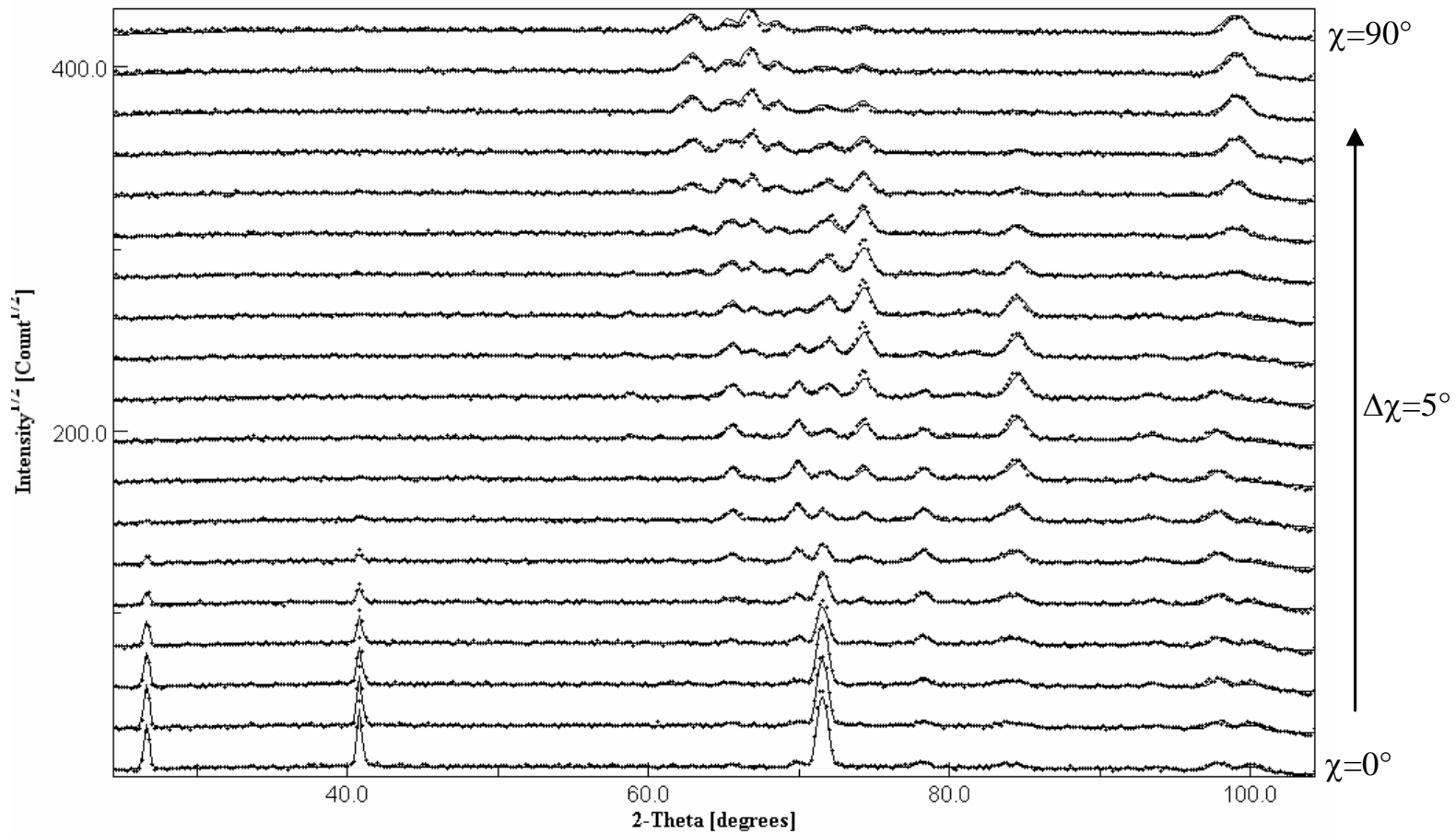


10 μ m

*Magnetic alignment
and
Templated Growth
method*

Analysis:

- neutrons
- 3D Supercell: $a=4.8309\text{\AA}$, $b\sim 8b1\sim 13b2\sim 36.4902\text{\AA}$, $c=10.8353\text{\AA}$, $\beta=98.13^\circ$
174 atoms/cell
- Sample : 0.6 cm^3

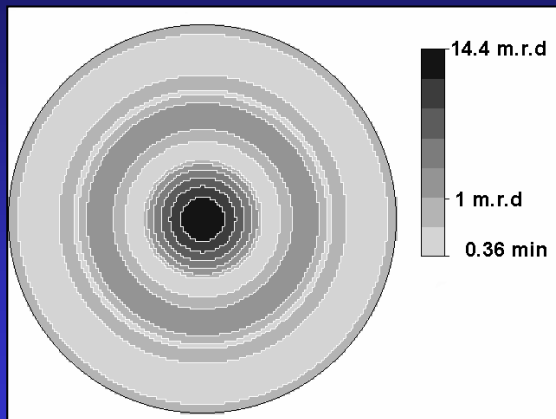


Supercell

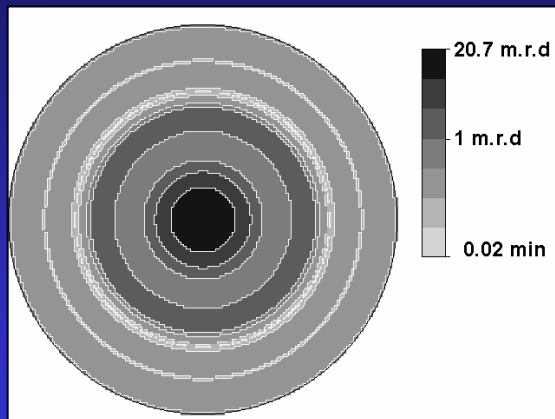


RP=19.7%, Rw=11.9%

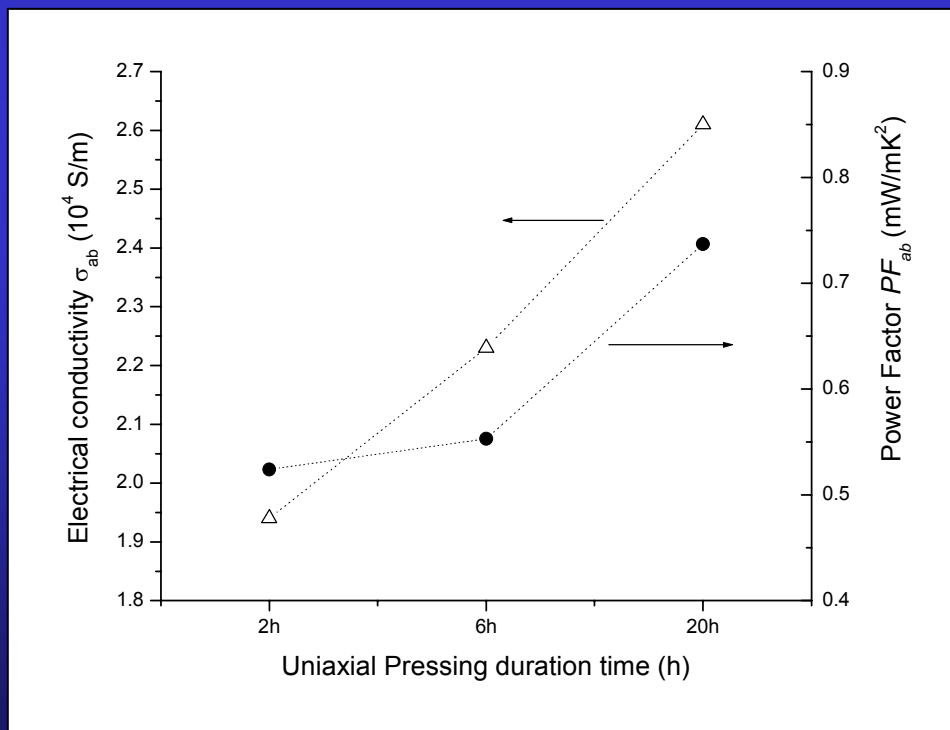
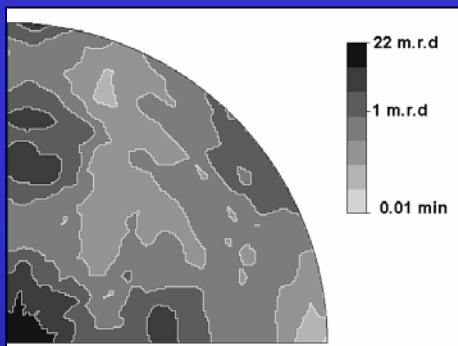
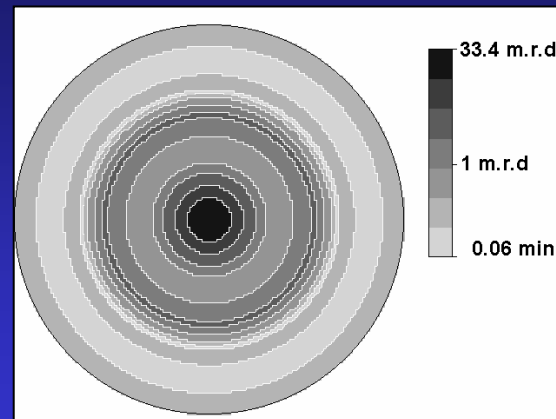
9.8 MPa for 2 h



19.6 MPa for 6 h

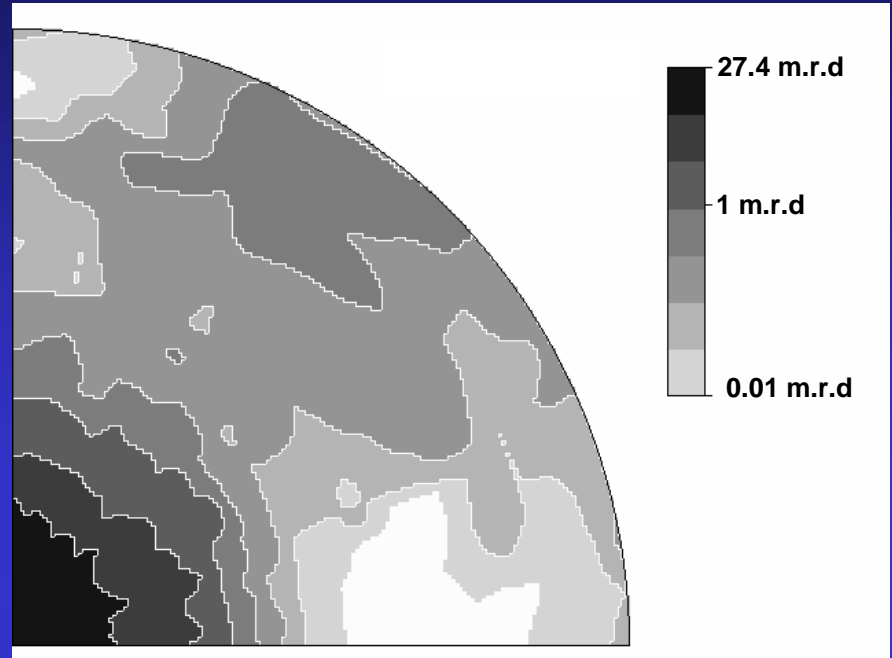


19.6 MPa for 20 h



Templated Growth Method

Logarithmic density scale, equal area projection



Magnetic Alignment



- *magnetic alignment really efficient to obtain strong textures*
- *combined analysis of modulated structures possible*

