

# Calcium carbonate microstructures in mollusc sea-shells: a voyage with the x-ray shuttle

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calcite - Nacre - aragonite

Electrochemistry

Biomaterialisation

Ti-Coating

Mollusc Phylogeny

Artificial Coral reefs

Calcareous deposits  
Scaling-antiscaling

Extinct species,  
fossils

CO<sub>2</sub> sequestration

Snail Farming

Jewelry - Pearls

Geology

Environment

Shell spores

Bio-Integration, Osteoinduction

Fauna preservation  
Biodiversity remediation

Cosmetics

Dentistry - Implantology - Prosthodontics

Structure Reinforcements

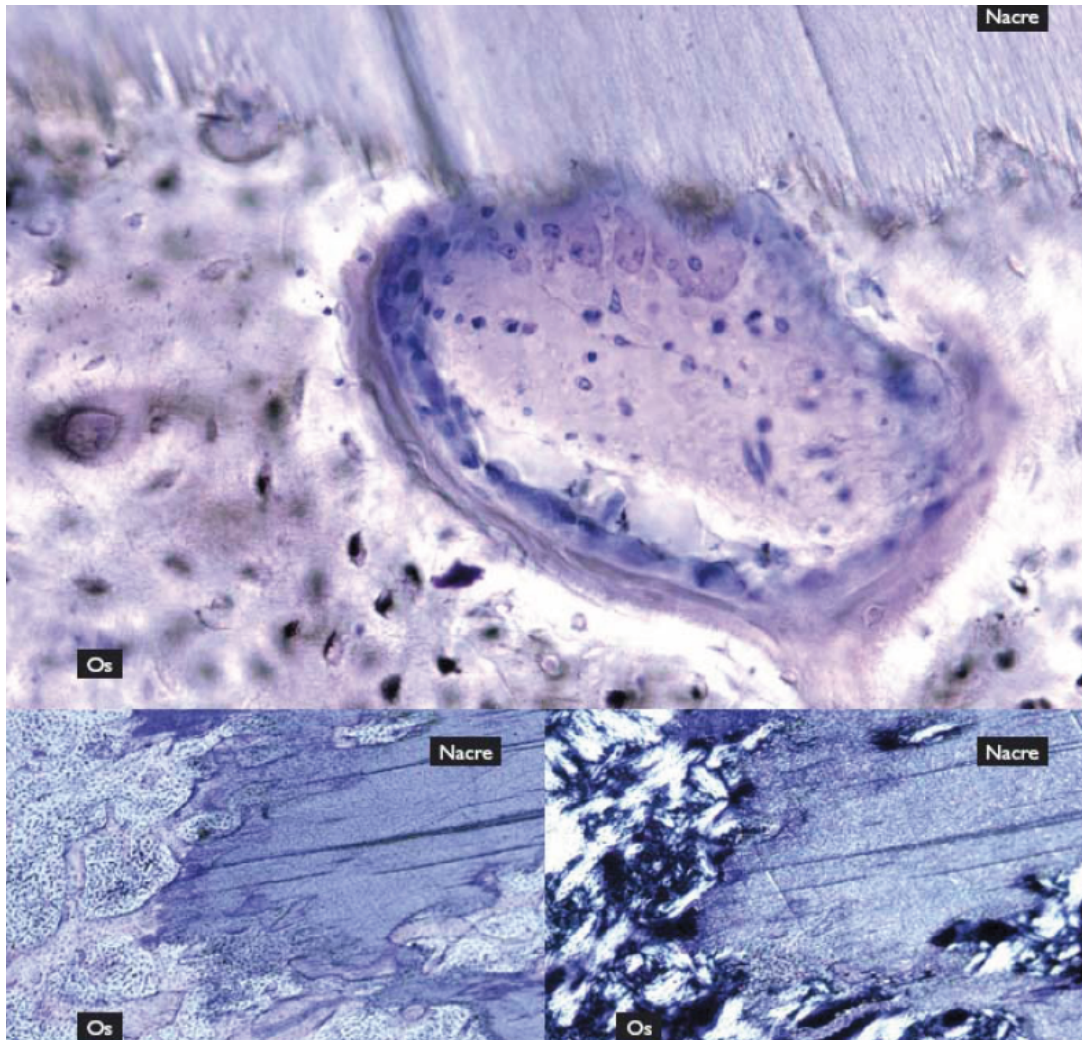
Medicine



4000 BC maya cranes,  
Honduras

Amadéo Bobbio (1972) *Bull. Historical  
Dentology*

Evelyne Lopez, MNHN, Paris



Bone-cells stimulation at the  
nacre/bone interface

Penetration of neo-bone  
inside nacre

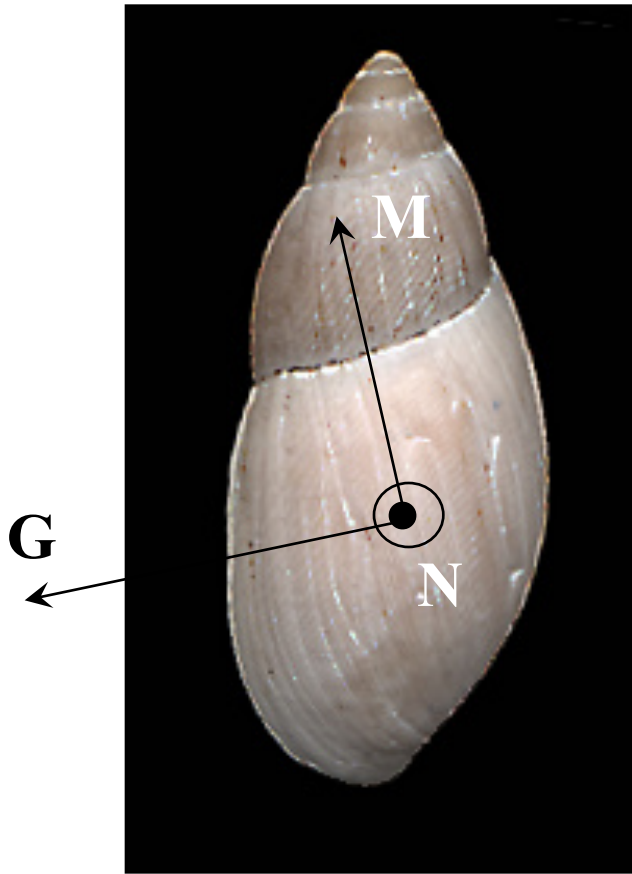
Evelyne Lopez *et al.* (1992) *Tissue & Cell*

## Why rays (X, n, e<sup>-</sup>) diffraction ?

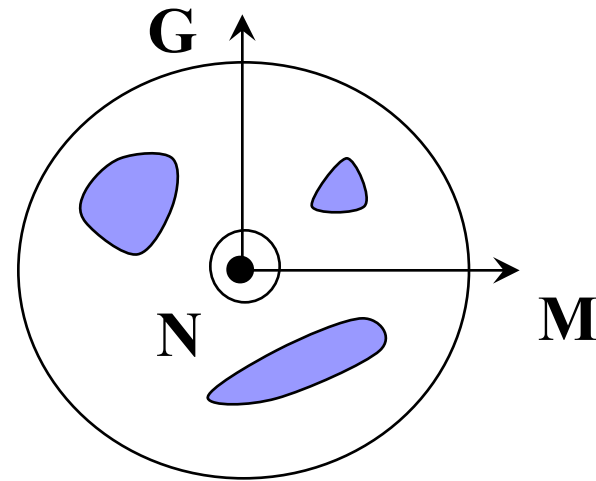
- Microstructure versus texture
- Mollusc Phylogeny (Texture ...)
- A link to mollusc ancestors
- Cell distortions in biogenic crystals
- Synthetic nacre-like biocrystals
- In corals

# Reference frame

*Euglandina rosea*: a land snail, carnivorous mollusc introduced in Pacific and Indian oceans, to regulate *Achatina fulica*



- Crystal:  $\text{CaCO}_3$ , aragonite ( $\text{Pm}\bar{c}n$ ) or calcite ( $\text{R}\bar{3}c$ )
- Sample: triclinic

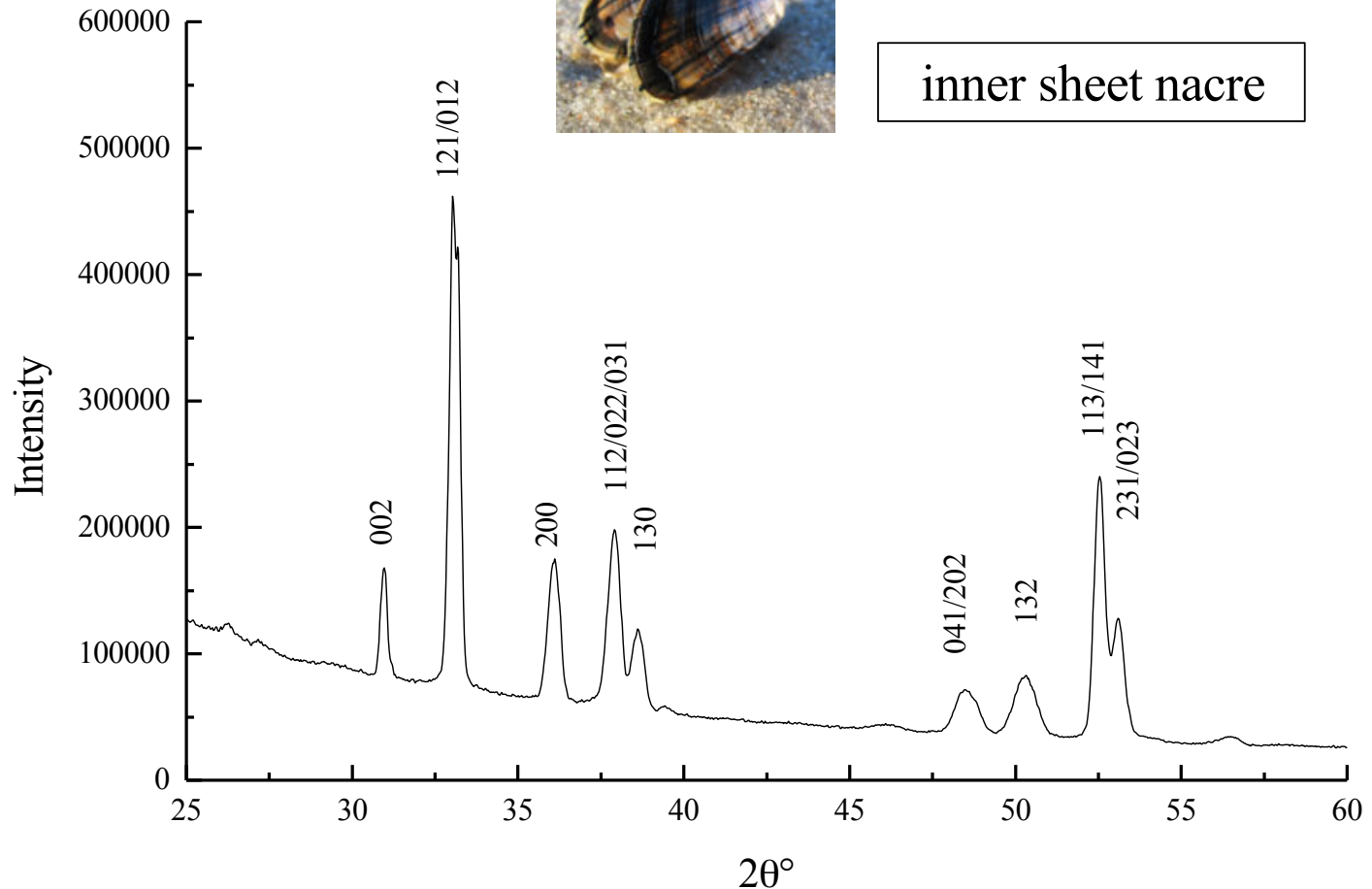


# Typical patterns: using the CPS120-INEL

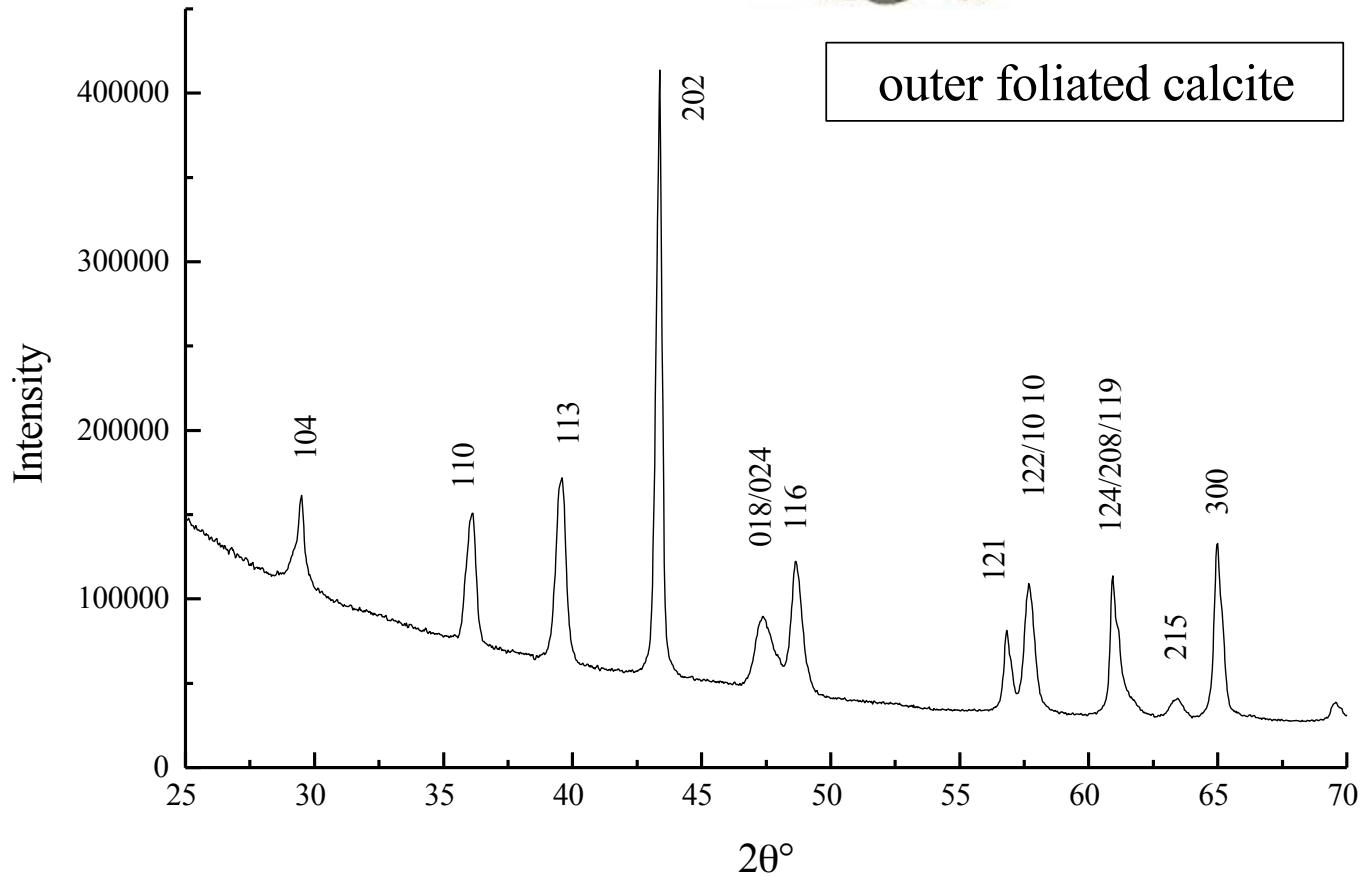
*Mytilus edulis* (common mussel): sum diagrams



inner sheet nacre



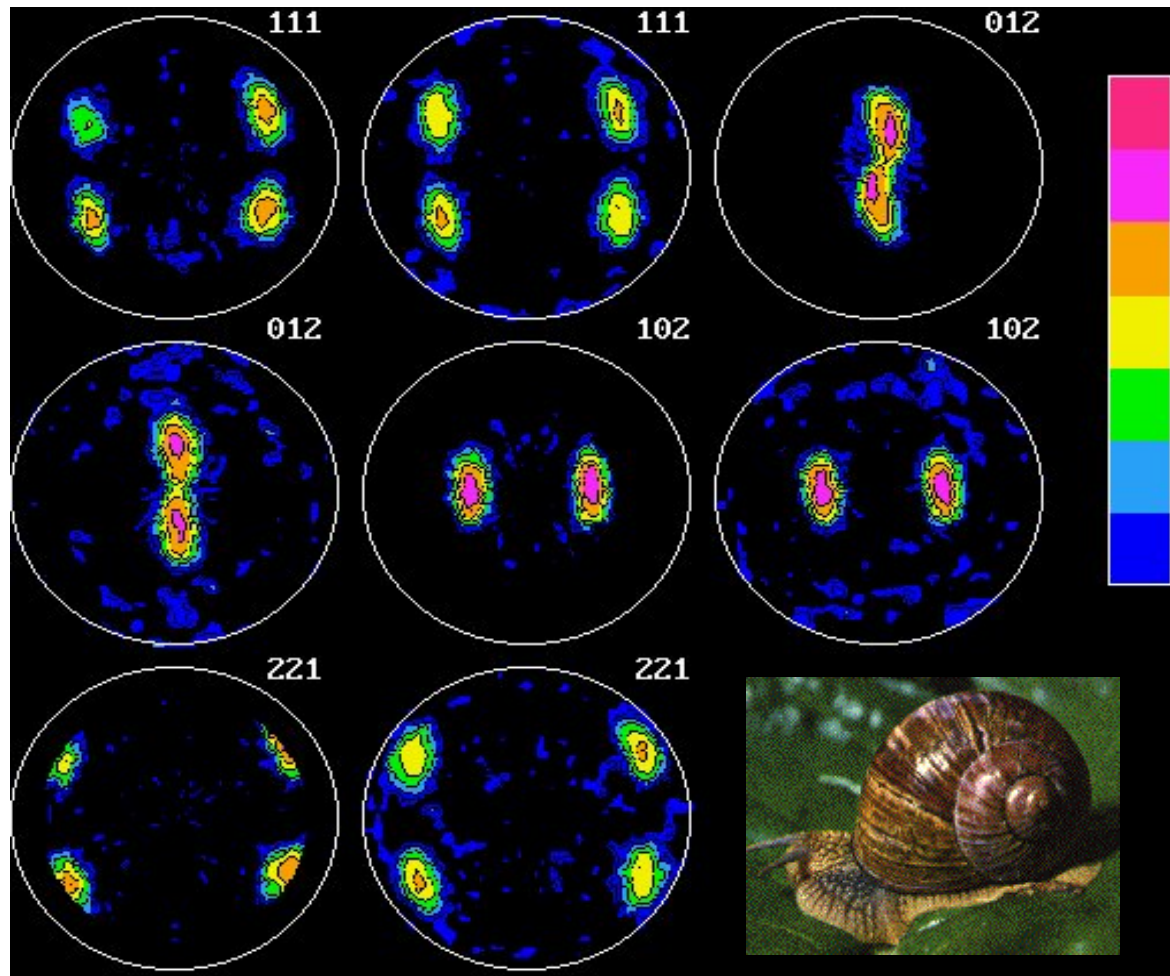
# *Crassostrea gigas* (common oyster)



Measured for around 1000 sample orientations, using x-rays, neutrons or electrons, depending on the desired probed volume



OD-reliability: *Helix pomatia* (Burgundy land snail:  
Outer com. crossed lamellar)



22.7

$$RP_{0.05} = 67\%$$

$$RP_1 = 40\%$$

Lin. scale

Eq. area

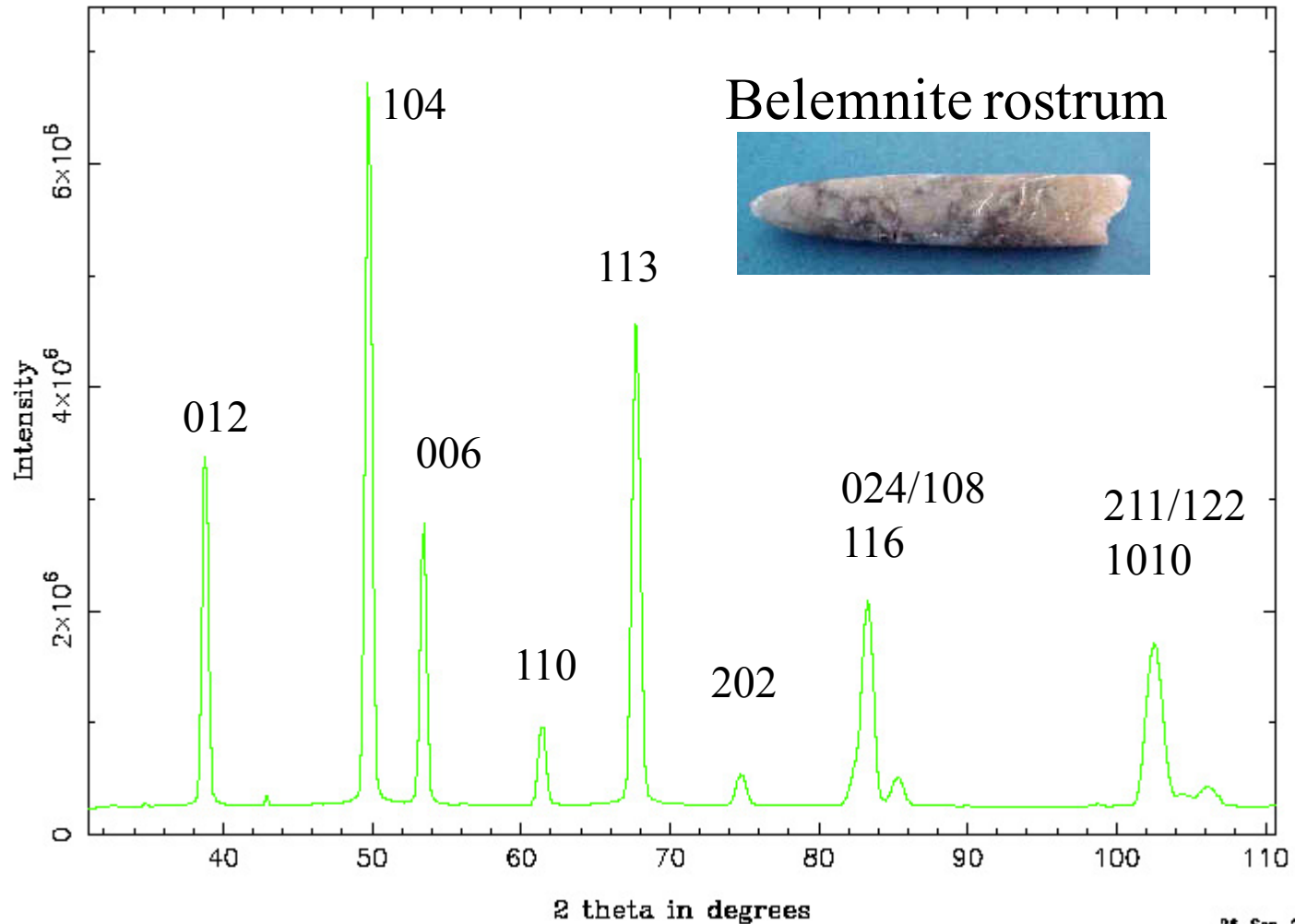
1 m.r.d.

$$S = -4.1$$

$$F^2 = 106 \text{ m.r.d.}^2$$

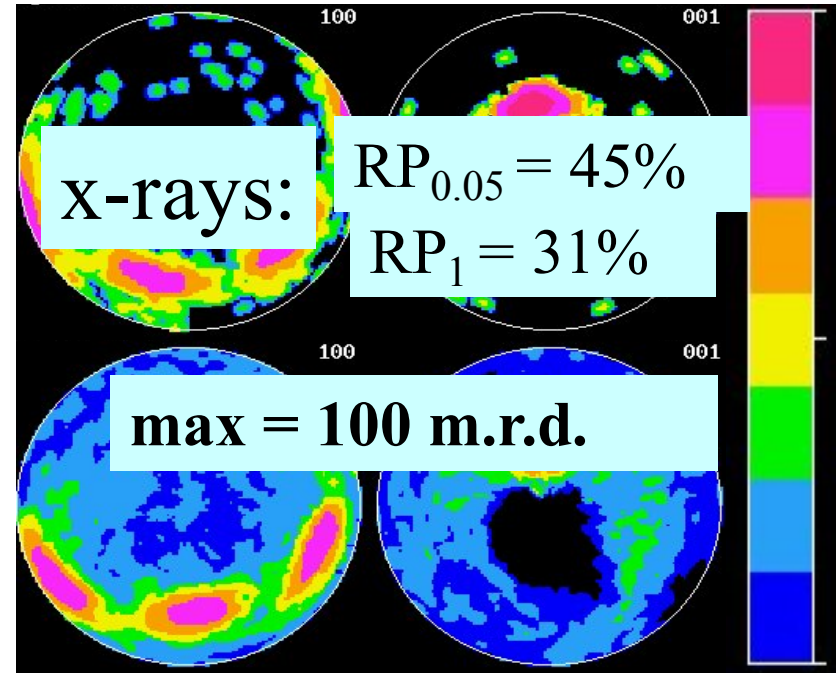
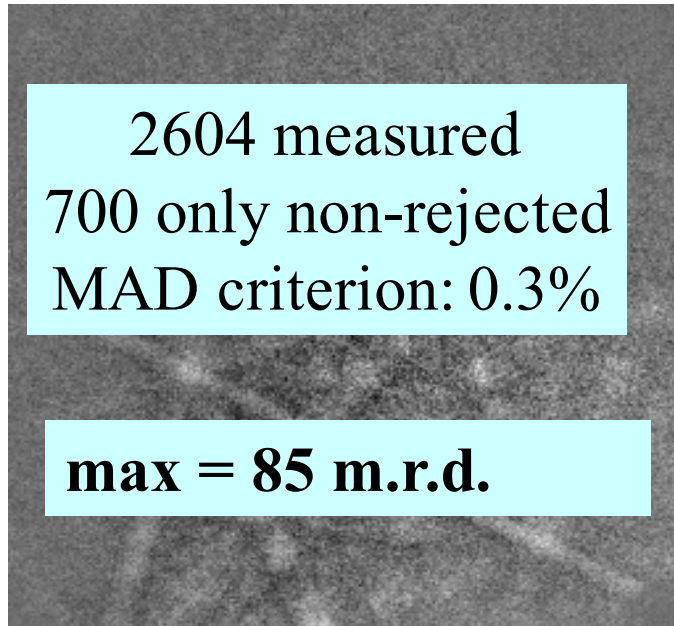
$$OD_{\max} = 444 \text{ m.r.d.}$$

# D1B-ILL experiments



# *Crassostrea gigas* (Inner foliated calcite)

Electrons



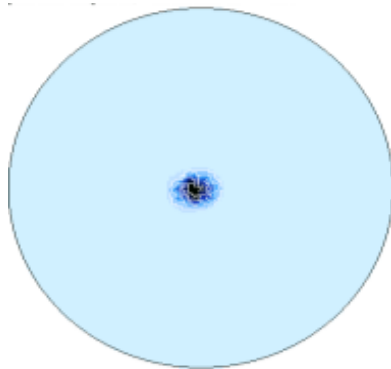
Global analysis is coherent with local ones like synchrotron microfocus x-rays (*Aizenberg et al. (1996) Connective Tissue Research 34 255*)

## c-axes texture patterns

*Pinctada  
maxima*

ISN

“gold pearl  
oyster”

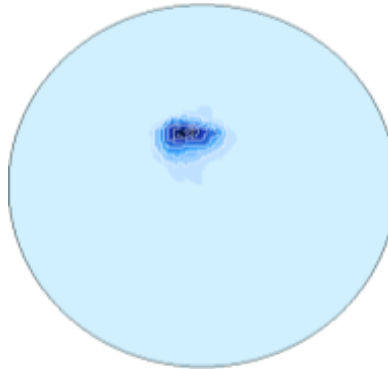


T

*Nerita  
polita*

ICCL

“polished  
nerite”

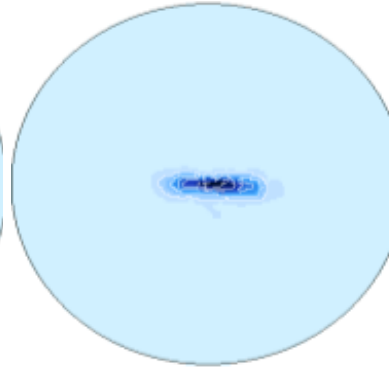


Z

*Fragum  
fragum*

ICCL

“cockle”

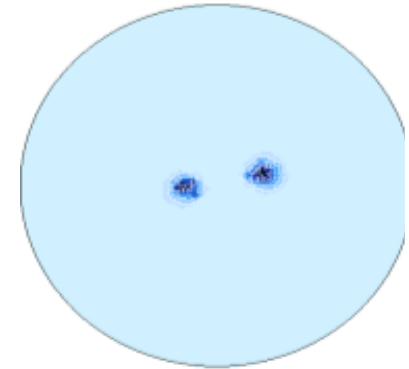


A

*Cypraea  
testudinaria*

ICCL

“turtle  
cowry”



V

## a-axes texture patterns

*Helix  
pomatia*

OCCL

“burgundy  
land snail”

*Tectus  
niloticus*

ICN

“commercial  
top shell”

*Conus  
leopardus*

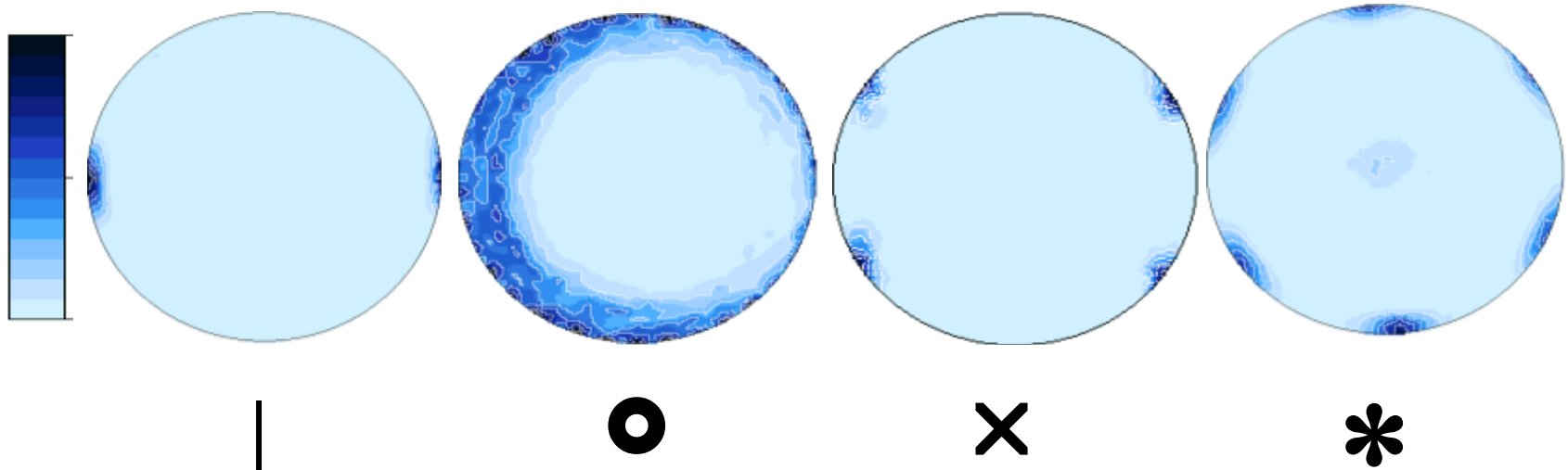
ICCL

“leopard  
cone”