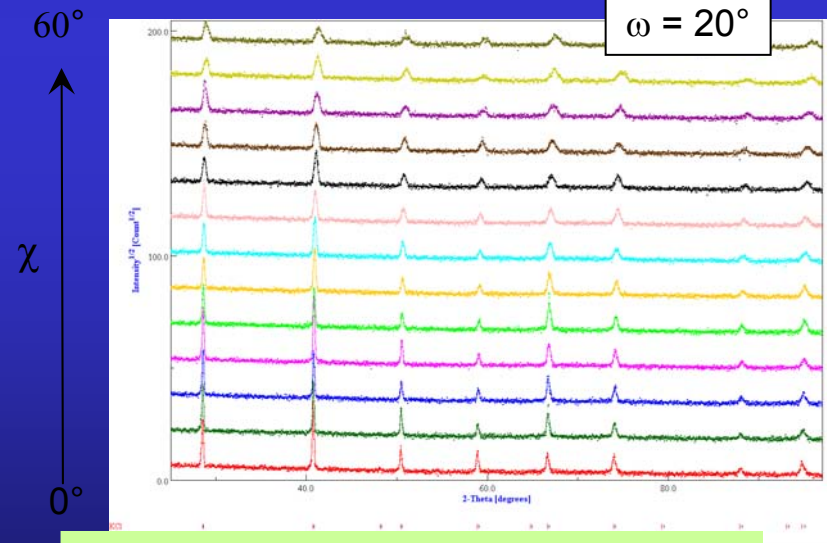
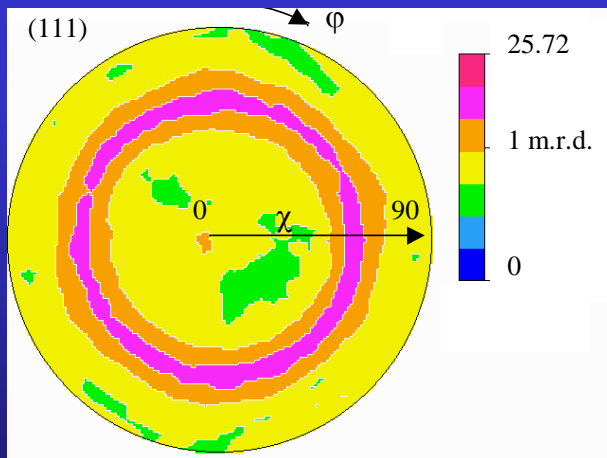
Ferroelectric PCT films

J. Ricote, Madrid

thin films:

$(\text{Ca}_{0.24}\text{Pb}_{0.76})\text{TiO}_3$ sol-gel synthesised solutions deposited by spin coating on a substrate of $\text{Pt}/\text{TiO}_2/\text{Si}$, with and without a treatment at 650°C for 30 min.

All films are crystallised at 700°C for 50 s by Rapid Thermal Processing (RTP; $30^\circ\text{C}/\text{s}$). A series is also recrystallised at 650°C for 1 to 3 h.



Refinement of individual spectra

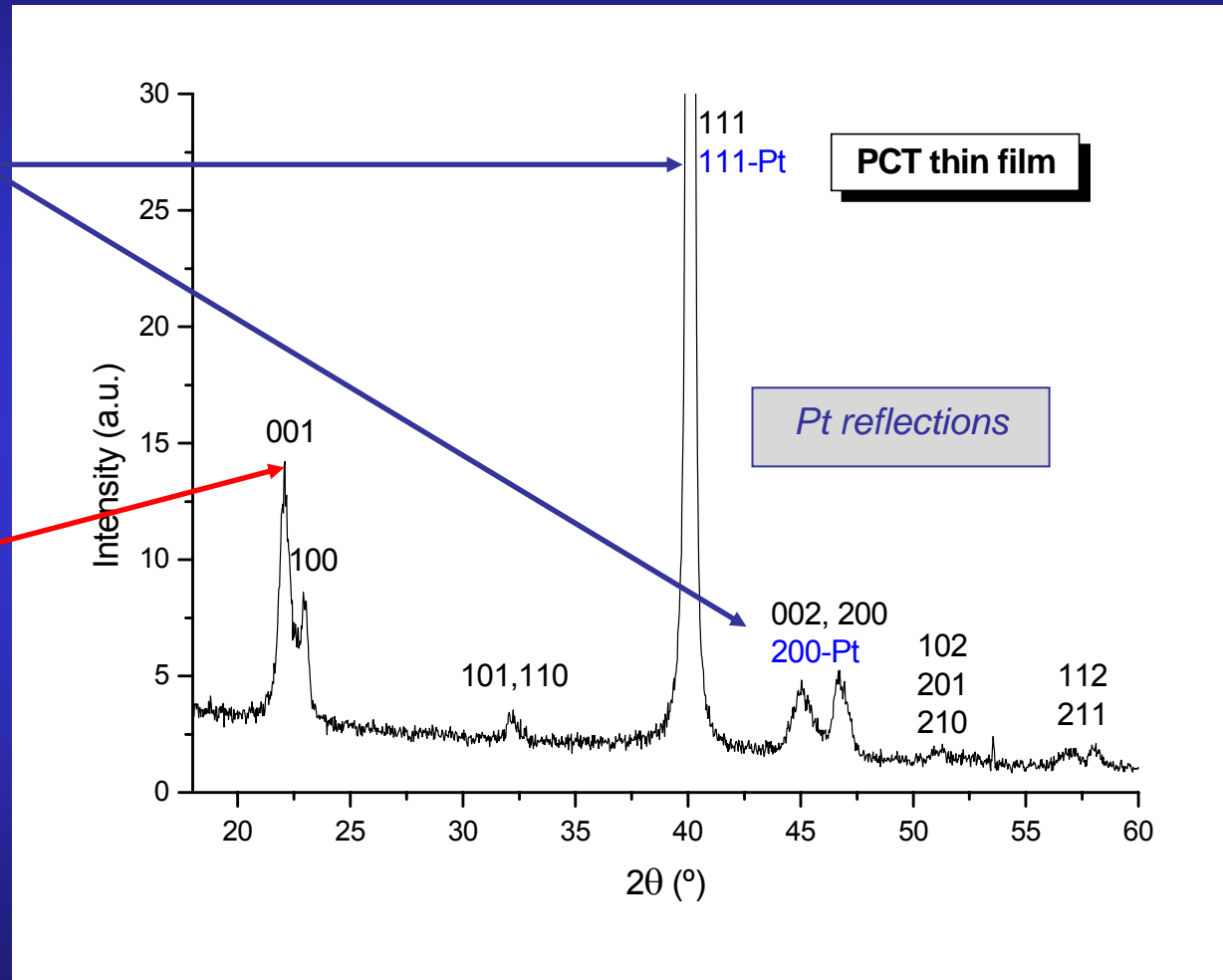
Limitations of the simple Quantitative Texture Analysis

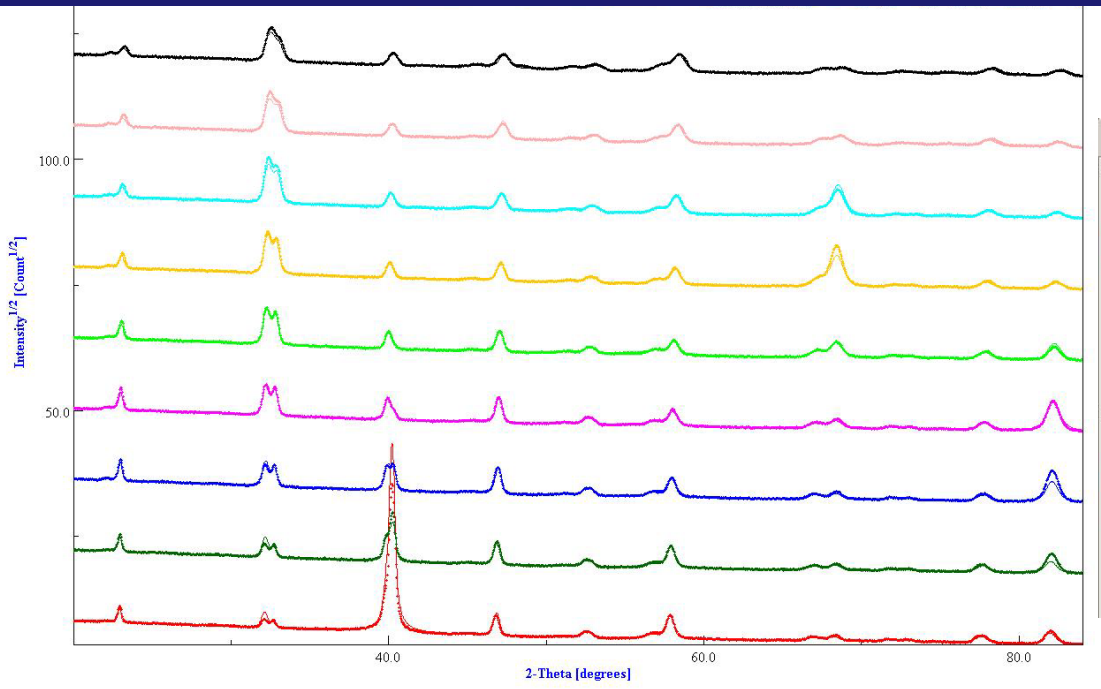
Structural parameters are difficult to obtain due to:

Substrate influence:

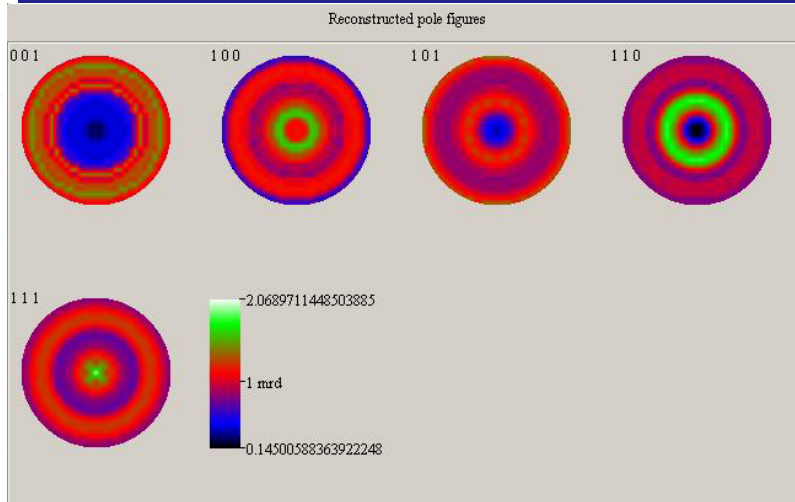
overlapping of reflections from the film and the substrate