*Nautilus  
pompilius*

ICN

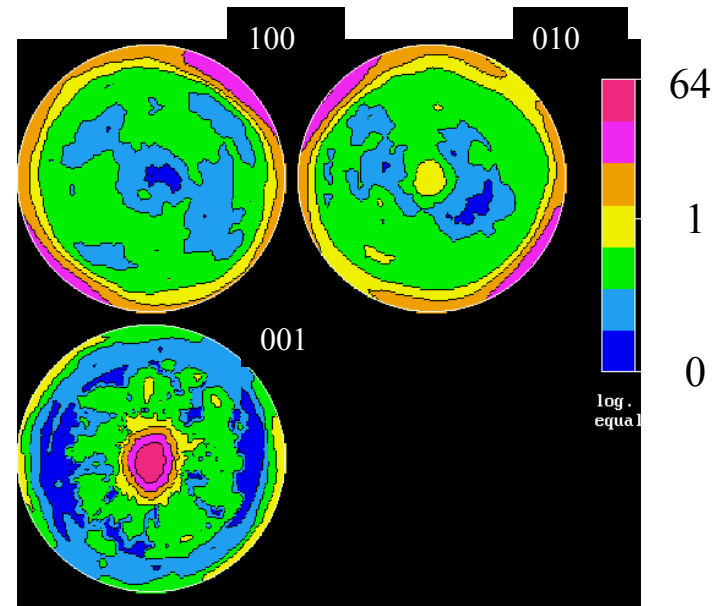
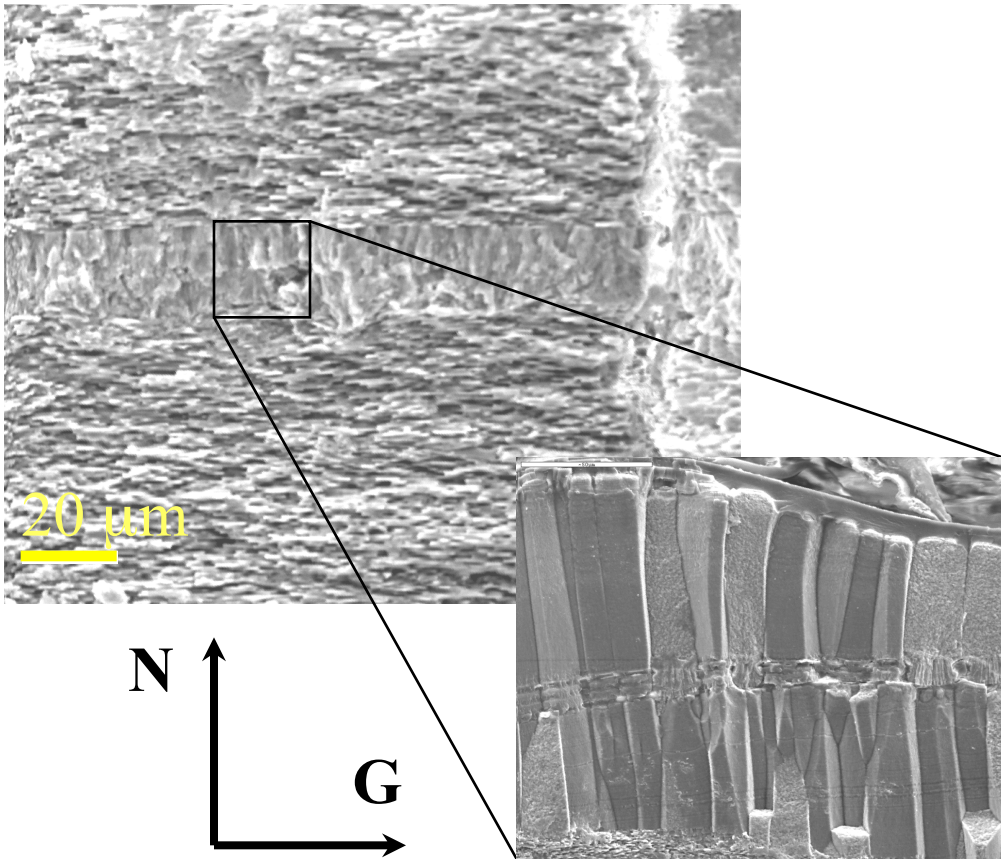
“new caledonia  
nautilus”



# Microstructure versus texture



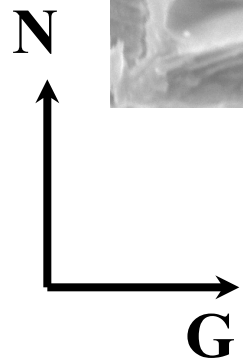
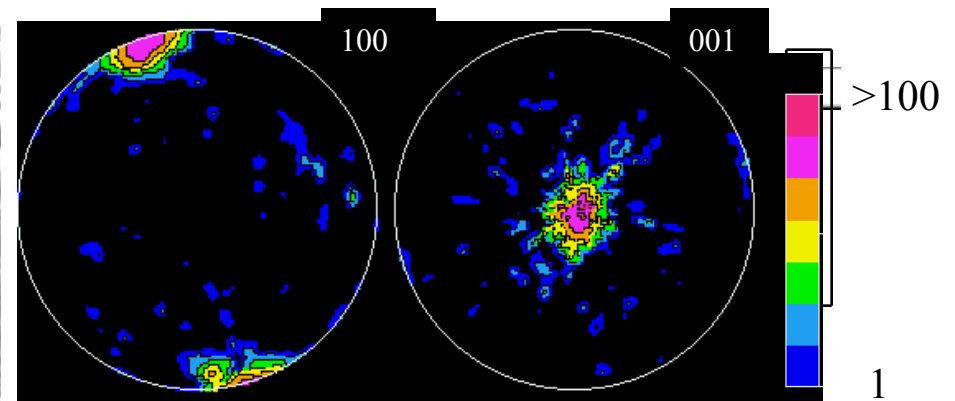
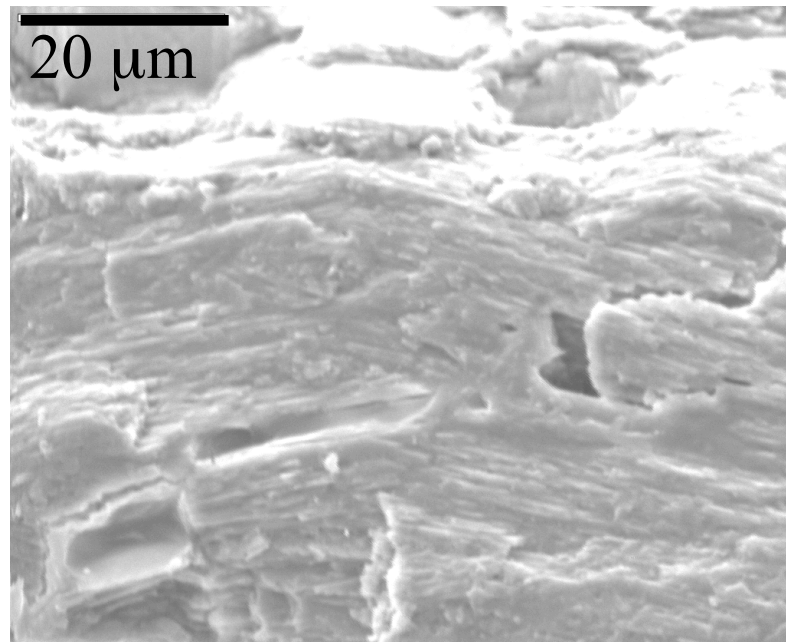
Inner sheet nacre of *Anodonta cygnea* (freshwater swan mussel)



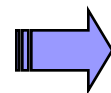
$$\langle \perp | \text{ISN} | *_{25}^{a, -45} \rangle$$

# Microstructure versus texture

*Cyclophorus woodianus*: different crystal orientations look like single crystal from diffraction !



$$\langle \perp | \text{IRCL} |^a, 20 \rangle$$



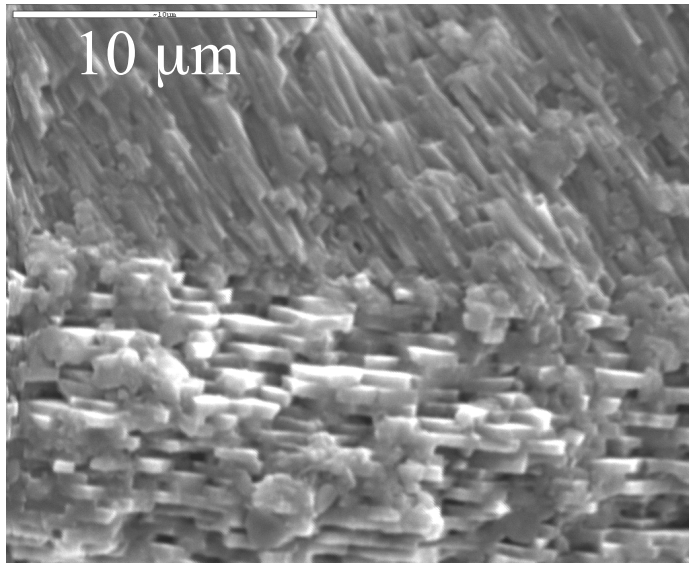
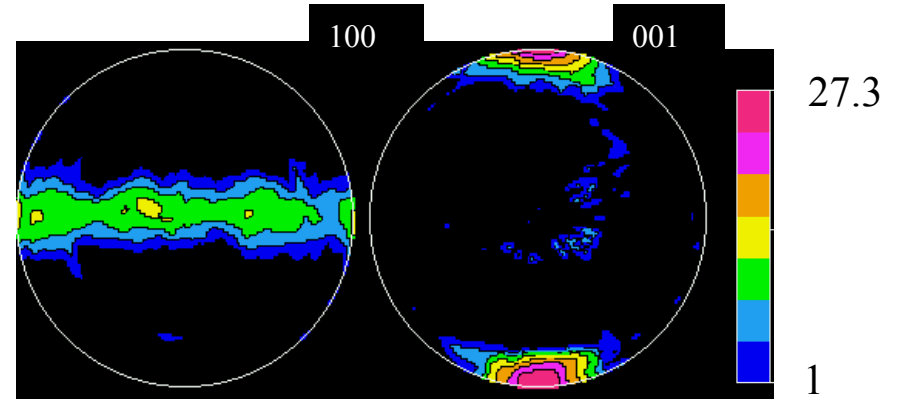
Texture parameters may deserve phylogenetic analysis

# Microstructure versus texture

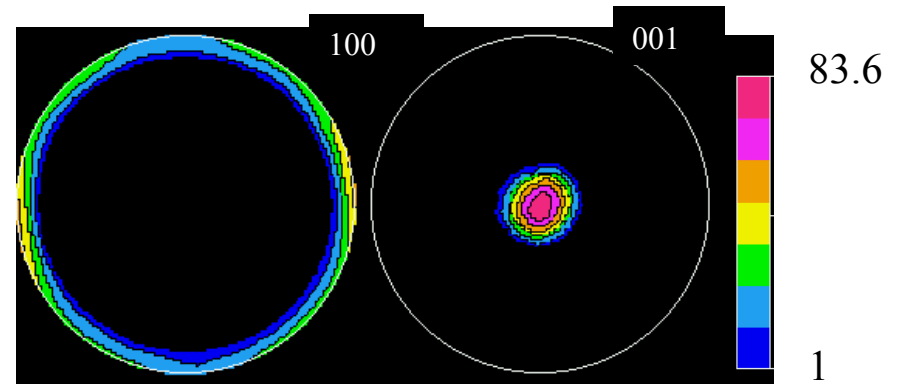


*Bathymodiolus thermophilus* (-2400m deep event mussel)

$$\langle \angle, 90 | \text{OFC} | I^{c,0} \rangle$$



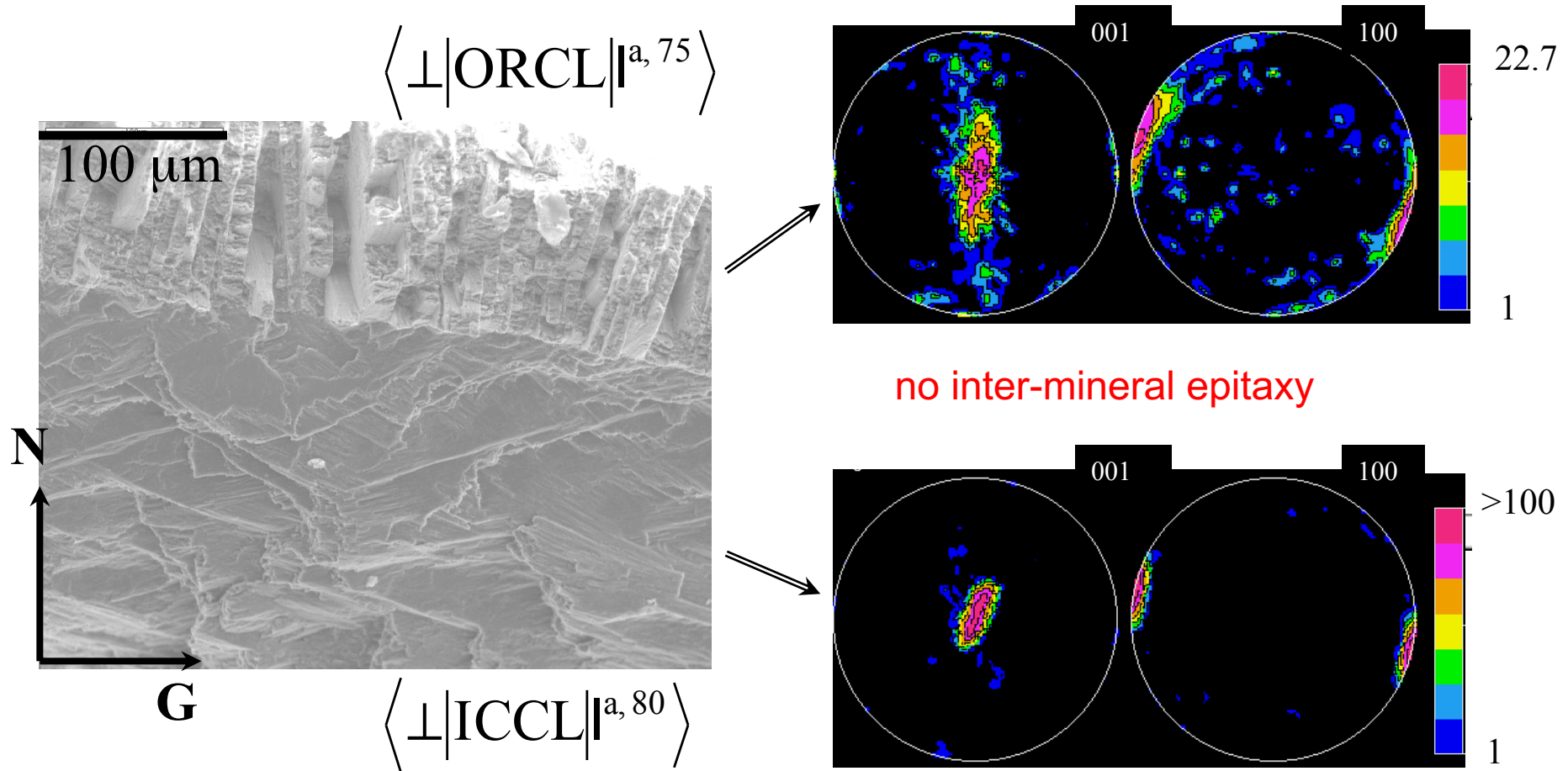
$$\langle \perp | \text{ISN} | *_{38}^{a,90} \rangle$$





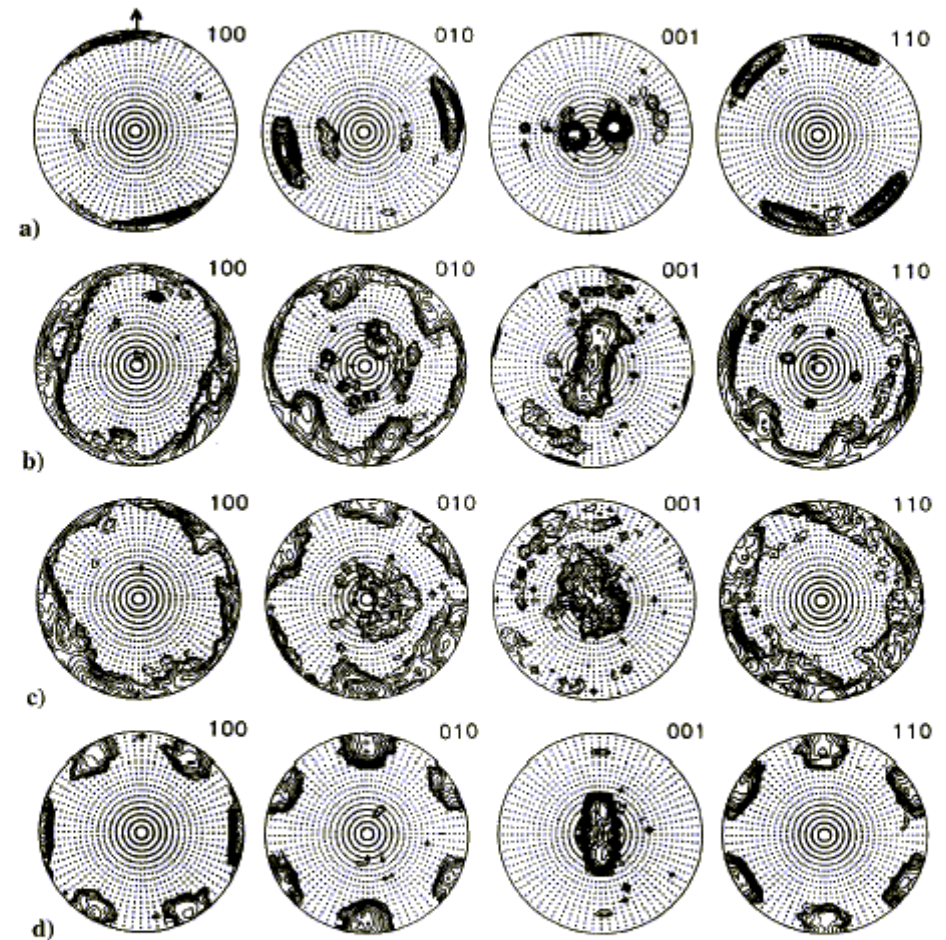
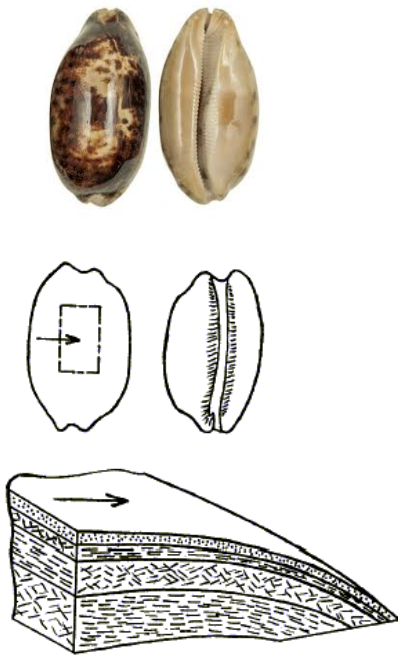
# Microstructure versus texture

*Euglandina rosea* different crystallite shapes, close orientations !



# Microstructure versus texture

Inner sheet nacre of *Cypraea testudinaria* (cowry):  
**no inter-layer epitaxy**



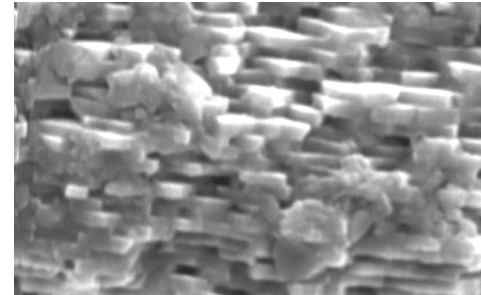
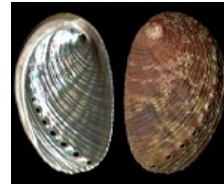
➡ Organically driven growth

# Dealing with nacre

*Gastropods*

*Columnar Nacre*

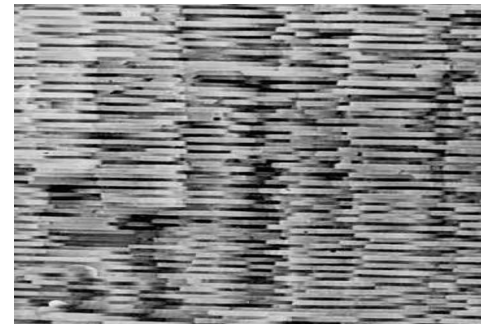
*Haliotis tuberculata* (common abalone)



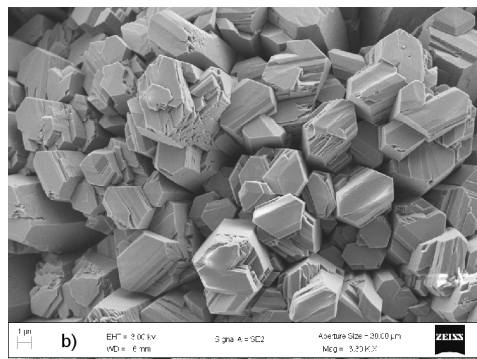
*Bivalves*

*Sheet Nacre*

*Pinctada maxima* (Mother of pearl oyster)

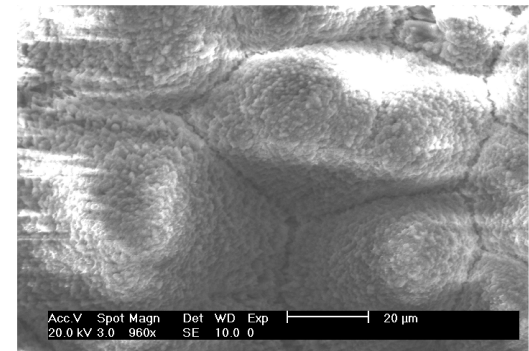


*Electrodeposited CaCO<sub>3</sub>/Ti-Al-V coatings*

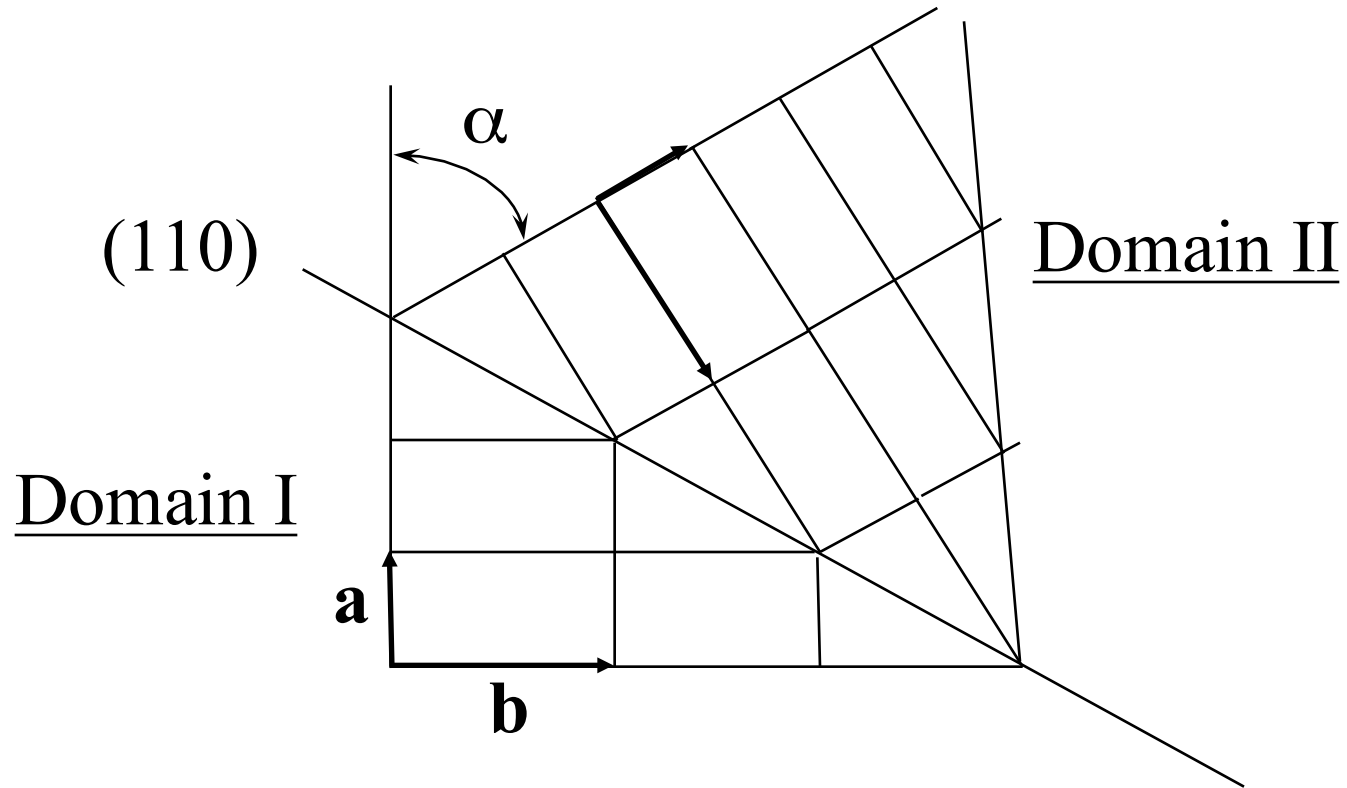


Inorganic

non-polar extract  
*Pinctada maxima*

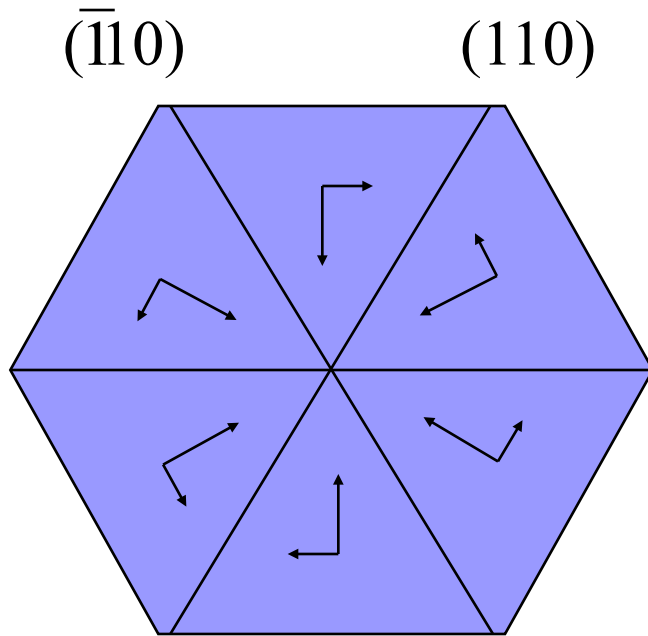


# Twining in aragonite ...

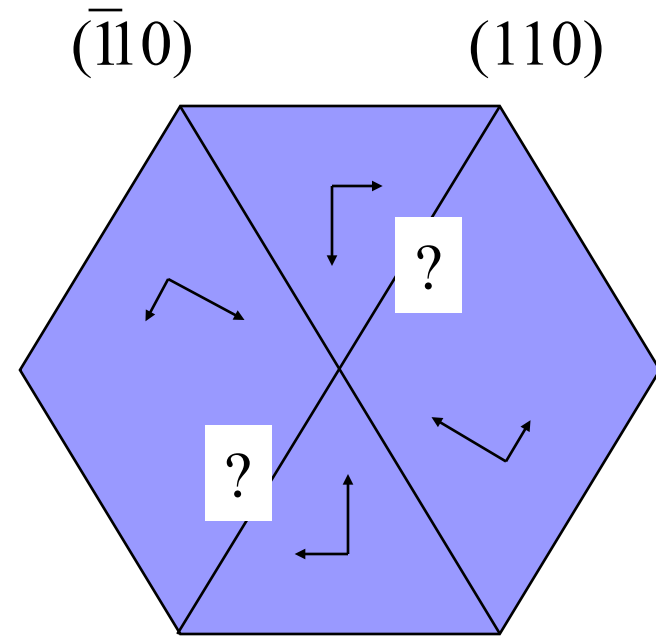


$$\alpha = 2 \arctan(a/b) = 63.8^\circ$$

... forms nacre platelets ...

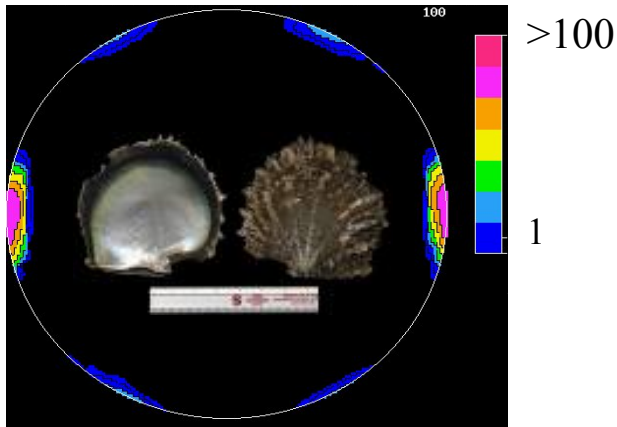
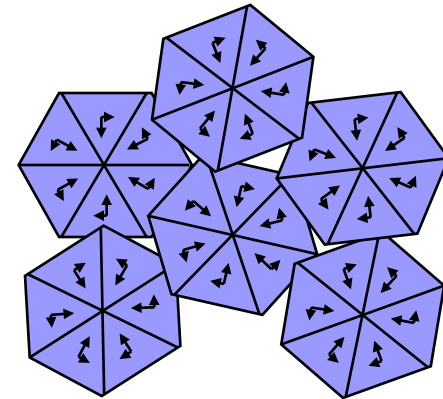
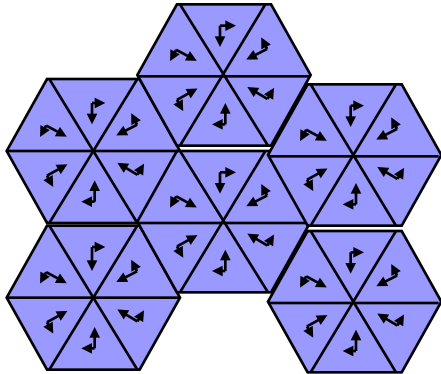


Bragg, 1937

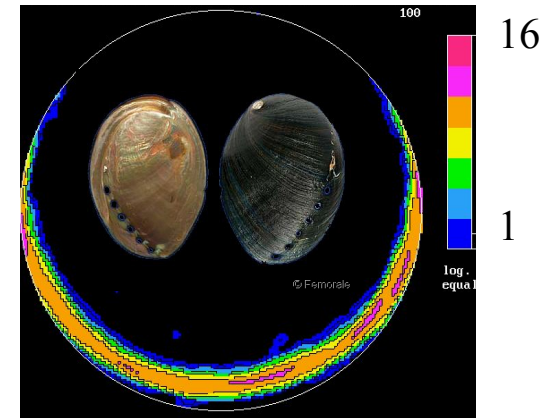


Mutvei, 1980

... that rearrange ...



*Pinctada margaritifera*  
(black pearl oyster)



*Haliotis cracherodi*  
(black abalone)

# QTA and Mollusc Phylogeny

Around 80 mollusc species (gastropods, bivalves, monoplacophoras and cephalopods), around 150 layers studied, incl. fossils

Closely related species, close textural characters, but significant variations: **textural parameters** can serve **character analysis**

**Gastropoda**

**Monoplacophora**

*Neopilina galathea* <⊥|IN|O>  
*Entemnotrochus adansonianus* <⊥|ICN|O>  
*Rokopella zografi* <⊥|IN|O>

*Atrina maurea*

*Perotrochus* <⊥|ISN|\*<sup>a,20</sup>> <⊥|ICN|O>  
*Nautilus pompilius* <⊥|ICN|\*<sup>a,75</sup><sub>61</sub>>

**Cephalopoda**

*Nautilus macromphali* <⊥|ISN|\*<sup>a,95</sup>> <⊥|ICN|\*<sup>a,80</sup>>  
*Pinna nobilis* <⊥|ISN|\*<sup>a,95</sup>> <⊥,15|ICN|O>

*Lampsilis*

*Scutellaster halimatus* <⊥|ISN|\*<sup>a,25</sup>> <⊥|ICN|O>  
*Haliotis* <⊥|ISN|\*<sup>a,25</sup>> <⊥|ICN|O>

*Fragum fragum*

*Conus leopardus* <⊥,15|ICCL|\*<sup>a,60</sup>> <⊥|ORCL|O>  
*Tectus niloticus* <⊥|ICN|O>

*Glycymeris gigantea*

*Muricanthus nigritus* <⊥,15|ICCL|\*<sup>a,-50</sup>> <⊥,15|OSP|O>  
*Tectus pyramis* <⊥,15|OSP|O>

*Spondylus princeps*

*Cyclophorus woodianus* <⊥|IRCL|\*<sup>a,20</sup>>  
*Turbo petholatus* <⊥,10|ICCL|\*<sup>a,45</sup>> <⊥|OSP|O>

*Paphia solanderi*

*Cypraea mus* <⊥|ICCL|O> <⊥|IP|\*<sup>a,45</sup>>  
*Phasianella australis* <⊥,20|OSiP|O>  
*Cypraea testudinaria* <⊥,15|ICCL|\*<sup>a,10</sup>>

**Bivalvia**

*Neotrigonia* sp.