TEXTURE effects:
peaks that do not appear at low χ angles

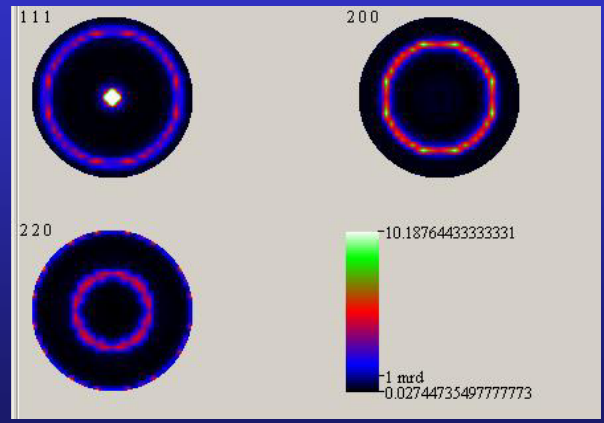




PCT



Pt

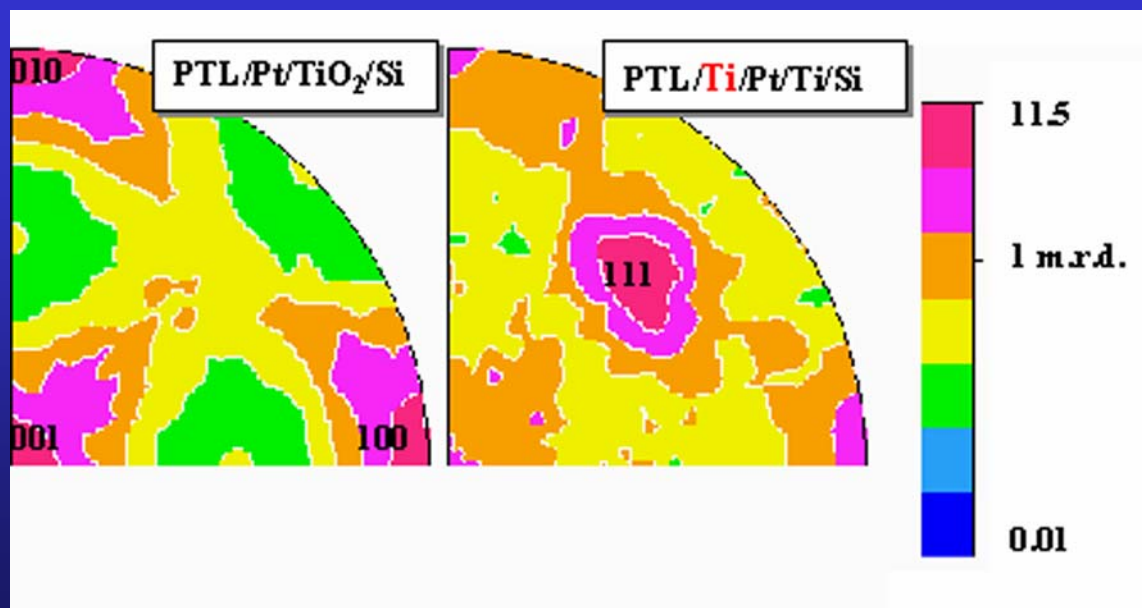


$a = 3.9108(1) \text{ \AA}$
 $T = 457(3) \text{ \AA}$
 $t_{\text{iso}} = 458(3) \text{ \AA}$
 $\epsilon' = 0.0032(1) \text{ rms}$

$a = 3.9156(1) \text{ \AA}$
 $c = 4.0497(3) \text{ \AA}$
 $T = 2525(13) \text{ \AA}$
 $t_{\text{iso}} = 390(7) \text{ \AA}$
 $\epsilon = 0.0067(1) \text{ rms}$

$R_W = 13\%$; $R_B = 12\%$; $R_{\text{exp}} = 22\%$.(Rietveld)
 $R_W = 5\%$; $R_B = 6\%$ (E-WIMV)

Atom	Occupancy	x	y	z
Pb	0.76	0.0	0.0	0.0
Ca	0.24	0.0	0.0	0.0
Ti	1.0	0.5	0.5	0.477(2)
O1	1.0	0.5	0.5	0.060(2)
O2	1.0	0.0	0.5	0.631(1)



Structural parameters

Pt layer

	a (Å)	thickness (nm)	R factors (%)
non-treated substrate			
Pt	3.9108(1)	45.7(3)	$R_W=13, R_B=12, R_{exp}=22$
annealed substrate			
Pt	3.9100(4)	46.4(3)	$R_W=8, R_B=14, R_{exp}=21$
Pt (Recryst. 1h)	3.9114(2)	47.8(3)	$R_W=9, R_B=20, R_{exp}=21$
Pt (Recryst. 2h)	3.9068(1)	46.9(3)	$R_W=9, R_B=14, R_{exp}=22$
Pt (Recryst. 3h)	3.9141(4)	47.5(9)	$R_W=27, R_B=12, R_{exp}=21$

Annealing of the substrate does not introduce significant variations on the structure of the Pt layer

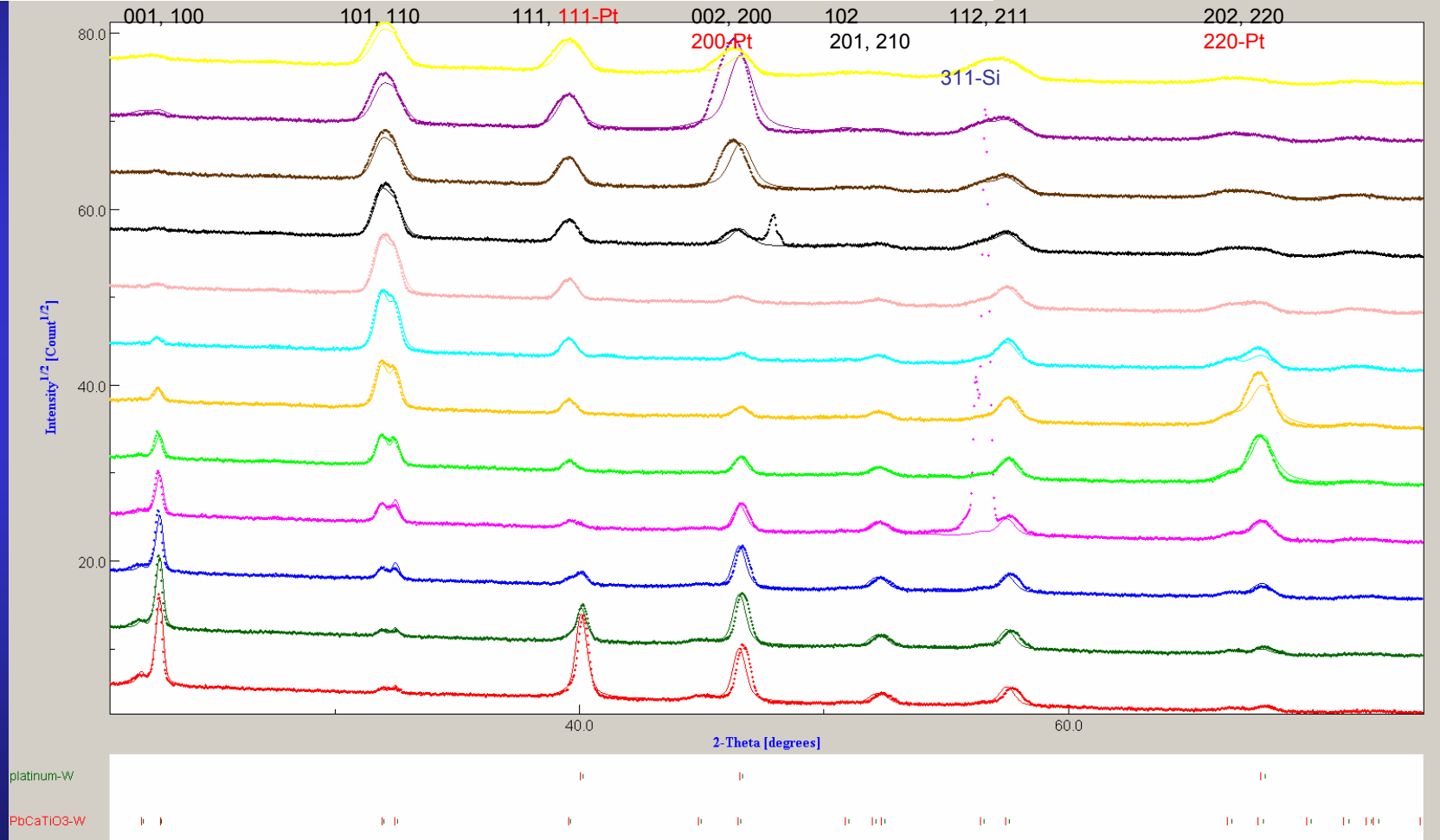
PTC film

	a (Å)	c (Å)	thickness (nm)
on non-treated substrate			
PCT	3.9156(1)	4.0497(6)	272.5(13)
on annealed substrate			
PCT	3.8920(6)	4.0187(8)	279.0(9)
PCT (Recryst. 1h)	3.8929(2)	4.0230(4)	266.1(11)
PCT (Recryst. 2h)	3.8982(2)	4.0227(4)	258.4(9)
PCT (Recryst. 3h)	3.9001(4)	4.0228(11)	253.6(29)

Recrystallisation reduces the stress on the film, and, increases the lattice parameters