*Oliva miniacea* <⊥|ISN|\*<sup>a,90</sup>> <⊥|OCCL|\*<sup>a,30</sup><sub>50</sub>>  
*Fissurella orientalis* <⊥,20|ICoCL|\*<sup>a,110</sup><sub>55</sub>>

*Pinctada margaritifera*

*Euglandina* sp. <⊥|ICCL|\*<sup>a,-80</sup>>  
*Strefa antipodensis* <⊥|ISN|\*<sup>a,90</sup>> <⊥|ICCL|\*<sup>a,90</sup><sub>17</sub>>  
*Helix aspera* <⊥|OCCL|\*<sup>a,90</sup>>

*Pinctada maxima*

*Pomatia pomatia* <⊥|ISN|\*<sup>a,90</sup>> <⊥,25|ICCL|\*<sup>a</sup><sub>58</sub>>  
*Nerita polita* <⊥,25|ICCL|\*<sup>a</sup><sub>58</sub>>

**Gastropoda**

*Ptereria penguin*

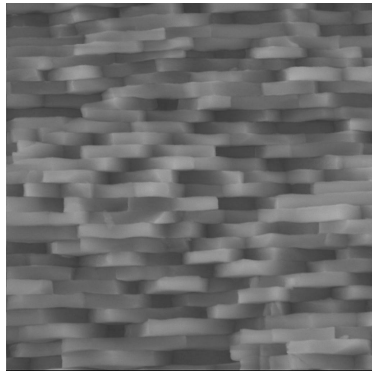
*Nerita scabricota* <⊥|ISN|\*<sup>a,30</sup>> <⊥|ICCoCL|O>

*Viana regina*

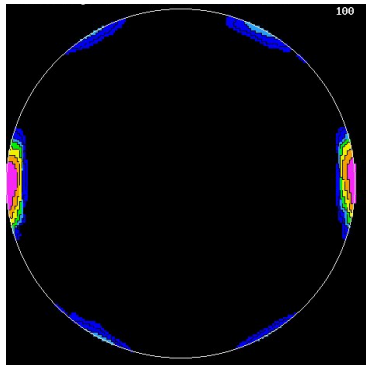
<⊥|ICCL|O> <⊥|OCCL|O> <⊥,15|OHC|O>



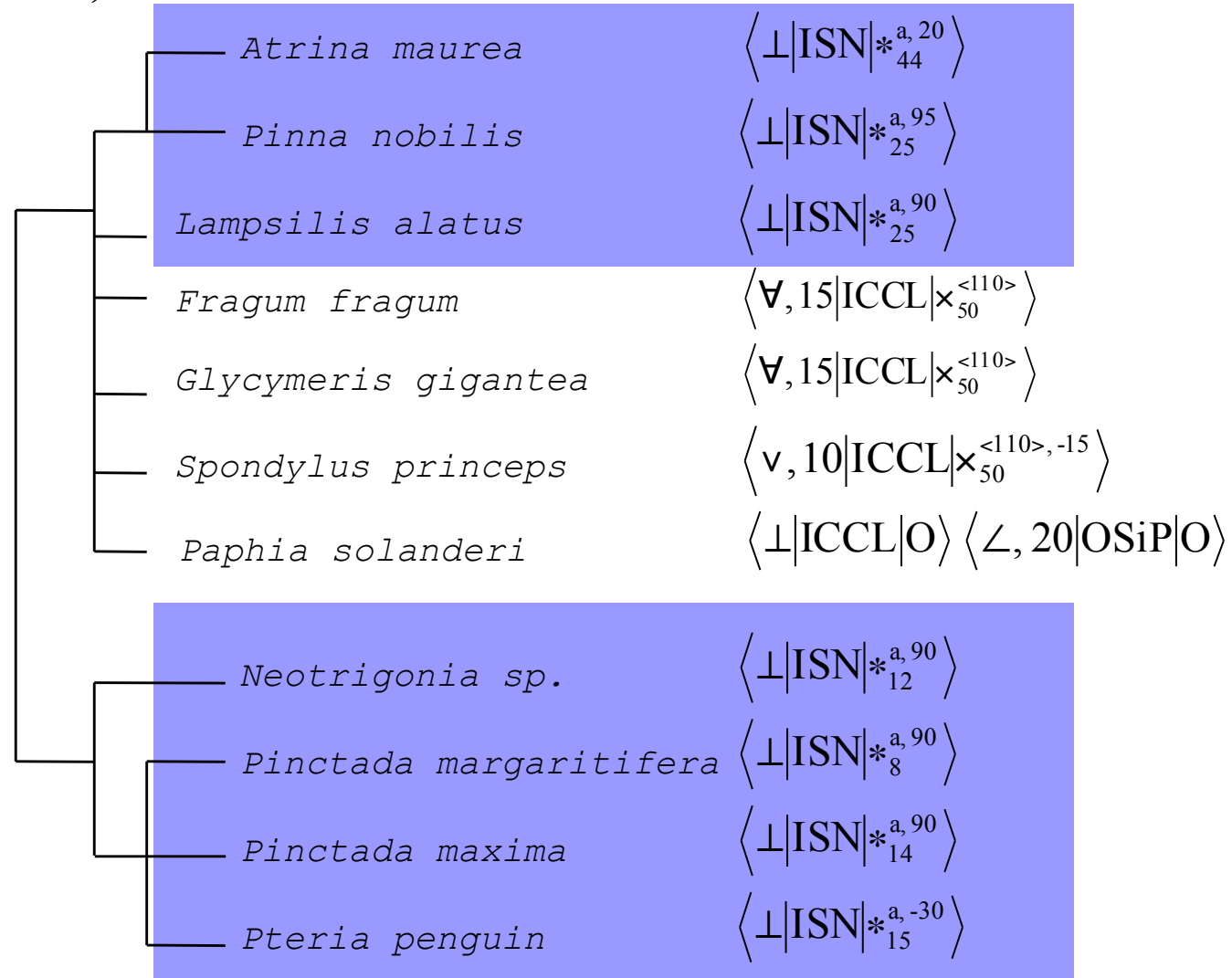
*Pinctada margaritifera*, *P. maxima* and *Pinna nobilis* nacres:  
 Bio-compatible and **osteo-inductive** for human osteoblasts (E. Lopez (MNHN, Paris))



**Bivalvia**



*P. Margaritifera*



Monoplacophora

*Neopilina galathea*

*Rokopella zographi*

*Tryblidium* sp.

Bivalvia

*Neotrigonia* sp.

*Pinctada margaritifera*

*Pinctada maxima*

*Pinna nobilis*

*Pteria penguin*

*Lampsili alatus*

*Atrina maurea*

*Acila castrensis*

*Mytilus edulis*

*Mytilus californianus*

*Bathymodiolus thermophilus*

*Anodonta cygnea*

Cephalopoda

*Nautilus pompilius*

*Nautilus macromphalus*

*Baculites* sp.

Gastropoda

*Entemnotrochus adansonianus*

*Perotrochus quoyanus*

*Haliotis cracherodi*

*Haliotis rufescens*

*Haliotis tuberculata*

*Tectus niloticus*

Nacre:

c: ⊥ a: ○

Osteoinductive

Sheet nacre

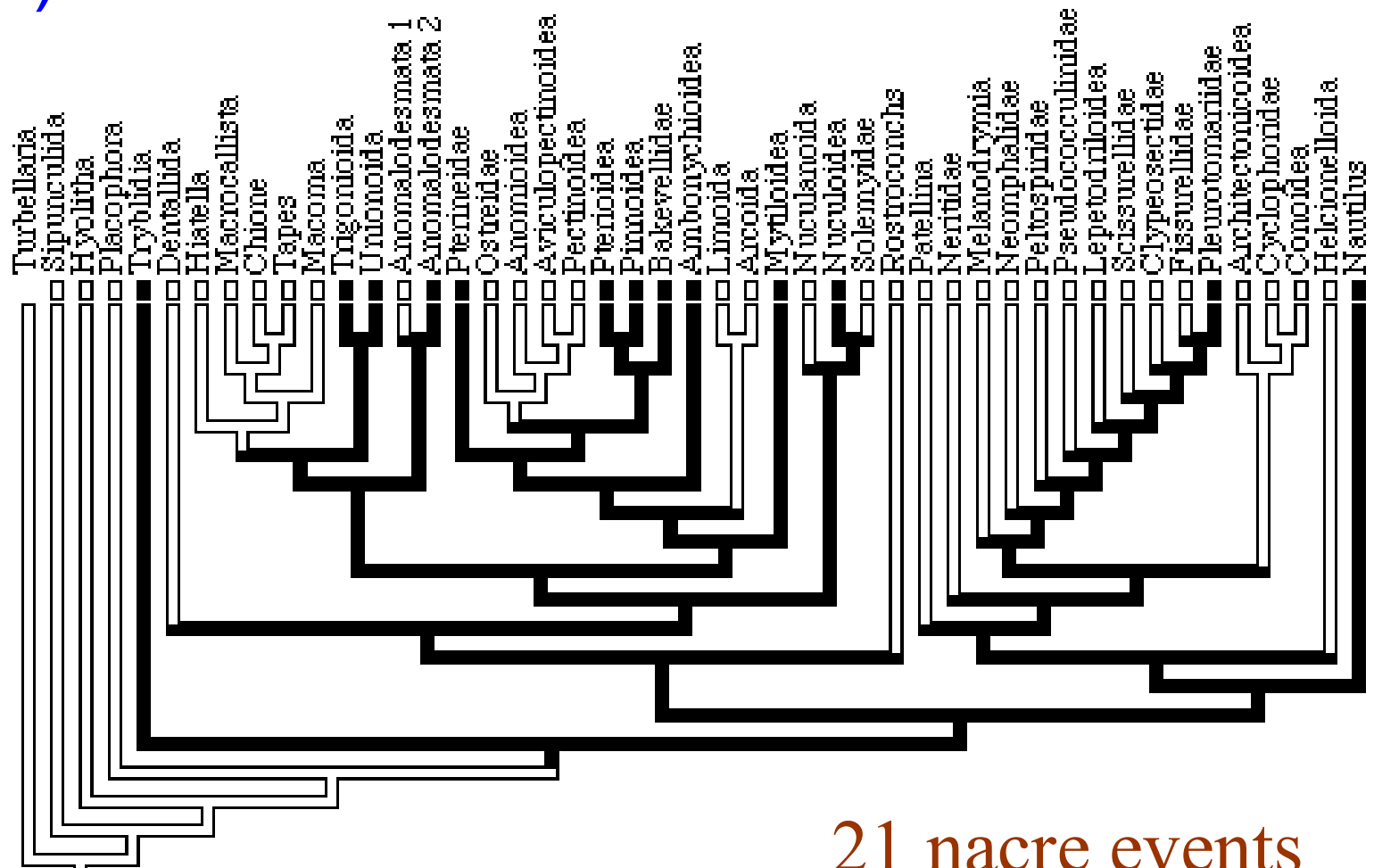
c: ⊥ a: \*

Different twin levels

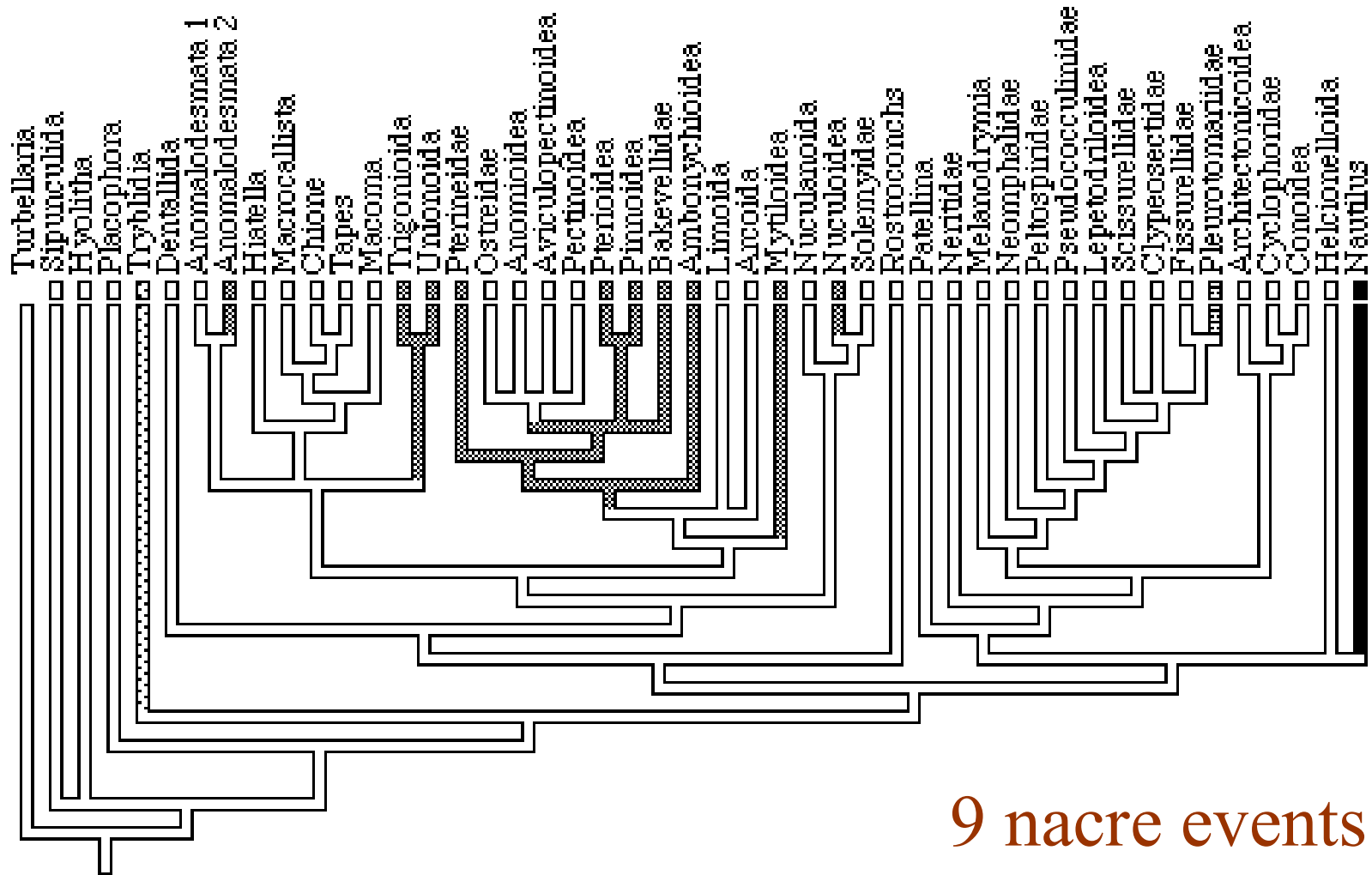
Columnar nacre: c: ⊥ a: \*

Columnar nacre: c: ⊥ a: ○

# cladistics: nacre = ancestral (Carter & Clarck, 1985)

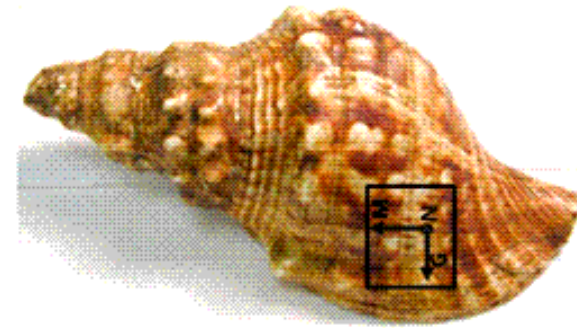


# nacre not ancestral: more parsimonious



9 nacre events

**Mediterranean sea and Eastern Atlantic carnivorous gastropod, protected (Bern conference)**

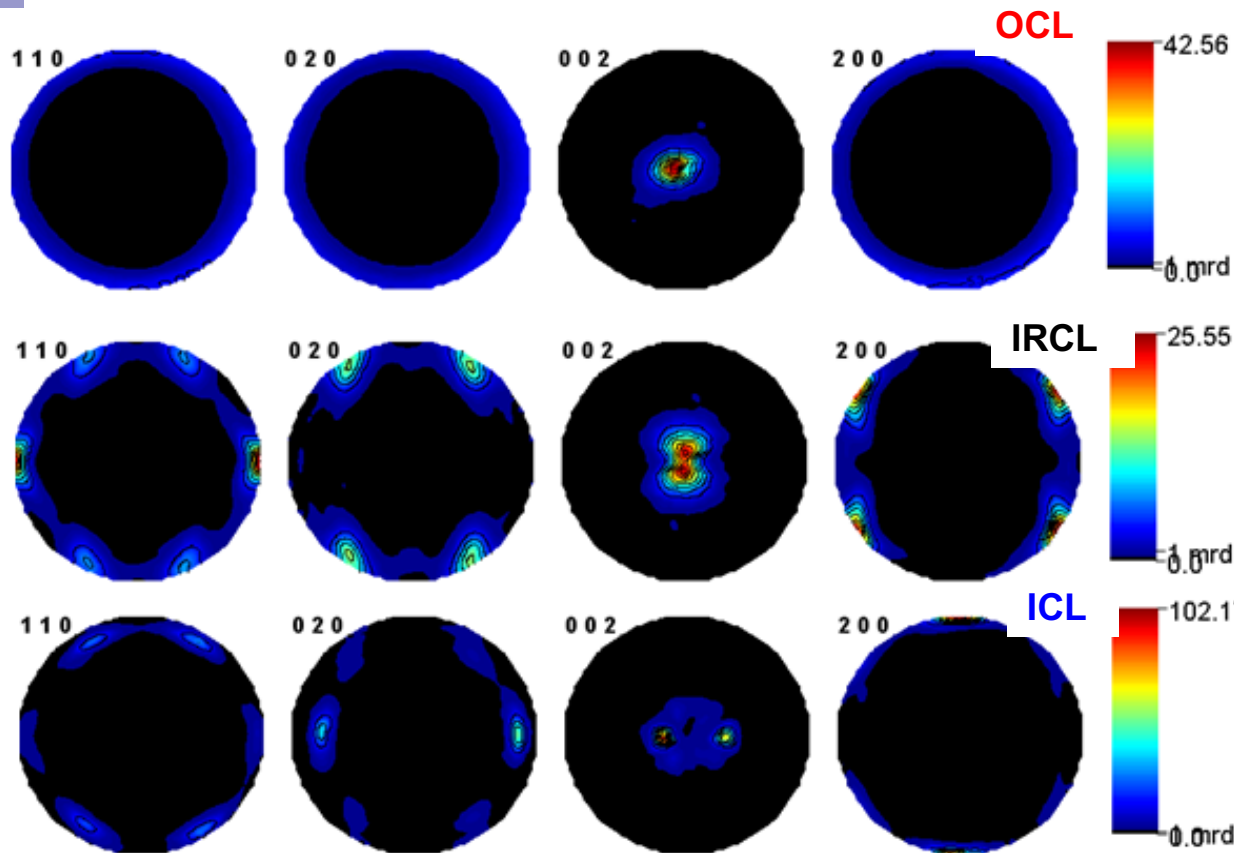


*Charonia lampas lampas*

**OCL : Outer Comarginal  
Crossed Lamellae : lamellae  
plane // M**

**IRCL : Intermediate Radial  
Crossed Lamellae : lamellae  
plane  $\perp$  M**

**ICCL : Inner Irregular Complex  
Crossed Lamellae**



**Fiber texture:  $\vec{c} \parallel N$**

**Split of  $\vec{c}$  axes around N  
+ two contributions //  
(G,N) plane.**

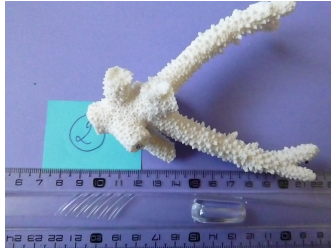
**Split of  $\vec{c}$  axes from N  
+ two contributions //  
(M,N) plane.**

**Texture information coherent with  
usually admitted gastropods  
phylogeny for this taxon**

# Elastic stiffnesses

<b>Single crystal</b>	160	37.3 87.2	1.7 15.7 84.8	41.2	25.6	42.7
<b>ICCL</b>	96.5	31.6 139	13.7 9.5 87.8	29.8	36.6	40.2
<b>RCL</b>	130.1	32.6 103.3	10.3 14.1 84.5	36.3	31.1	40.5
<b>OCL</b>	111.1	32.9 119	13.2 11.8 84.8	32.8	34.6	40.9

# In corals (Cnidaria) ?



*Seriatopora*



*Millepora*



*Acropora*

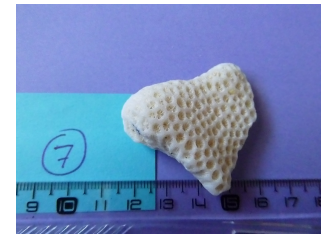


*Phaceloida*

Invariably aragonite  
Except fossils !



*Fossilized sp.*



*Stylocoeniella*



*Turbinaria*



*Fungia*



*Lobophyllia*



*Cerioda*



# Conclusions

- ➡ Intracrystalline molecules distort cell and structures
- ➡ Structures change through shell thickness
- ➡ Intercrystalline molecules modify crystal sizes
- ➡ QTA + Structural analysis deserve character analysis

But not in corals !

# Acknowledgements

S. Gascoin, CRISMAT

H.-R. Wenk, DEPS Berkeley

M. Morales, CIMAP Caen

L. Lutterotti, Trento Univ

E. Lopez, MNHN Paris

X. Bourrat, BRGM Orléans

C. Hedegaard †2009

D. Desbruyeres, MARVEL expedition (1997)

F. Lallier, HOPE expedition (1999)

EC: SOLSA

ANR: Ecocorail

Région Centre: SMAM

# Acknowledgements

University of California Museum of Paleontology, Berkeley;  
MARVEL expedition (1997) (Resp. Daniel Desbruyeres)  
Lab. d'ecologie abyssale, dept. environnement profond  
IFREMER Brest; HOPE expedition (1999) (Resp. Francois  
Lallier) Observatoire oceanologique de Roscoff  
Station Biologique Roscoff;

H.-R. Wenk, DEPS Berkeley

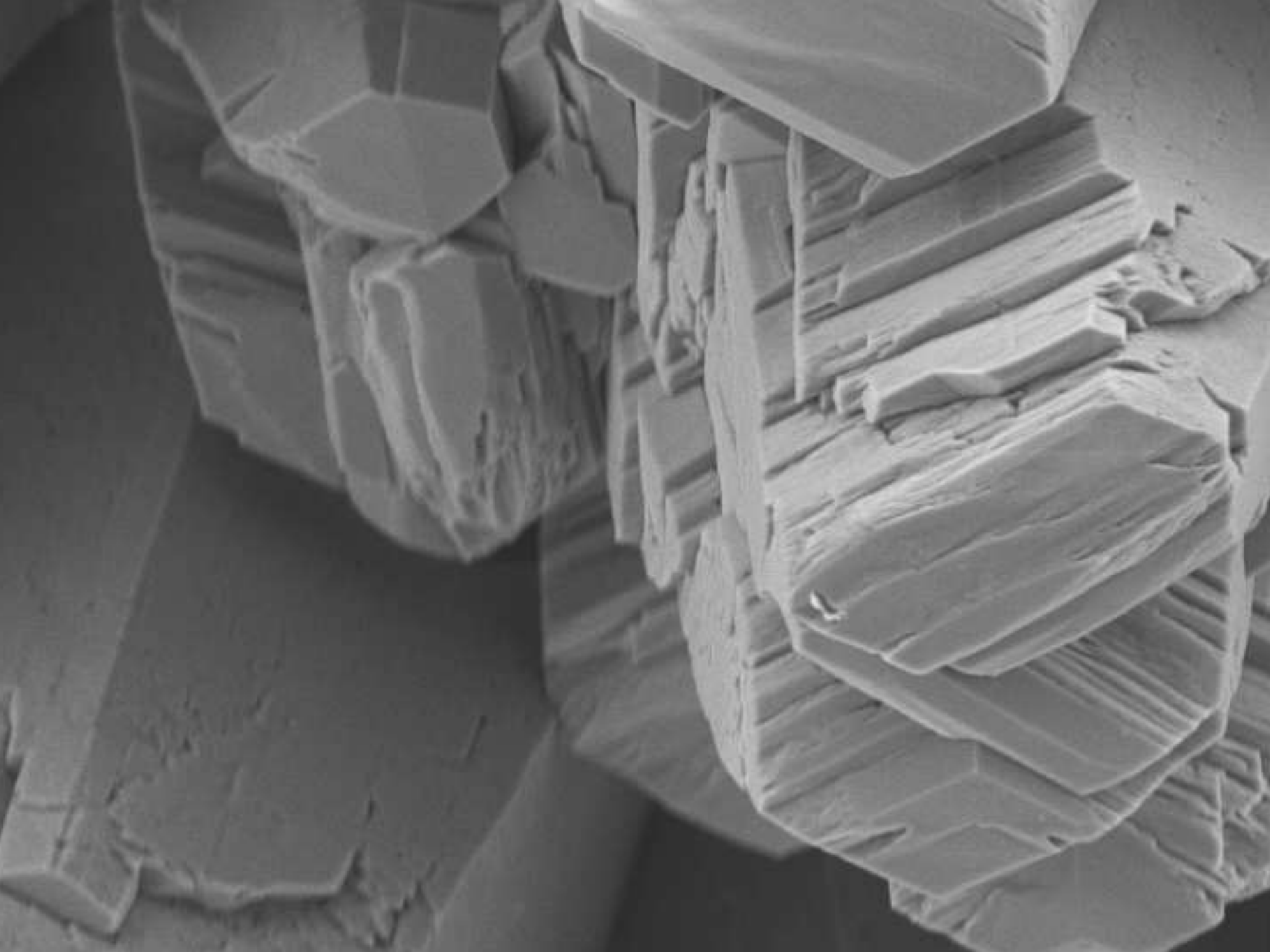
M. Morales, CIMAP Caen

L. Lutterotti, Trento Univ

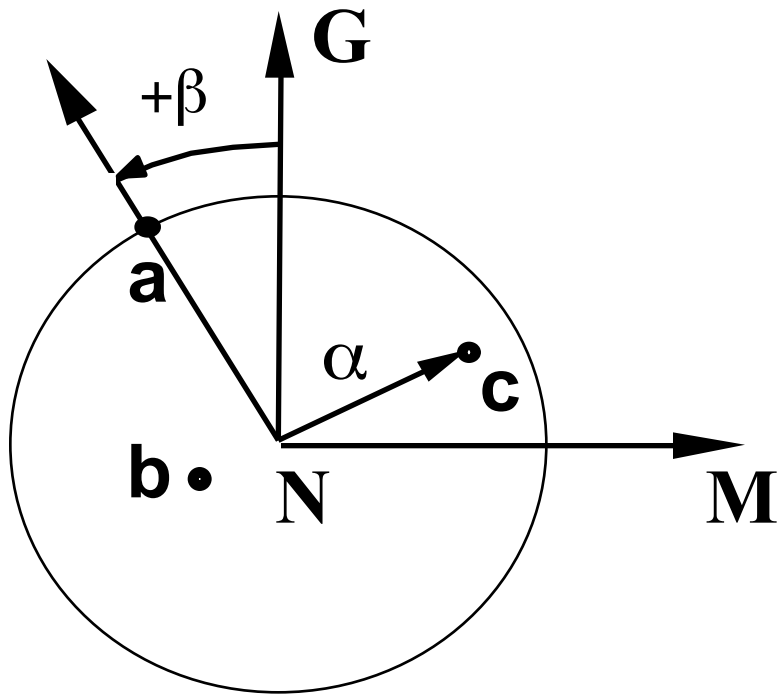
E. Lopez, MNHN Paris

Special dedicace to Claus Hedegaard,  
Aarhus Univ (1963-2009)





# Texture terms



$$\left\langle \mathbf{c}^\alpha \mid \mathbf{L} \mid \mathbf{a}_T^{\langle hkl \rangle}, \beta \right\rangle$$

**c:** ●, ∇, v, ∠, ⊥

**a:** ●, ⊙, \*, ×, |

**L:** ISN, ICN, ICCL

**T:** % twinned volume

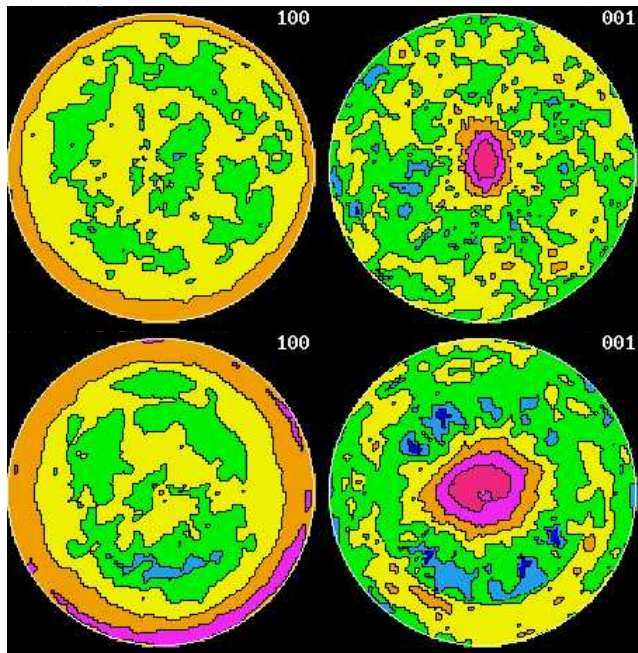
**<hkl>:** direction in (G,M)

# A link to mollusc ancestors

## Calcitic fossils: trichites

- Fragments of the large bivalve *Trichites* relatively abundant in shallow marine sediments from the Middle to Upper Jurassic of Europe, Asia and Africa
- Entire individuals are rare and the palaeobiology of the genus is poorly understood because of this
- Studied specimens are thick, some fragments up to 3 cm in thickness, composed of a coarse simple prismatic calcite
- Taxonomic position of *Trichites* remains problematic: pinnoids ?

## Pinnoid and Pteroid prismatic layers



*Pinna nobilis*

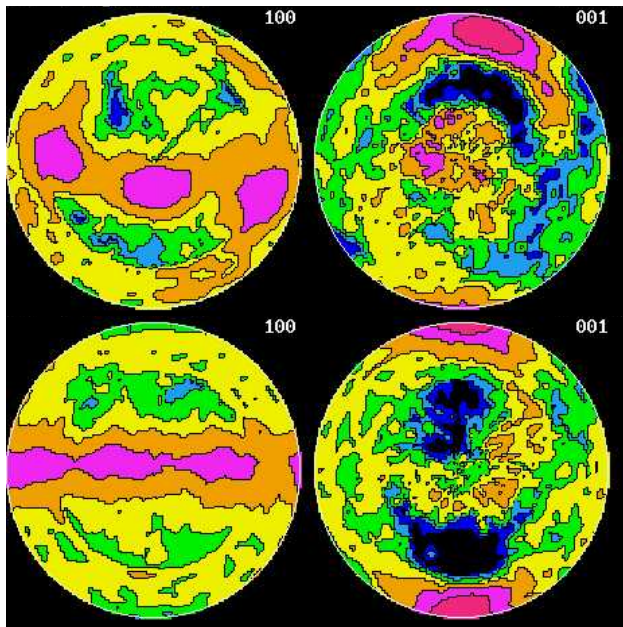


c-axes // N  
a-axes at random

*Pteria penguin*



## Mussels prismatic layers



*Mytilus edulis*

c-axes  $\angle$  **N**

a-axes single-crystal like

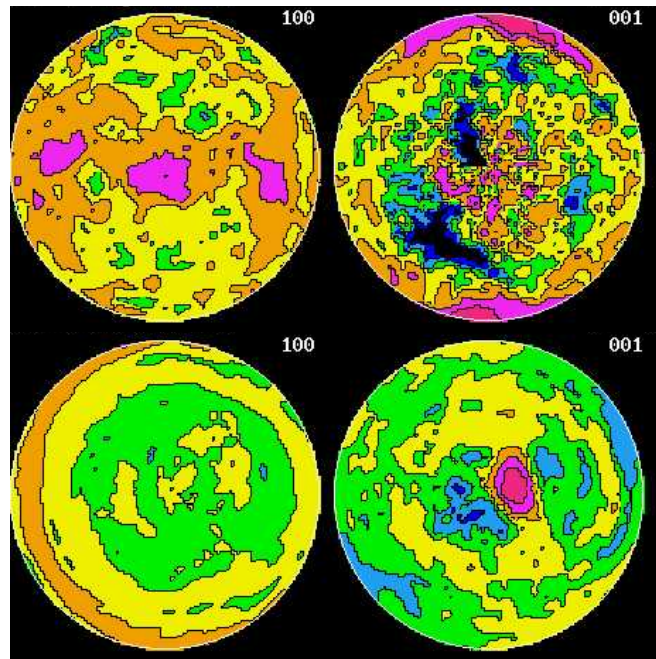
c-axes  $\perp$  **N**,  $\parallel$  **G**