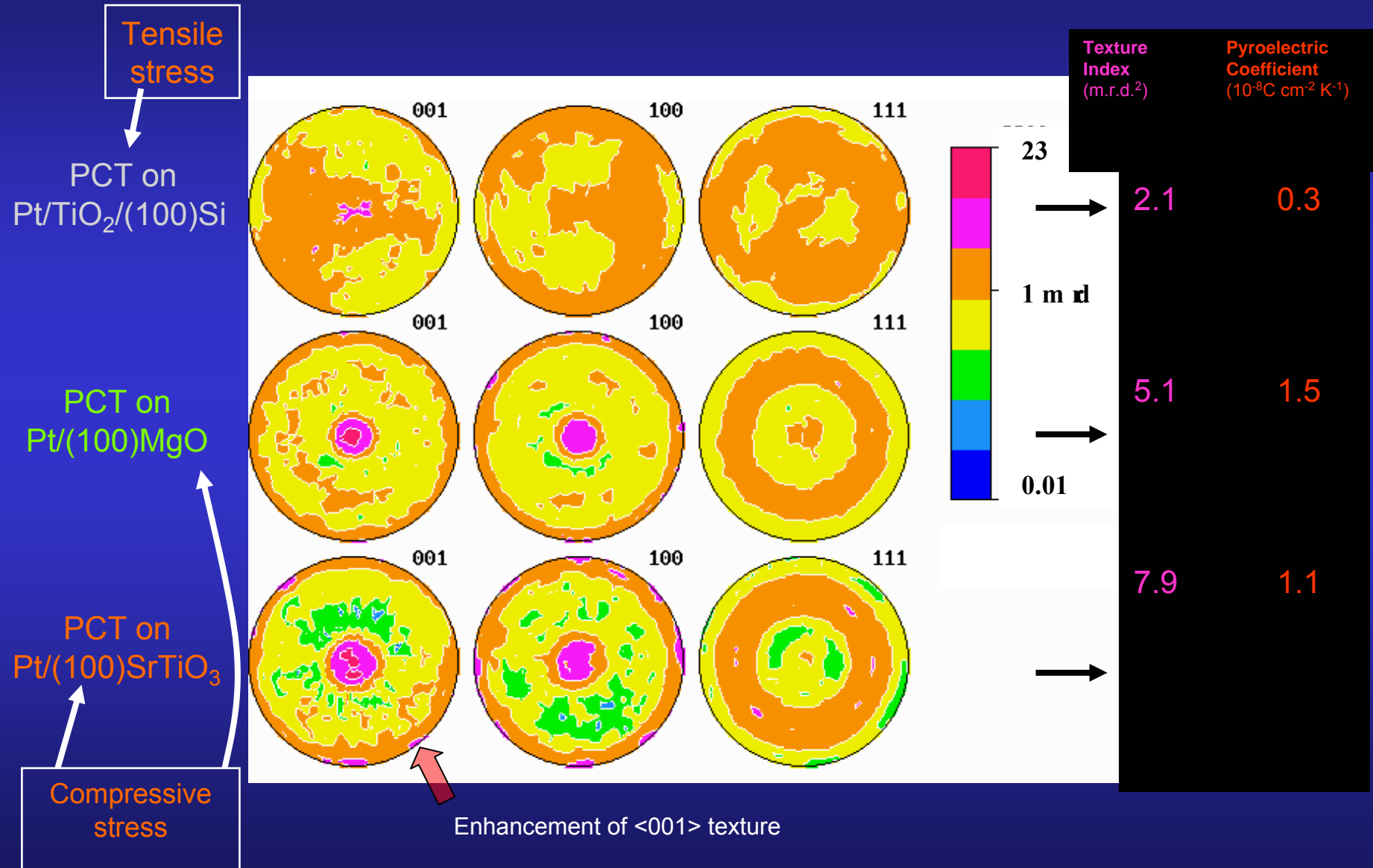
Structural, microstructural and texture quantitative characterisation of ferroelectric thin films by the combined method

Analysis of the X-ray diffraction diagrams of a PCT film on Pt/TiO₂/Si



$R_W = 13\%$; $R_B = 12\%$; $R_{exp} = 22\%$ (Rietveld)
 $R_W = 5\%$; $R_B = 6\%$ (E-WIMV)

Substrate influence on Residual Stress and Texture



Compliance coefficients [10 ⁻³ GPa ⁻¹]	PbTiO ₃ single crystal (data set A)	Film random orientation	PCT-Si <001> contrib.≈17%	PLT <001> contrib.≈49%	PCT-Mg <001> contrib.≈68%
S ₁₁	6.5	10.1	10.5	10.0	9.7
S ₂₂	6.5	10.0	10.5	10.0	9.7
S ₃₃	33.3	9.8	9.0	10.3	11.3
S ₄₄	14.5	13.2	12.8	12.9	13.1
S ₅₅	14.5	13.2	12.8	13.0	13.1
S ₆₆	9.6	13.4	14.0	13.5	12.7
S ₁₂	-0.35	-3.3	-3.5	-3.2	-3.0
S ₂₁	-0.35	-3.3	-3.5	-3.2	-3.0
S ₁₃	-7.1	-3.2	-3.1	-3.4	-3.6
S ₃₁	-7.1	-3.2	-3.1	-3.4	-3.6
S ₂₃	-7.1	-3.2	-3.1	-3.4	-3.6
S ₃₂	-7.1	-3.2	-3.1	-3.4	-3.6
S ₃₃ /S ₁₁	5.1	0.97	0.86	1.03	1.16
S ₁₃ /S ₁₂	20.3	0.97	0.89	1.06	1.20

Geometric mean average + biaxial stress state

Si nanocrystalline thin films

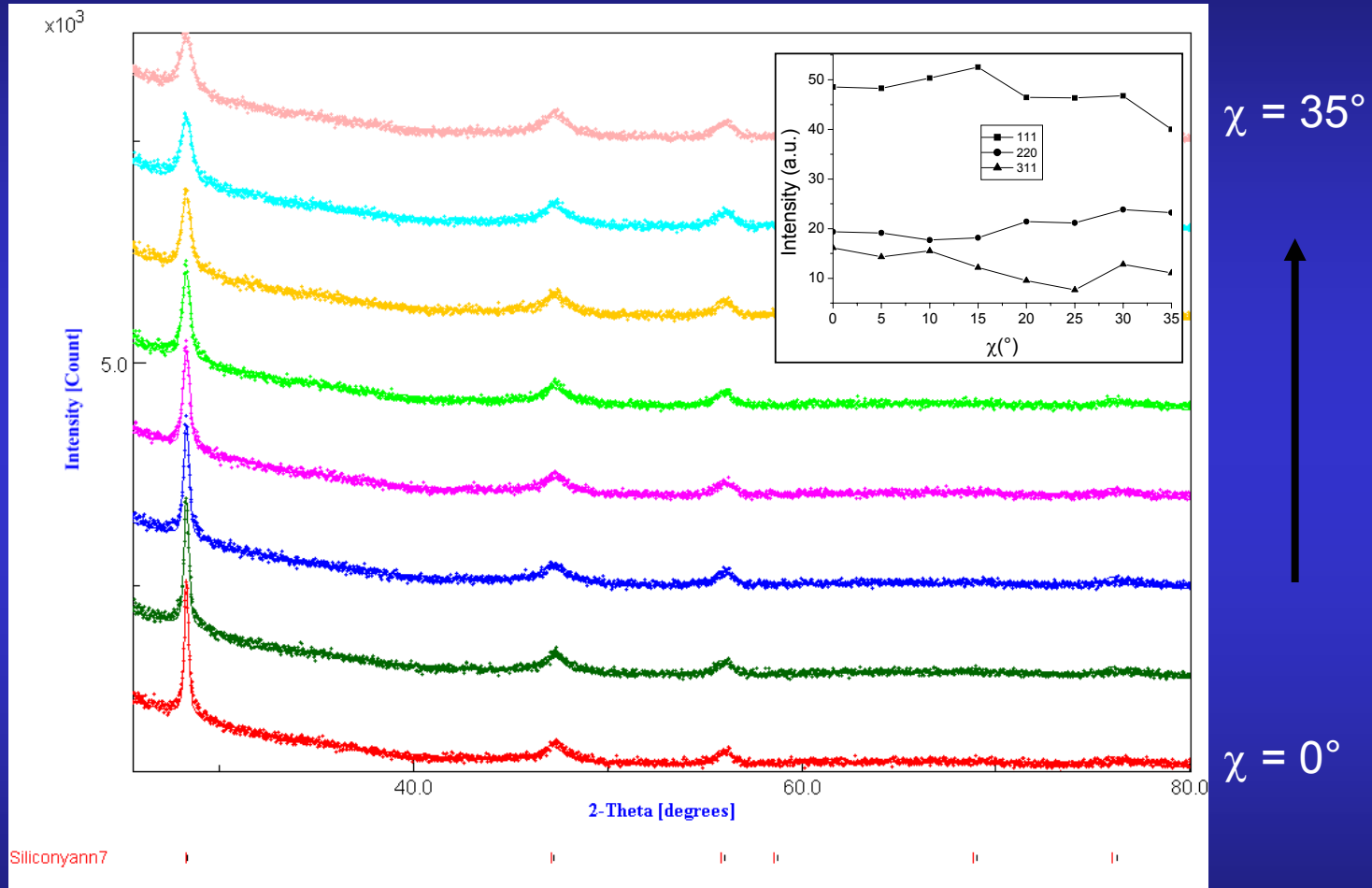
M. Morales, Caen

Silicon thin films deposition by reactive magnetron sputtering:

- ⇒ power density $2\text{W}/\text{cm}^2$
- ⇒ total pressure: $p_{\text{total}} = 10^{-1}$ Torr
- ⇒ plasma mixture: H_2 / Ar , $p_{\text{H}_2} / p_{\text{total}} = 80\%$
- ⇒ temperature: 200°C
- ⇒ substrates: amorphous SiO_2 (a- SiO_2)
(100)-Si single-crystals
- ⇒ target-substrate distance (d)
 - a- SiO_2 substrates: $d = 4, 6, 7, 8, 10, 12$ cm
films A, B, C, D, E, F
 - (100)-Si: $d = 6, 12$ cm
films G, H

Aim: quantum confinement, photoluminescence properties

Typical refinement

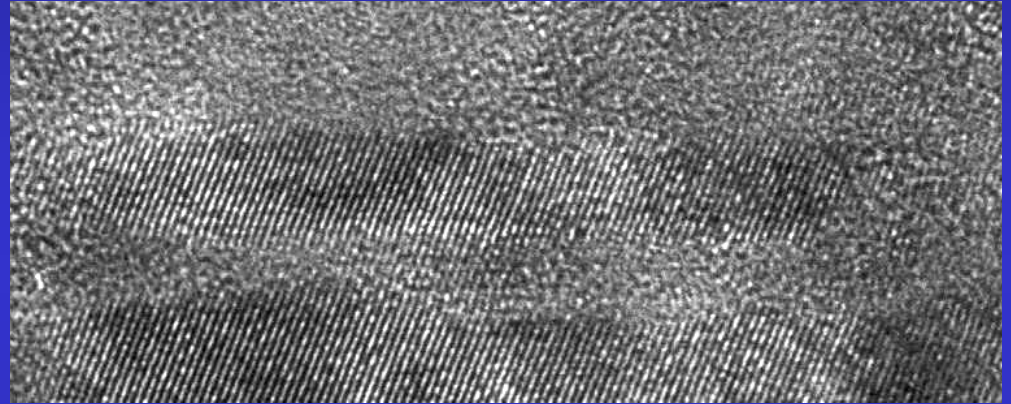
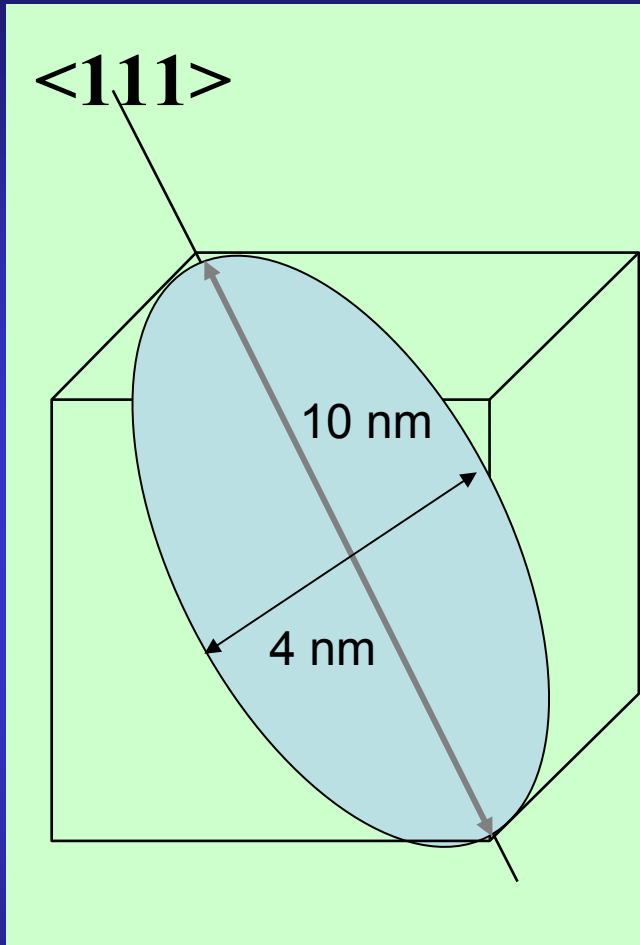


broad, anisotropic diffracted lines, textured samples

Refinement Results

Sample	d (cm)	a (Å)	RX thickness (nm)	Anisotropic sizes (Å)			Texture parameters			Reliability factors (%)			
				<111>	<220>	<311>	Maximum (m.r.d.)	minimum (m.r.d.)	Texture index F ² (m.r.d ²)	RP ₀	R _w	R _B	R _{exp}
A	4	5.4466 (3)	—	94	20	27	1.95	0.4	1.12	1.72	4.0	3.7	3.5
B	6	5.4439 (2)	711 (50)	101	20	22	1.39	0.79	1.01	0.71	4.9	4.3	4.2
C	7	5.4346 (4)	519 (60)	99	40	52	1.72	0.66	1.05	0.78	4.3	4.0	3.9
D	8	5.4461 (2)	1447 (66)	100	22	33	1.57	0.63	1.04	0.90	5.5	4.6	4.5
E	10	5.4462 (2)	1360 (80)	98	20	25	1.22	0.82	1.01	0.56	5.0	3.9	4.0
F	12	5.4452 (3)	1110 (57)	85	22	26	1.59	0.45	1.05	1.08	4.2	3.5	3.7
G	6	5.4387 (3)	1307 (50)	89	22	28	1.84	0.71	1.01	1.57	5.2	4.7	4.2
H	12	5.4434 (2)	1214 (18)	88	22	24	2.77	0.50	1.12	2.97	5.0	4.5	4.3

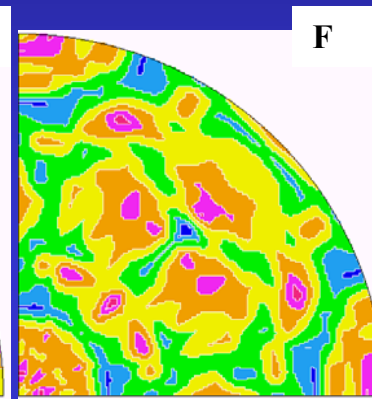
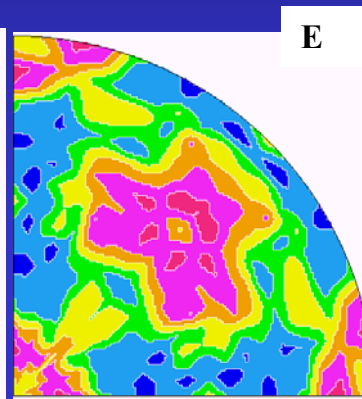
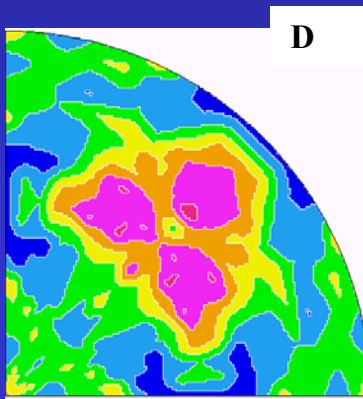
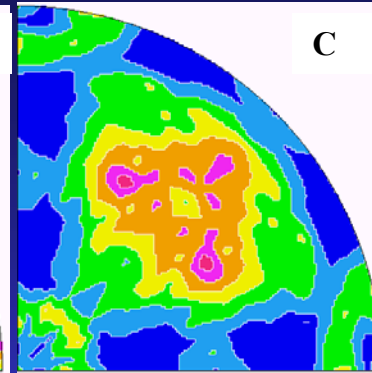
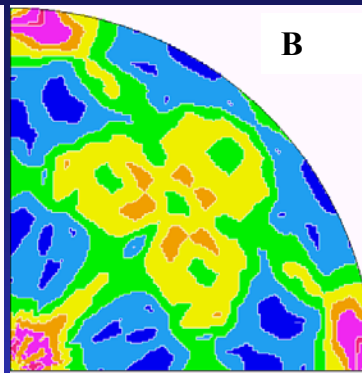
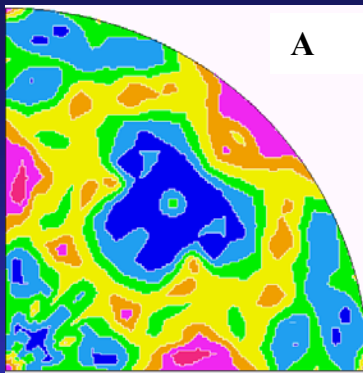
Mean anisotropic shape



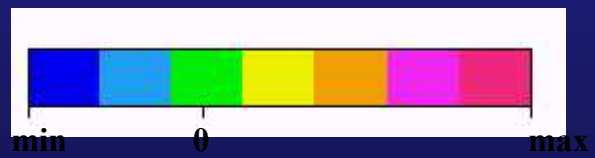
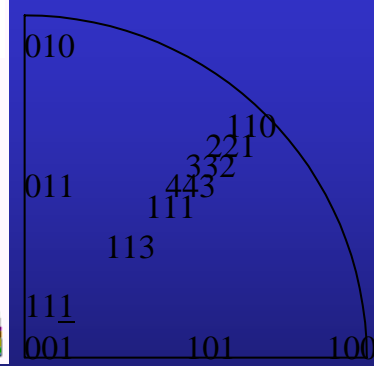
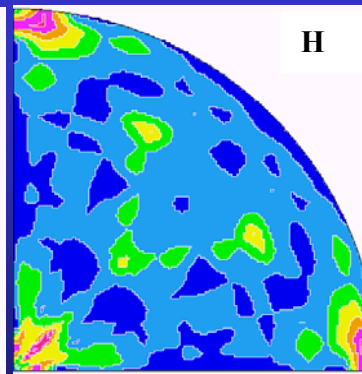
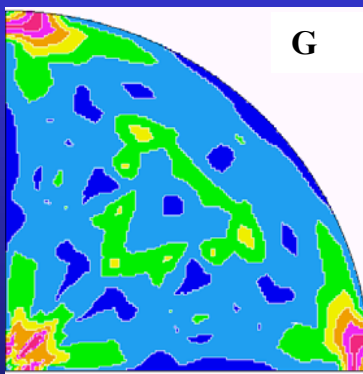
Schematic of the mean crystallite shape for Sample D represented in a cubic cell, as refined using the Popa approach and exhibiting a strong elongation along $\langle 111 \rangle$, and TEM image