*Bathymodiolus*

*thermophilus*



## Scallop and trichite prismatic layers



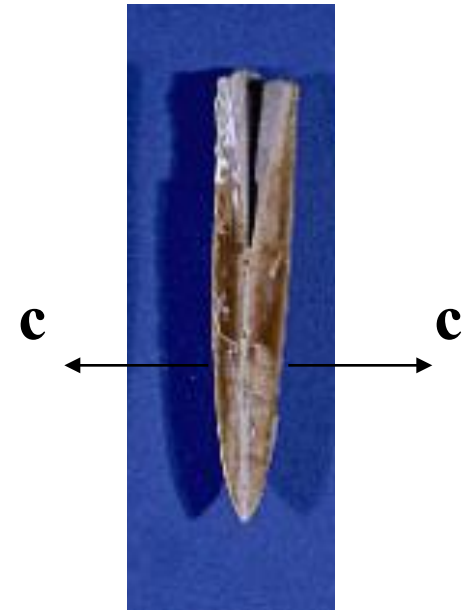
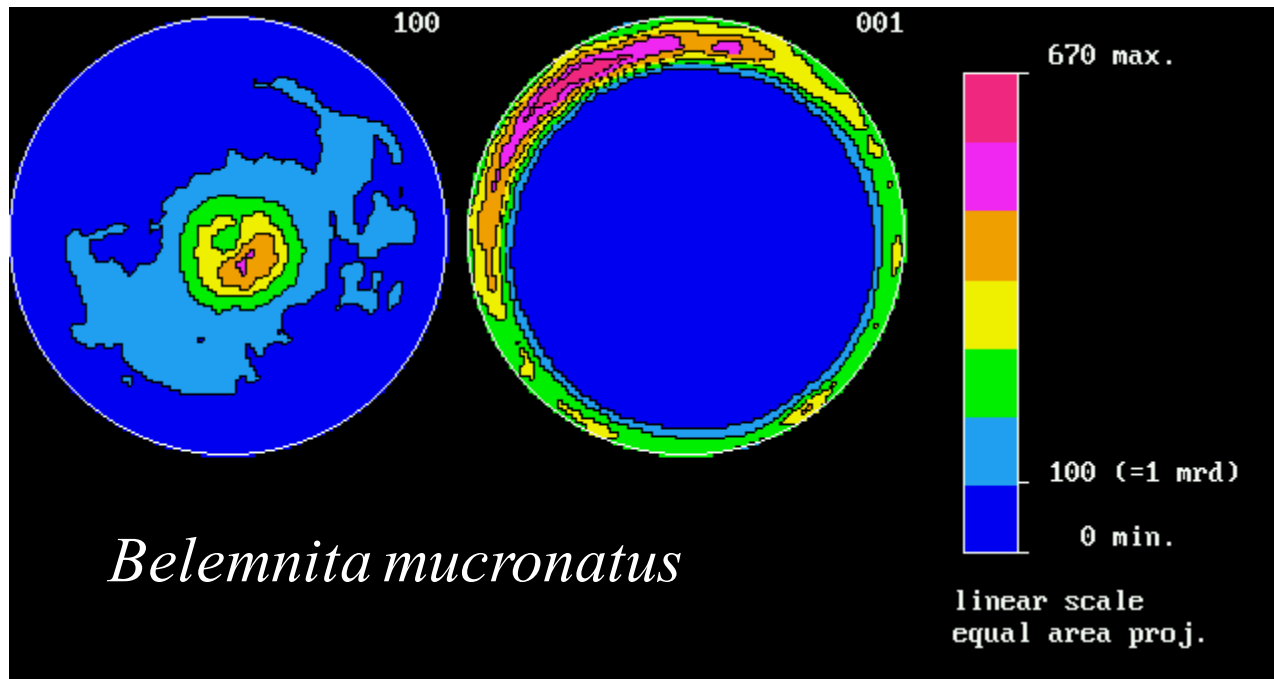
*Amusium parpiraceum*  
(scallop)  
c-axes  $\perp$  **N**, // **G**  
a-axes single-crystal like

*Trichites*  
(fossil)  
c-axes  $\angle$  **N**  
a-axes random

	Layer type	ODF Max (mrd)	ODF min (mrd)	RP0 (%)	RP1 (%)	c-axis	a-axis	{001} Max (mrd)	F <sup>2</sup> (mrd <sup>2</sup> )	- S
<i>Pinna nobilis</i>	OP	303	0	50	29	// N	random	68	29	2.3
<i>Pteria penguin</i>	OP	84	0	29	15	// N	random	31	13	1.9
<i>Amussium parpiraceum</i>	OP	330	0	53	33	// G	<110> // M	20	31	2.6
<i>Bathymodiolus thermophilus</i>	OP	63	0	25	18	// G	// M	27	13	1.9
<i>Mytilus edulis</i>	OP	207	0	41	25	75° from N	<110> // M	23	21	2.2
<i>Trichites</i>	P	390	0	52	28	15° from N	random	56	41	2.2
<i>Crassostrea gigas</i>	IF	908	0	45	31	35° from N	// M	>100	329	5.1

No DNA is available on fossils like *Trichites*, but *Trichite's* textural parameters are close to the ones of *pinnoids* or *pteriods*: interesting for the **classification of extinct species**

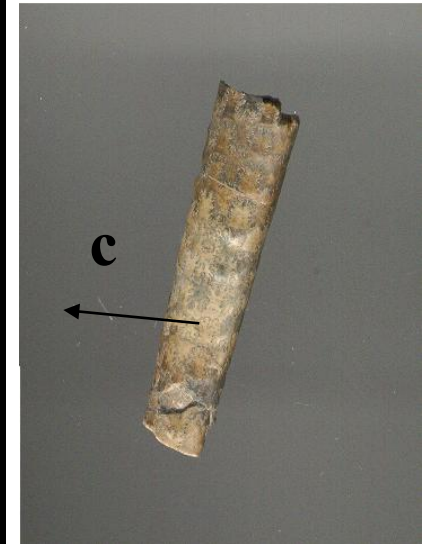
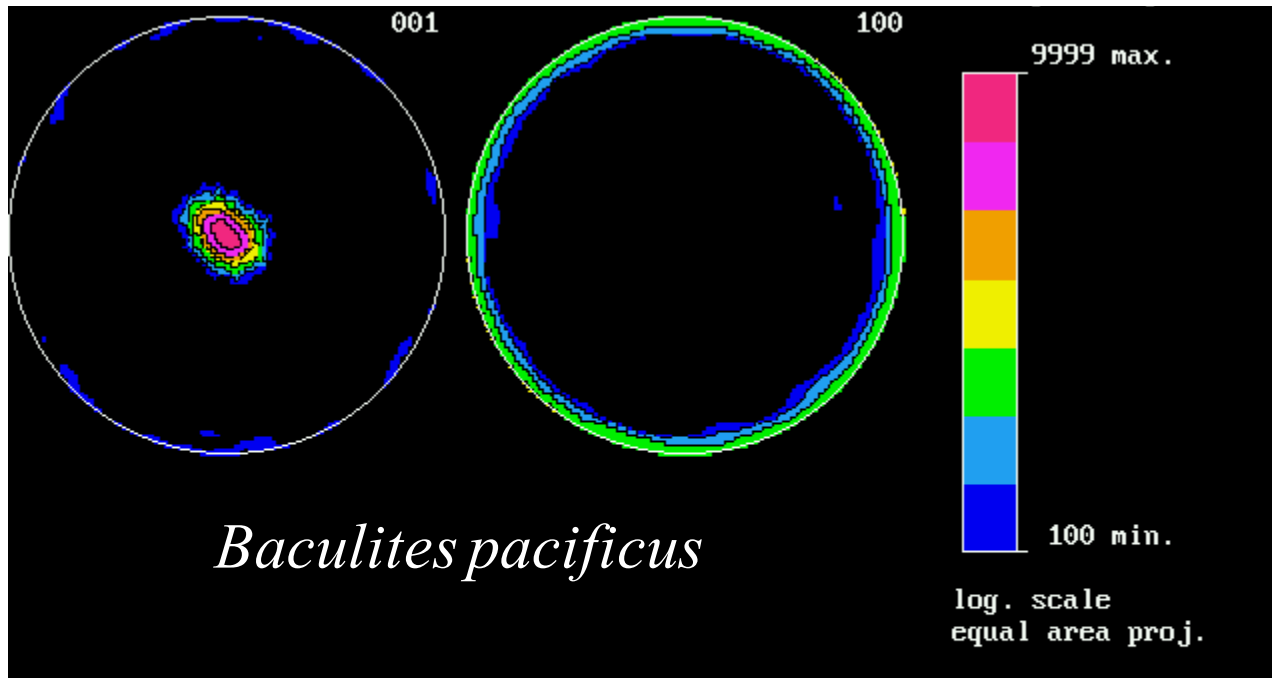
## Calcitic fossils: *Belemnites*: Belemnoidea



**c**-axes perp. to the shell: as in other cephalopods

No significant phylogenetic differences between Cretaceous (145-65 Mya) and Jurassic (200-145 Mya) species

# Aragonite fossils: *Baculites* sp.: Amonoidea, late Cretaceous

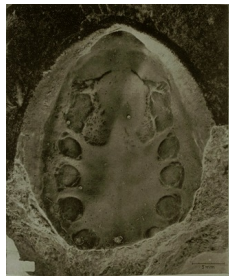


**c**-axes perp. to the shell: as in other cephalopods,  
strong **c**-calcite to **c**-aragonite fossils interaction

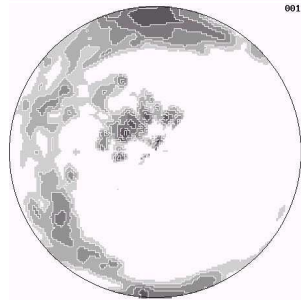
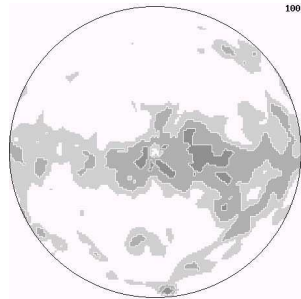
Is nacre the ancestor form ?

# Recrystallized Aragonite ? *Pilina unguis*: Tryblidiidae Monoplacophora, Paleozoic (550-250 Mya)

{100}



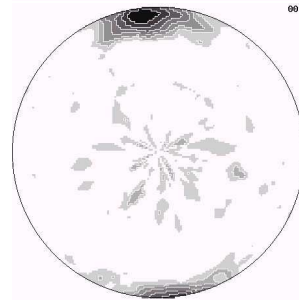
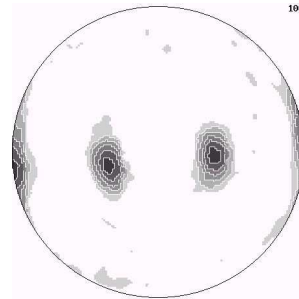
{001}



$$\langle \angle, 90 | \text{IFC} | *^{<100>} \rangle$$

*Pilina unguis*

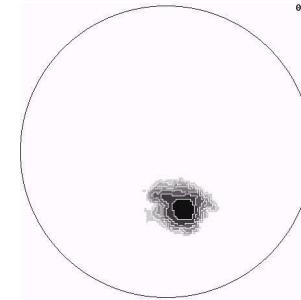
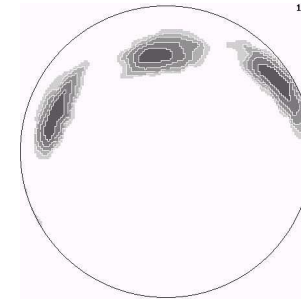
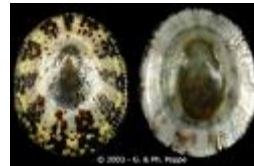
Recrystallised  
aragonite ?  
(Erben 1968)



$$\langle \angle 90 | \text{IRFC} | *_{50}^{<110>, 90} \rangle$$

*Cellana testudinaria*

Rather original  
foliated calcite ?



$$\langle \angle 30 | \text{IRFC} | *_{50}^{<110>, 90} \rangle$$

*Crassostrea gigas*

Nacre ancestor ?

# Structural distortions from x-rays

**Aplanarity of carbonate groups in  
 $\text{CaCO}_3$**

$$\Delta Z_{\text{C-O1}} = c(z_{\text{C}} - z_{\text{O1}})$$

*Calcite*

*Biogenic  
aragonite*

*Mineral  
aragonite*

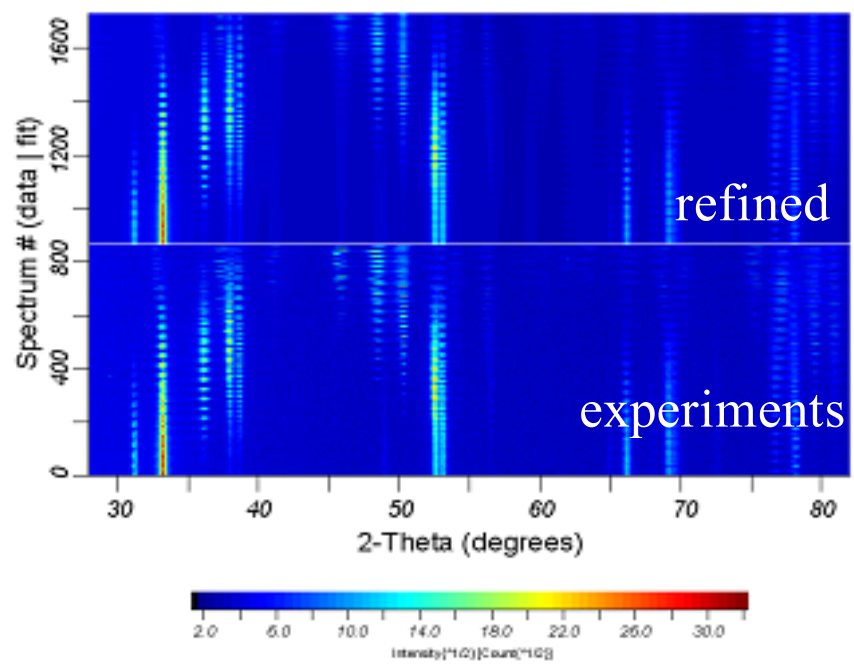
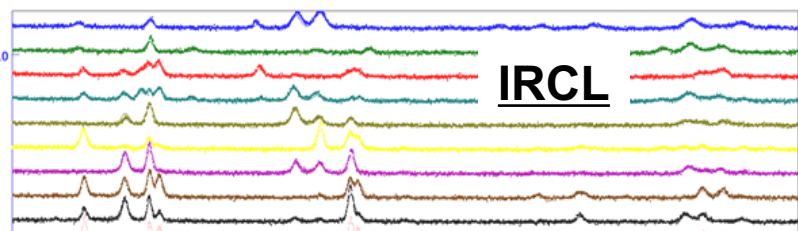
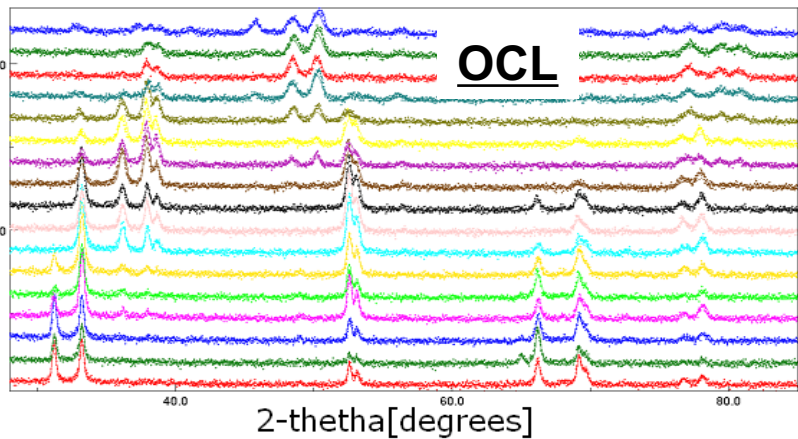
$0 \text{ \AA}$

*Intermediate,  
more distorted  
?*

$0.05744 \text{ \AA}$

**How to probe this ?**

Synchrotron (Pokroy & Zolotoyabko), but also  
Lab XRD, in the Combined Analysis frame



layer	OCL	IRCL	ICCL	
a (Å)	4.98563(7)	4.97538(4)	4.9813(1)	
b (Å)	8.0103(1)	7.98848(8)	7.9679(1)	
c (Å)	5.74626(3)	5.74961(2)	5.76261(5)	
$\Delta V/V$	1.05 %	0.62 %	0.71 %	
OD maximum (m.r.d.)	299	196	2816	
OD minimum (m.r.d.)	0	0	0	
<b>Texture index (m.r.d.<sup>2</sup>)</b>	<b>42.6</b>	<b>47</b>	<b>721</b>	
OD reliability factors	$R_w$ (%)	14.3	11.2	32.5
	$R_B$ (%)	15.6	12.7	47.8
Rietveld reliability factors	GoF (%)	1.72	1.72	3.05
	$R_w$ (%)	29.2	28.0	57.3
	$R_B$ (%)	22.9	21.7	47.2
	$R_{exp}$ (%)	22.2	21.3	32.8