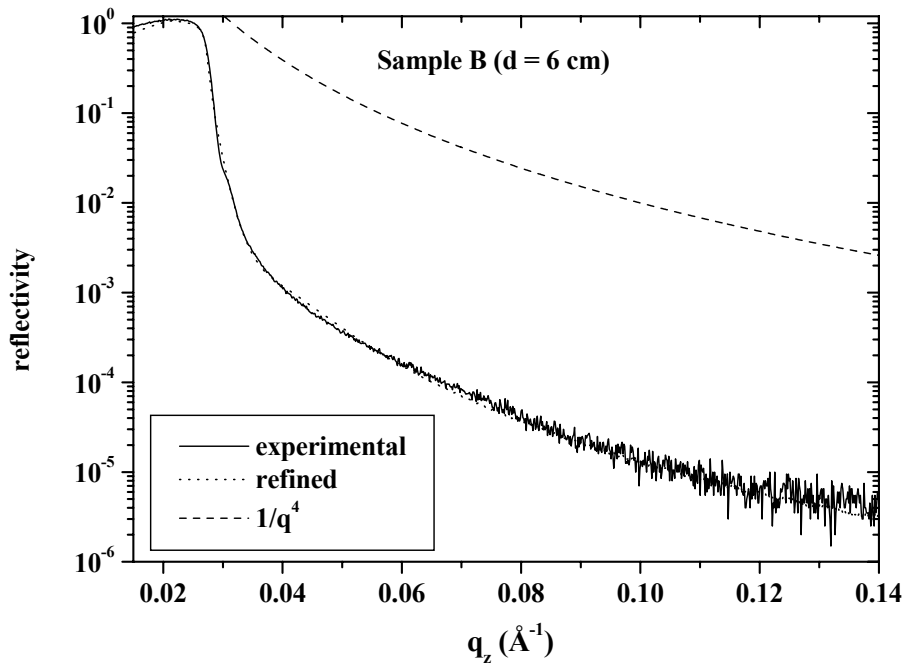
001 Inverse Pole Figures

a-SiO₂



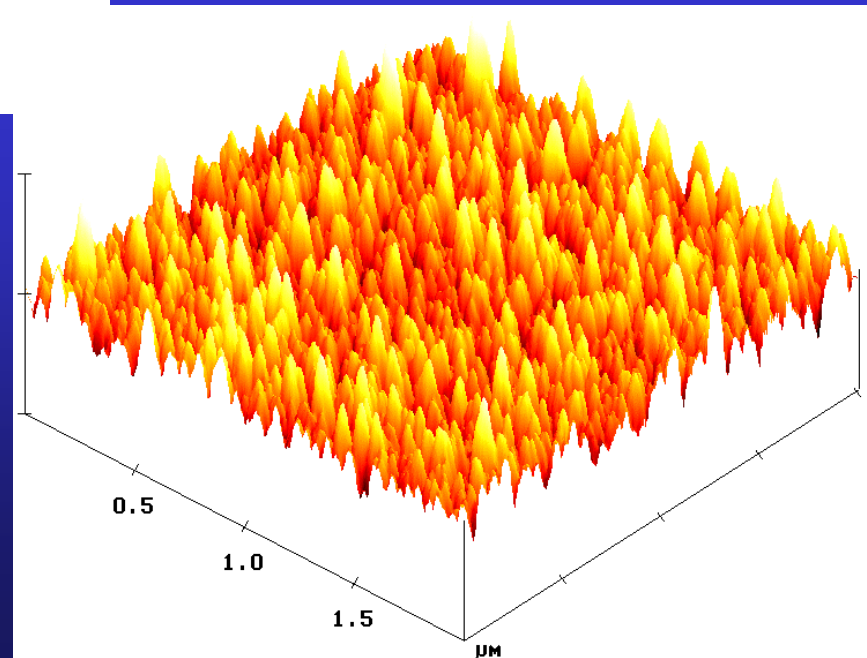
(100)-Si

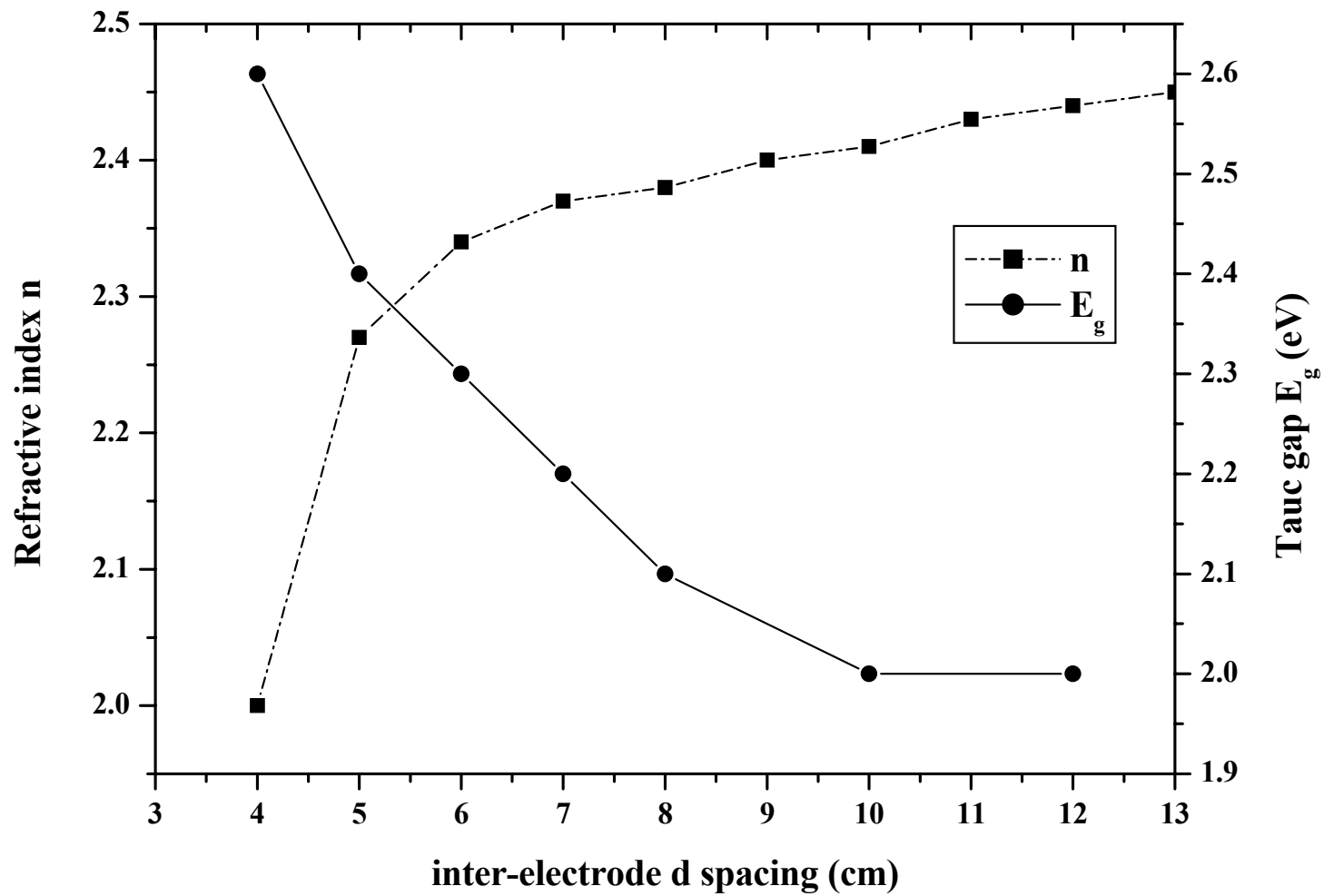




XRR:
Roughness
governed

AFM:
homogeneous
roughness

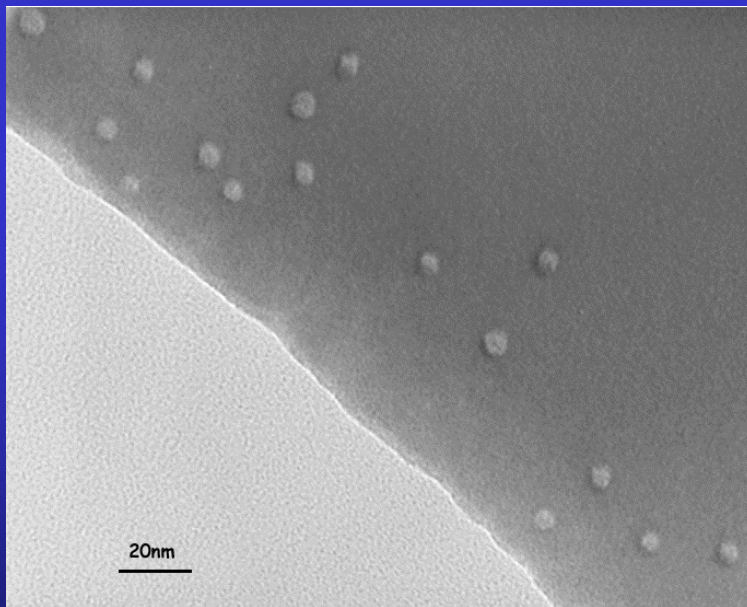




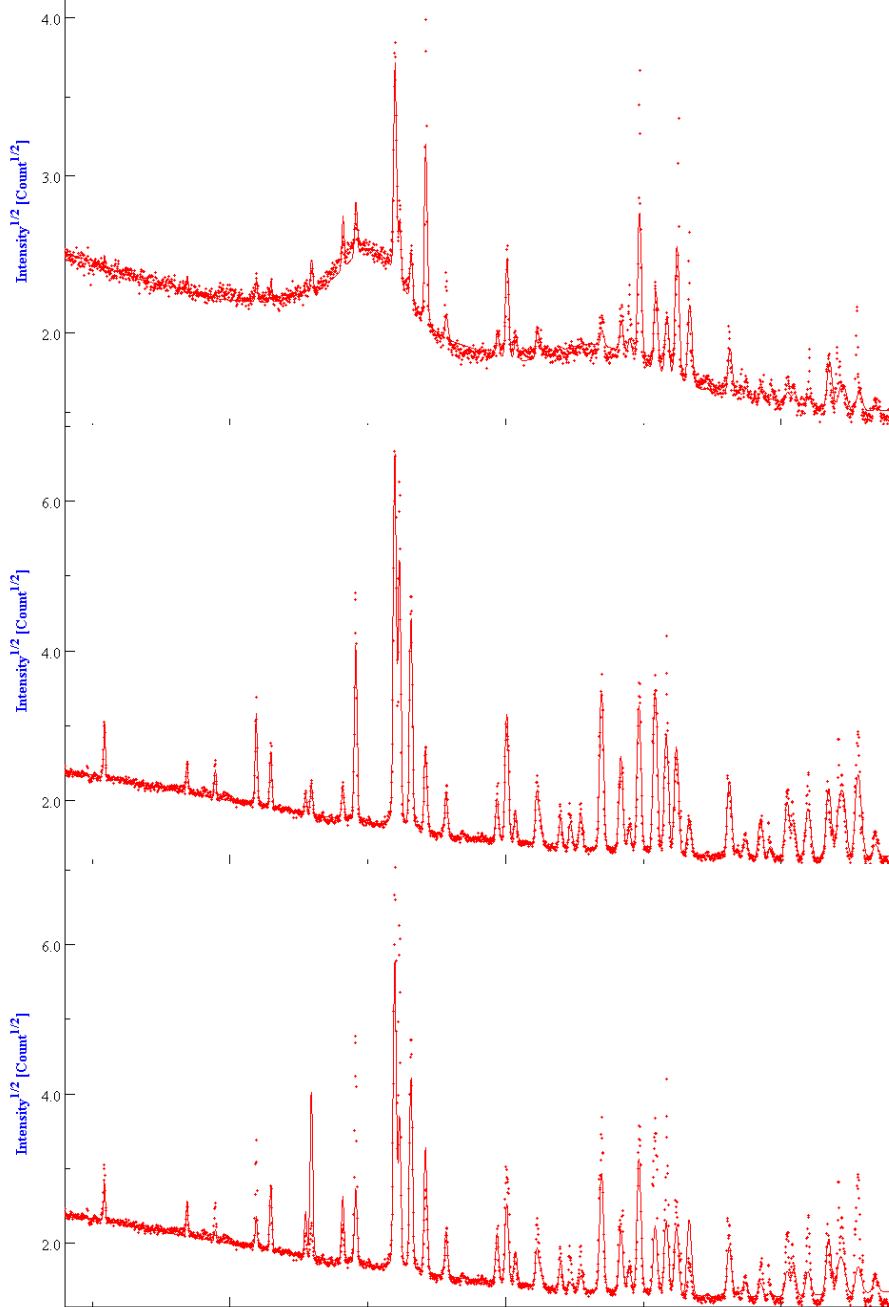
Irradiated FluorApatite (FAp) ceramics

S. Miro, PhD

Self-recrystallisation under irradiation, depending on $\text{SiO}_4 / \text{PO}_4$ ratio (FAp / Nd-Britholite) and on irradiating species



TEM of FAp
irradiated with 70
MeV, 10^{12} Kr cm^{-2}
ions



Ca5-(P-O4)3-F

texture corrected,
 10^{13} Kr cm^{-2}

Virgin, with texture
correction

Virgin, no texture
correction

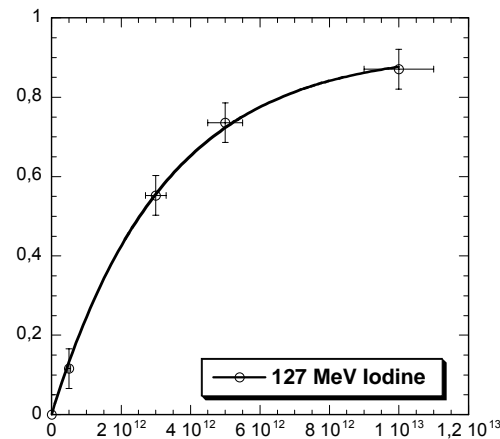
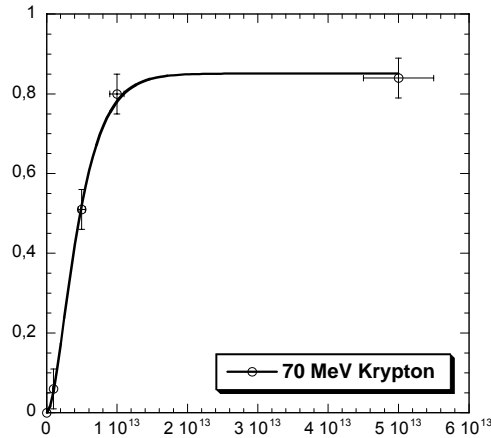
Fluence (ions.cm ⁻²)	Vc/V (%)	A (Å)	c (Å)	<t> (nm)	Δa/a ₀ (%)	Δc/c ₀ (%)	R _w (%)	R _B (%)
0	100	9.3365(3)	6,8560(5)	294(22)	-	-	14.6	9.1
Kr								
10 ¹¹	100	-	-	-	-	-		
10 ¹²	100	-	-	-	-	-		
5.10 ¹²	49(1)	9.3775(9)	6.8912(8)	294(20)	0.44	0.53	24	15
10 ¹³	20(1)	9.4236(5)	6.9105(5)	291(20)	0.94	0.82	9.9	6
5.10 ¹³	14(1)	9.3160(4)	6.8402(5)	294(22)	-0.21	-0.22	10.5	5.9
I								
10 ¹¹	-	-	-	-	-	-		
5.10 ¹¹	86(2)	9.3603(3)	6.8790(5)	90(10)	0.26	0.35	23.9	15.1
10 ¹²	-	-	-	-	-	-		
3.10 ¹²	47(2)	9.3645(3)	6.8840(5)	91(6)	0.30	0.42	13.3	9
5.10 ¹²	29.2(5)	9.3765(5)	6.8881(6)	77(11)	0.44	0.48	10.4	7.3
10 ¹³	13.2(2)	9.3719(4)	6.8857(6)	82(9)	0.38	0.45	6.7	4.9

Single impact model associated to crystal size reduction

Cell parameters and volume increase, then relax

Amorphisation / recrystallisation competition: single or double impact

Amorphous/crystalline volume fraction (damaged fraction $F_d = V_a / V$) as determined by x-ray diffraction



B

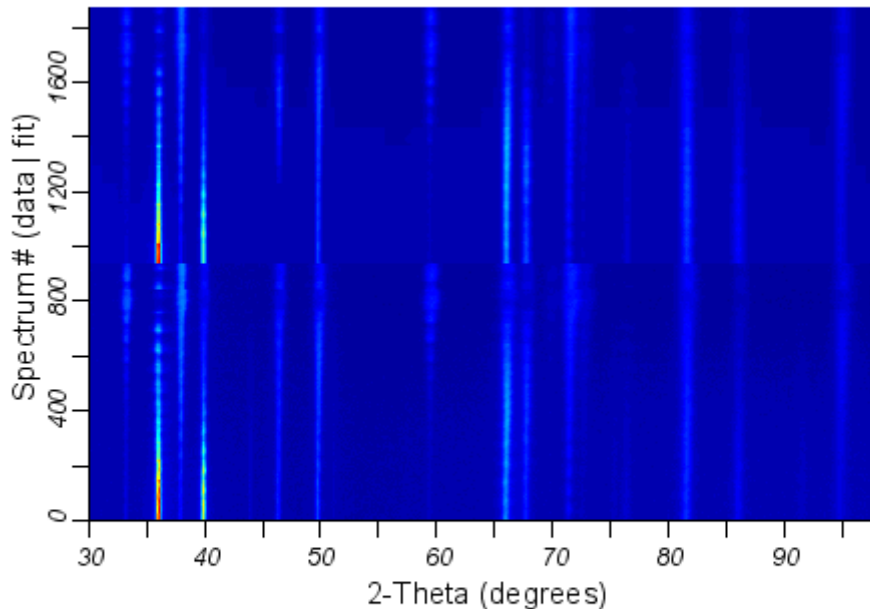
Fitting parameters	Krypton		Iodine
	Single impact	Double impact	Single impact
	$F_d = B(1 - \exp(-A\phi t))$	$F_d = B(1 - (1 + A\phi t) \exp(-A\phi t))$	$F_d = B(1 - \exp(-A\phi t))$
$A = \pi R^2$ (cm ²)	$1.85 \pm 0.15 \cdot 10^{-13}$	$4.1 \pm 0.15 \cdot 10^{-13}$	$3.3 \pm 0.15 \cdot 10^{-13}$
Radius R (nm)	2.4 ± 0.2	3.6	3.2
B (Max.damage rate)	0.87	0.85 ± 0.2	0.92 ± 0.2
χ^2	0.013	0.0006	0.0004