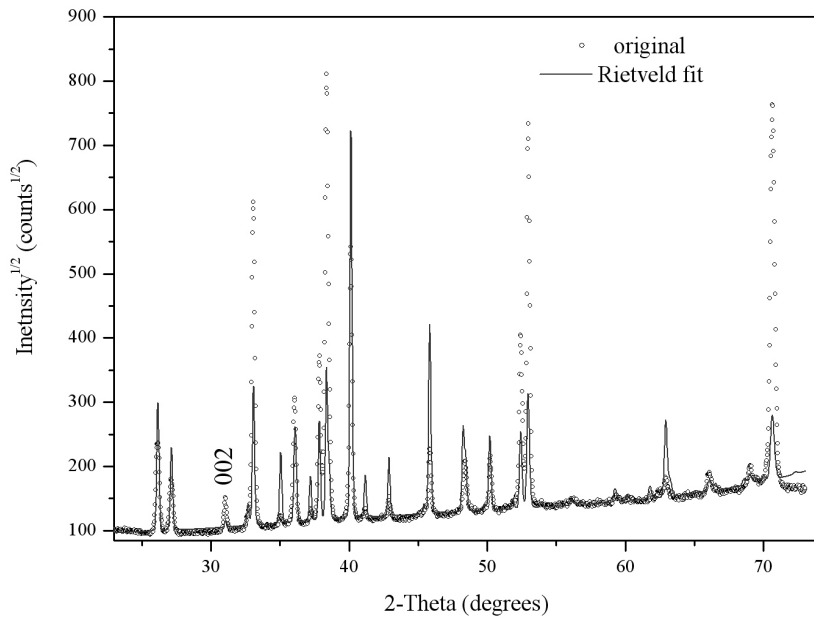
**Largest crystallite organisation closer to the animal**

		Geological reference	<i>Charonia lampas</i> OCL	<i>Charonia lampas</i> IRCL	<i>Charonia lampas</i> ICCL
a (Å)		4.9623(3)	4.98563(7)	4.97538(4)	4.9813(1)
b (Å)		7.968(1)	8.0103(1)	7.98848(8)	7.9679(1)
c (Å)		5.7439(3)	5.74626(3)	5.74961(2)	5.76261(5)
Ca	y	0.41500	0.41418(5)	0.414071(4)	0.41276(9)
	z	0.75970	0.75939(3)	0.76057(2)	0.75818(8)
C	y	0.76220	0.7628(2)	0.76341(2)	0.7356(4)
	z	-0.08620	-0.0920(1)	-0.08702(9)	-0.0833(2)
O1	y	0.92250	0.9115(2)	0.9238(1)	0.8957(3)
	z	-0.09620	-0.09205(8)	-0.09456(6)	-0.1018(2)
O2	x	0.47360	0.4768(1)	0.4754(1)	0.4864(3)
	y	0.68100	0.6826(1)	0.68332(9)	0.6834(2)
	z	-0.08620	-0.08368(6)	-0.08473(5)	-0.0926(1)
$\Delta Z_{C-O1}$ (Å)		0.05744	0.00029	0.04335	0.1066

$\Delta Z_{C-O1}$  ↗ from outer to inner layer correlated to the organic macromolecules presence + coherent with the  $\Delta$  of texture strength → control loss from macromolecules on aragonite stabilization farther from animal!

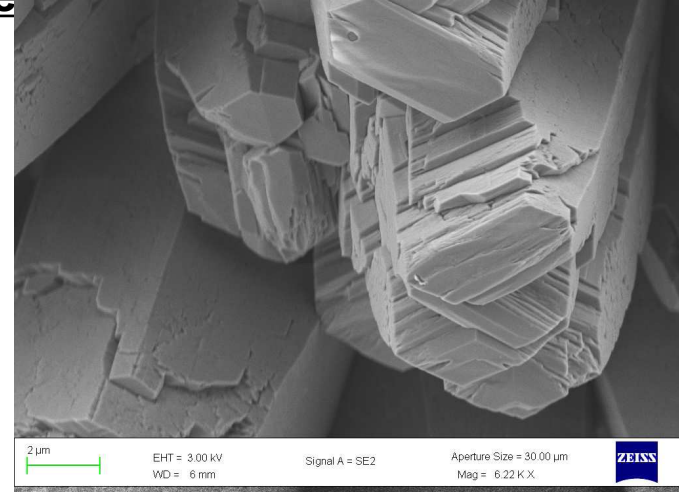
**Anisotropic cell distortions yet observed in biogenic aragonite powderised layers**



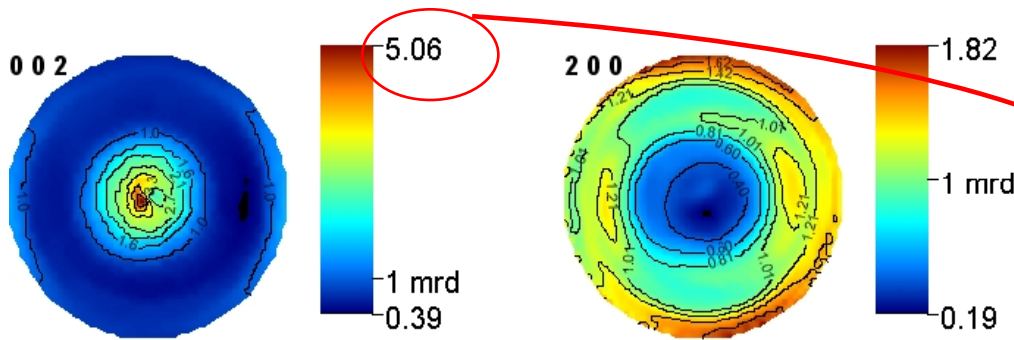


**Nonoptimized deposited films:**  
**Corresponding X-ray diagram:**  
 cauliflower-shaped aragonite +  
 only aragonite is evidenced with  
 calcite + vaterite  
 a pronounced (001) texture

## I grade Ti foils by electrodeposition



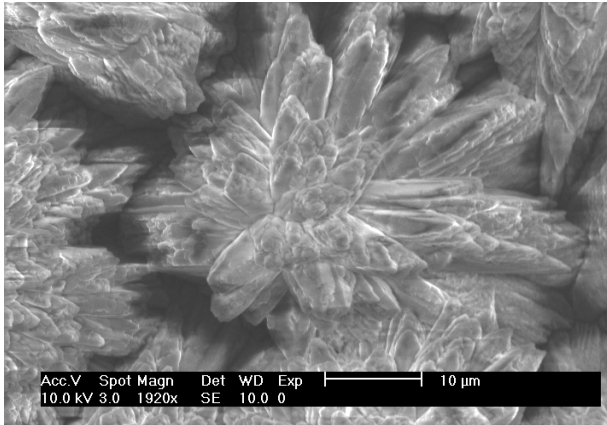
Optimized deposited films with nacre like pseudo hexagonal shaped crystals



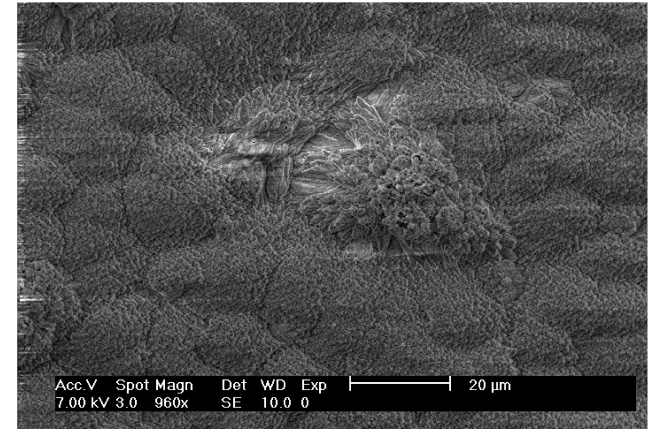
**Texture strength far from natural nacre → differences can be associated to organic driven processes**

Recalculated pole figure : <001> fiber like texture

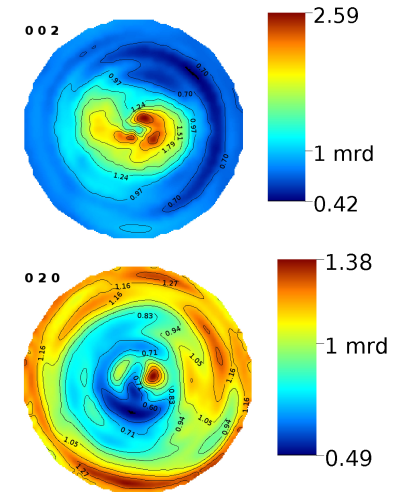
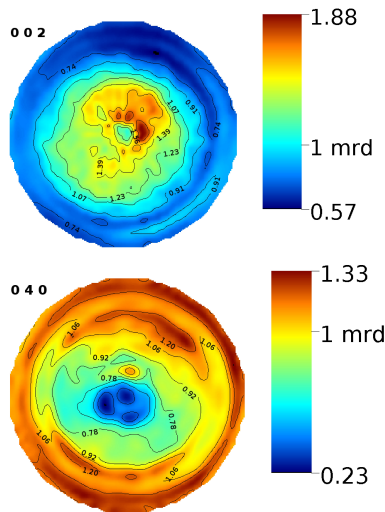
Krauss et al., *Cryst. Growth & Design* **8** (2008)



**Apolar Ethanol extracted molecules: cauliflower-shaped aragonite**



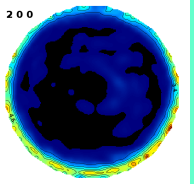
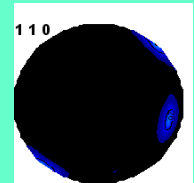
**Polar Water extraction: compact cauliflower-shaped aragonite**



**reduction of the <00l> texture  
Structural distortions ?**

# $\Delta Z_{C-01}$ (Å)

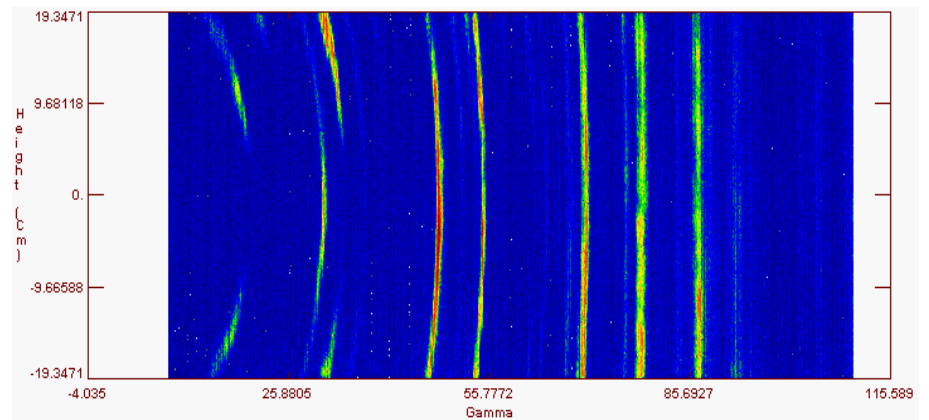
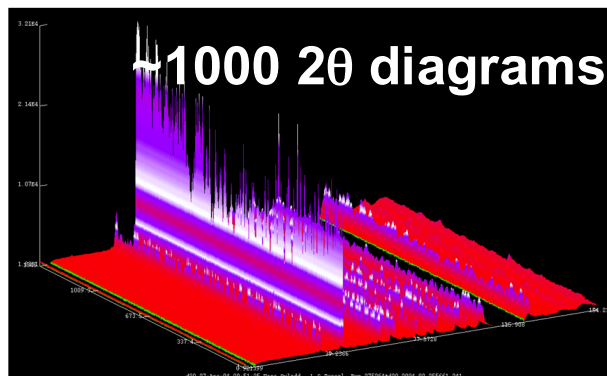
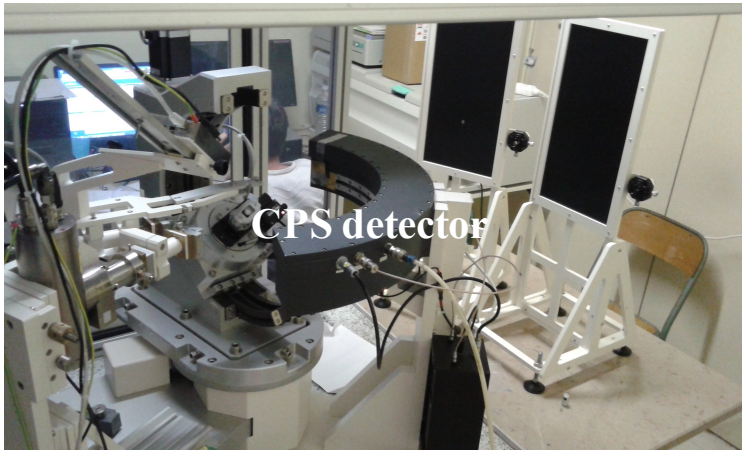
Geological reference **0.05744**

<b>Gastropods</b>	<i>Haliotis tuberculata</i> ICN		<i>Charonia lampas</i> ICCL	<i>Charonia lampas</i> IRCL	<i>Charonia lampas</i> OCL	<i>Strombus decorus</i> All layers
	<b>0.089</b>		<b>0.107</b>	<b>0.043</b>	<b>0.0003</b>	<b>0.031</b>
<b>Bivalves</b>	<i>Pinctada maxima</i> ISN		<i>Mercenaria mercenaria</i> IP	<i>Mercenaria mercenaria</i> IntP	<i>Mercenaria mercenaria</i> OP	
	<b>0,054</b>		<b>0.069</b>	<b>0.092</b>	<b>0.11</b>	
<b>Synthetic layers</b>	Inorganic	Chitosan	Non-polar Extraction		Polar Extraction	
	<b>890Å</b>	<b>1272Å</b>	10 mg/l <b>1211Å</b>	20 mg/l <b>1126Å</b>	10 mg/l <b>1284Å</b>	20 mg/l <b>1150Å</b>
<b>Crystallite size</b>						
<b>CaCO<sub>3</sub> / Ti</b>	<b>0,087</b>	<b>0.04</b>	<b>0.173</b>	<b>0.086</b>	<b>0.134</b>	<b>0.081</b>

As a result of the presence of the hydrophilic groups in the shells of *Strombus* and *Charonia*, the crystallite size is smaller than that of *Pinctada* and *Haliotis*.  
 Synthetic layers are produced in order to simulate the structure of the shells.  
 In *Pinctada*:  $\Delta Z=0.05$ , both inter- and intramolecules act

## Minimum experimental requirements:

1D or 2D Detector + 4-circle diffractometer (X-rays and neutrons)



~200 2θ diagrams

Geometric mean approach

Extracted Intensities

WIMV, E-WIMV  
Harmonics

Orientation Distribution Function

Rietveld

Structure  
+  
Microstructure  
+  
phase %

Popa-  
Balzar,  
 $\sin^2\psi$

Residual stresses  
Strain Distribution Function

Specular Reflectivity

Roughness,  
electron  
Density & EDP,  
Thickness

pole figures  
inverse pole figures

Structural parameters  
atomic positions, substitutions, vibrations  
cell parameters

Multiphased, layered samples:  
Thickness,  
Anisotropic Sizes  
and  $\mu$ -strains (Popa),  
Stacking faults (Warren),

Phase ratio (amorphous + crystalline)  
Le Bail Rietveld

Le Bail

Fresnel, Matrix (Parrat), DWBA

Combined analysis approach

## Rietveld enlarged: Structure – Texture – Stress – Phase – Microstructure – Layering analyses - Reflectivity

$$y_{ic}(\mathbf{y}) = y_{ib}(\mathbf{y}) + \sum_{\Phi=1}^{N_{\Phi}} S_{\Phi} \sum_{k=K_1}^K j_{\Phi k} L_{p_{\Phi k}} P_{\Phi k}(\mathbf{y}) |F_{\Phi k}|^2 \Omega_{i\Phi k} A_{i\Phi}(\mathbf{y})$$

$$P_k(\mathbf{y}) = \int_{\varphi} f(g, \tilde{\varphi}) d\tilde{\varphi}$$

Tensor homogeneisation, geometric mean ...