AlN/Pt/TiO_x/Al₂O₃/Ni-Co-Cr-Al

E. Derniaux, PhD

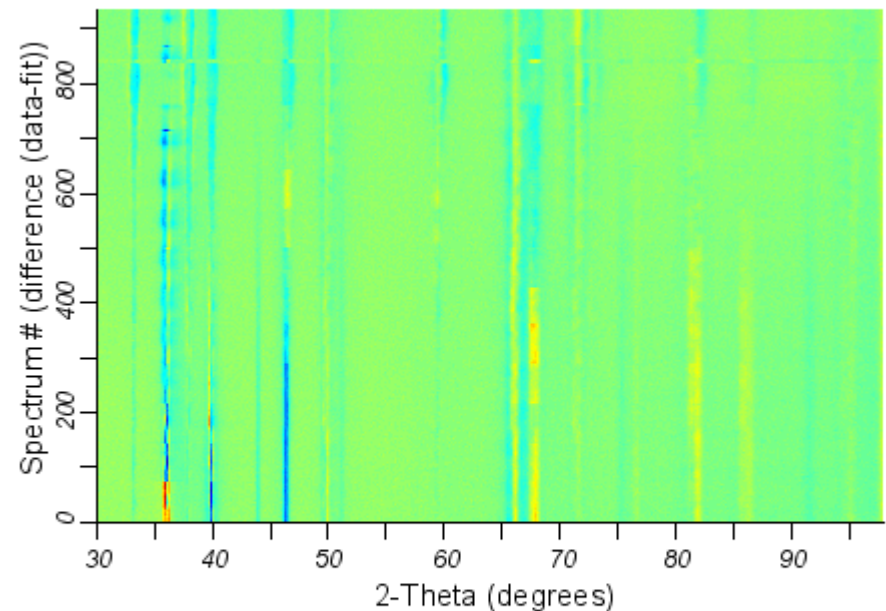
2D Multiplot for Data 05_37P64

measured data and fit



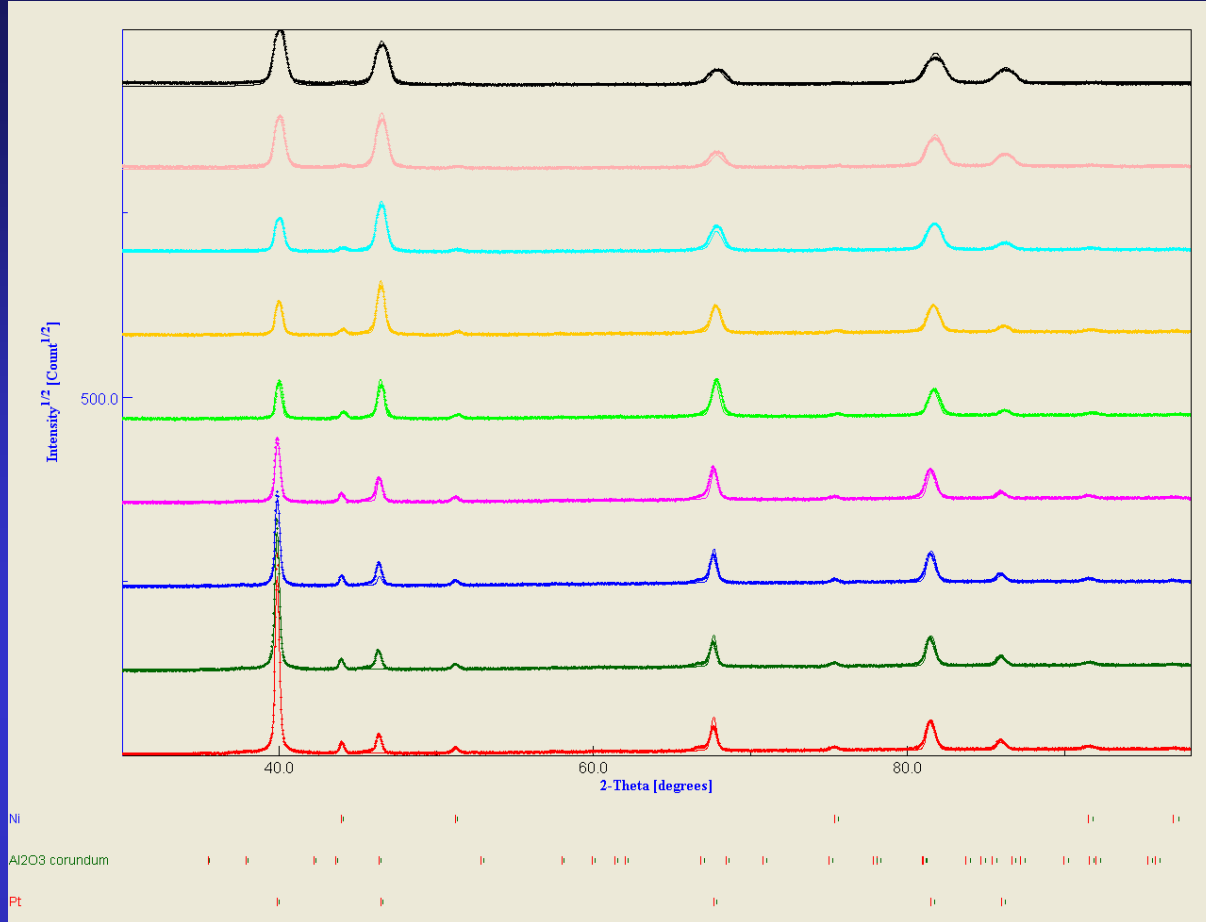
2D difference plot for Data 05_37P64

difference data - fit

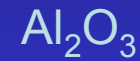


Rw (%) = 24.120445
Rexp (%) = 5.8517213

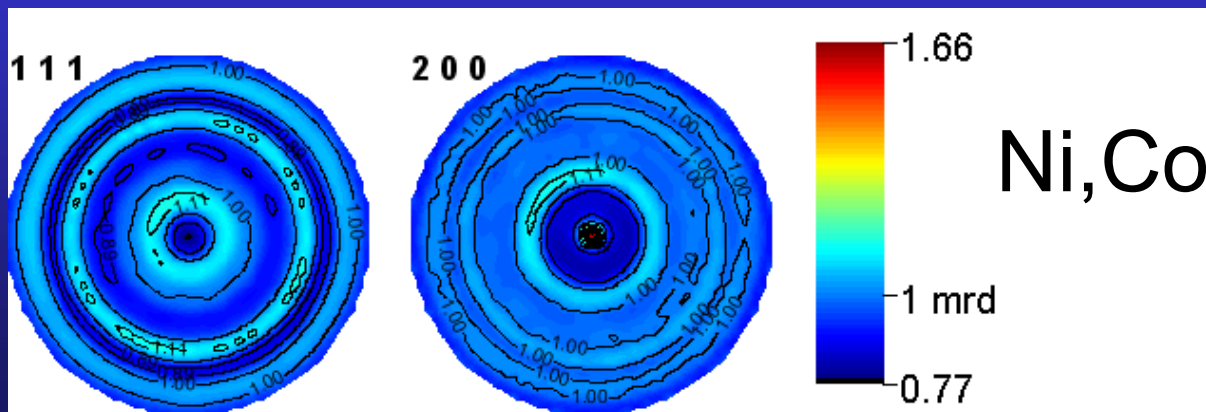
T(AlN) = 14270(3) nm
T(Pt) = 430(3) nm



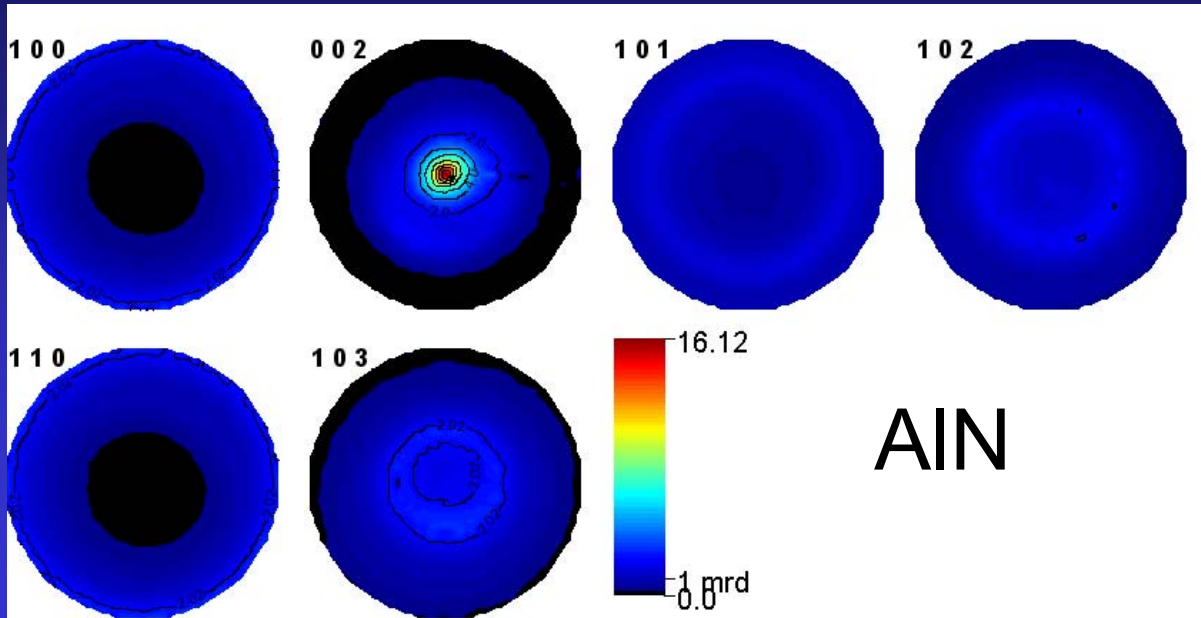
(χ, φ) randomly
selected diagrams



$a = 4.7562(6) \text{ \AA}$
 $c = 12.875(3) \text{ \AA}$
 $T = 7790(31) \text{ nm}$
 $\langle t \rangle = 150(2) \text{ \AA}$
 $\langle \varepsilon \rangle = 0.008(3)$



$a = 3.569377(5) \text{ \AA}$
 $\langle t \rangle = 7600(1900) \text{ \AA}$
 $\langle \varepsilon \rangle = 0.00236(3)$
 $\sigma_{11} = -328(8) \text{ MPa}$
 $\sigma_{22} = -411(9) \text{ MPa}$



Rw (%) = 4.1

$a = 3.11203(1) \text{ \AA}$

$c = 4.98252(1) \text{ \AA}$

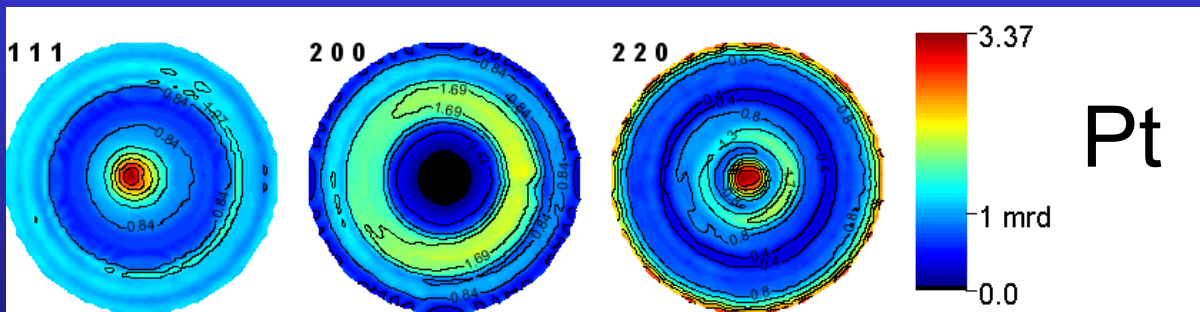
$T = 14270(3) \text{ nm}$

$\langle t \rangle = 2404(8) \text{ \AA}$

$\langle \varepsilon \rangle = 0.001853(2)$

$\sigma_{11} = -1019(2) \text{ MPa}$

$\sigma_{22} = -845(2) \text{ MPa}$



Rw (%) = 33.3

$a = 3.91198(1) \text{ \AA}$

$T = 1204(3) \text{ nm}$

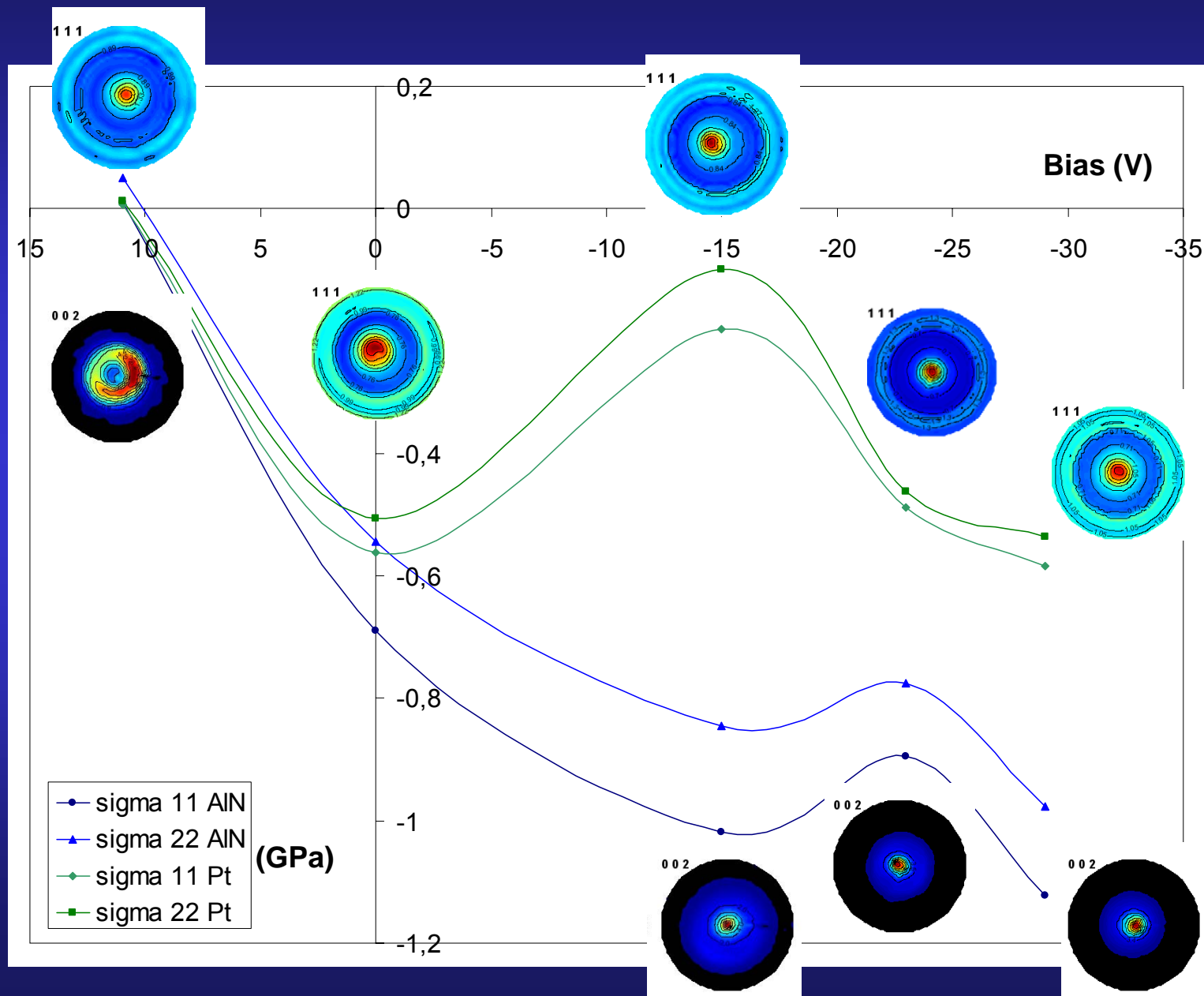
$\langle t \rangle = 2173(10) \text{ \AA}$

$\langle \varepsilon \rangle = 0.002410(3)$

$\sigma_{11} = -196.5(8)$

$\sigma_{22} = -99.6(6)$

Substrate bias vs stress-texture evolution



Conclusions

- a) Texture affects phase ratio and structure determination
- b) Microstructure (crystallite size) affects texture (go to a)
- c) Stresses shift peaks then affects structure and texture determination
- d) Combined analysis may be a solution, unless you can destroy your sample or are not interested in macroscopic anisotropy ...
- e) If you think you can destroy it, perhaps think twice
- f) more information is always needed: local probes ...
- g) www.ecole.ensicaen.fr/~chateign/texture/combined.pdf